

The Nano-Hertz Gravitational Wave Background: Connection to sub-GeV dark matter

Seminar at Stockholm university, November 13th 2025

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Based on work with Sowmiya Balan, Torsten Bringmann,
Frederik Depta, Felix Kahlhöfer, Thomas Konstandin, Jonas Matuszak,
Kai Schmidt-Hoberg, Pedro Schwaller

JCAP 11 (2023) 053,
JCAP 08 (2025) 062,
and **Phys.Rev.Res. 7 (2025)**



UPPSALA
UNIVERSITET

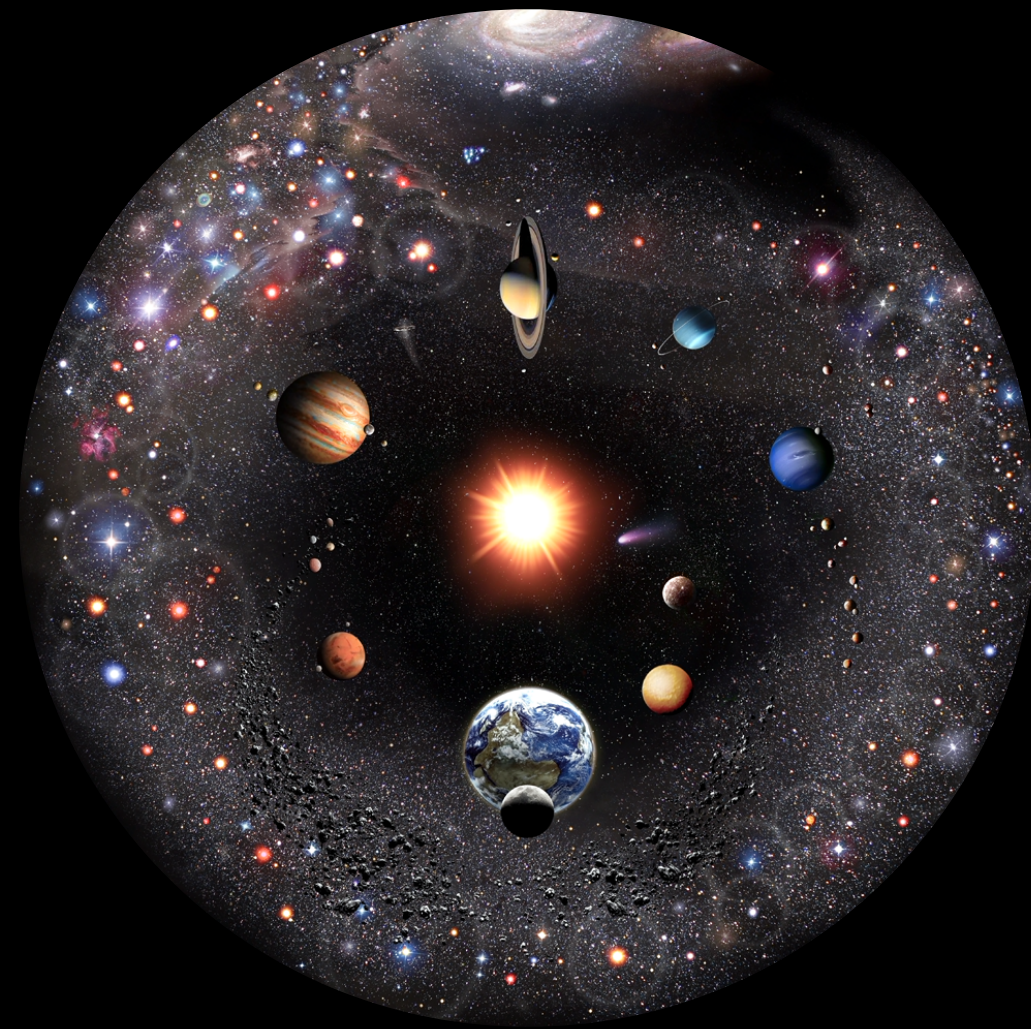
It's the end of the world as we know it (and I feel fine)



Our Solar System

PABLO
CARLOS
BUDASSI

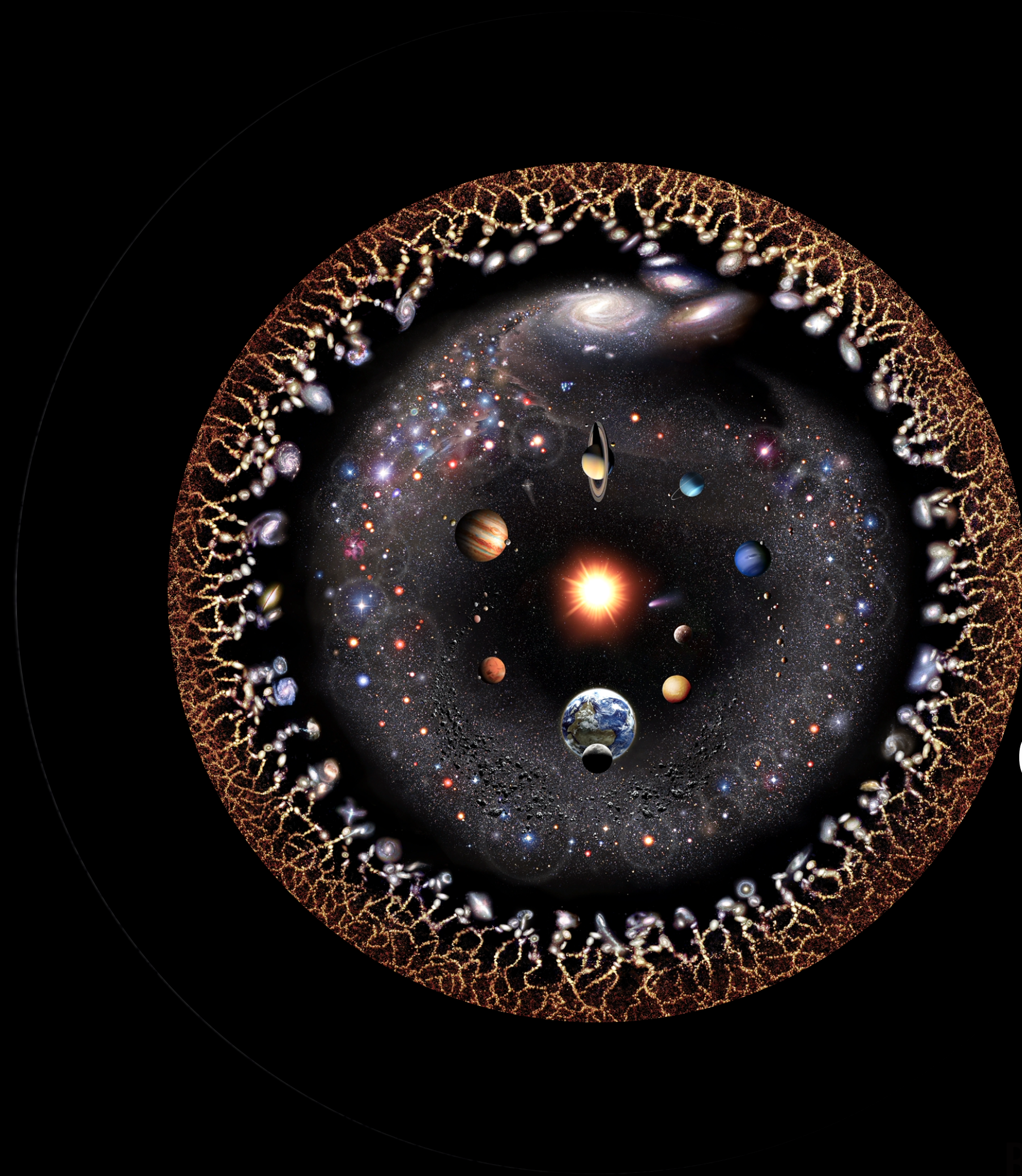
It's the end of the world as we know it (and I feel fine)



Our galaxy

PABLO
CARLOS
BUDASSI

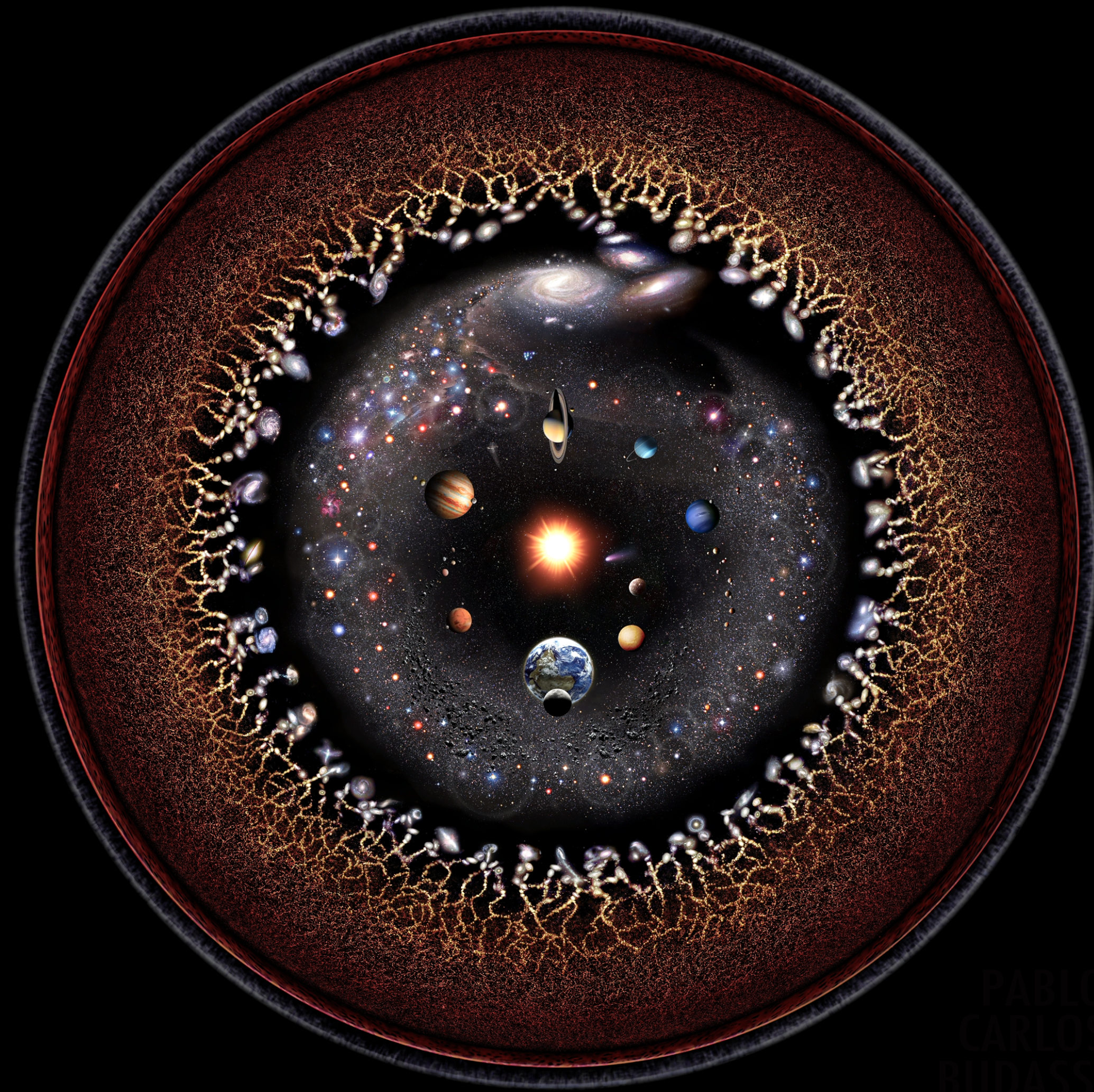
It's the end of the world as we know it (and I feel fine)



Other galaxies

PABLO
CARLOS
BUDASSI

It's the end of the world as we know it (and I feel fine)



**The CMB...
and the CGWB?**

PABLO
CARLOS
BUDASSI

At Last, There's

A globe-spanning

Astronomers detect 'cosmic bass note' of gravitational waves

Sound comes from the merging of supermassive black holes across the universe, according to scientists

Scientists 'hear' cosmic hum from gravitational waves

Gravitational waves that ripple through the universe

Scientists have observed for the first time the faint ripples caused by the motion of black holes that are gently stretching and squeezing everything in the universe

Black Holes in Space

Gravitational waves at the center of the Milky Way

Scientists reveal how black holes come from collisions

of Low-Frequency Gravitational Waves

the waves, which

and from pairs

cosmic hum from

faint ripples caused by the motion of black holes, which are stretching and squeezing everything in the universe.

A Background 'Hum' Pervades the Universe. Scientists Are Racing to Find Its Source

Astronomers are now seeking to pinpoint the origins of an exciting new form of gravitational waves that was announced earlier this year

Monster gravitational waves spotted for first time

Colossal gravitational waves—trillions of miles long—found for the first time

by studying rapidly spinning dead stars, which create giant ripples of spacetime likely from merging supermassive black holes

In a major discovery, scientists say space-time churns like a choppy sea

The mind-bending finding suggests that everything around us is constantly being rolled by low-frequency gravitational waves

it may be from merging supermassive black holes

Gravitational Waves

First Evidence of Giant Gravitational Waves Thrills Astronomers

For first time ever, scientists "hear" gravitational waves rippling through the universe

are tuning in to a never-before-seen type of gravitational waves spawned by pairs of supermassive black holes

new form of ripple in spacetime

Scientists discover that universe is a giant gravitational wave

background waves produce a hum across the whole universe

After decades of searching, astronomers have found a distinctive pattern of light, from spinning stars called pulsars, that suggests huge gravitational waves are creating gentle ripples in space-time across the universe

The results are a hum across the universe.

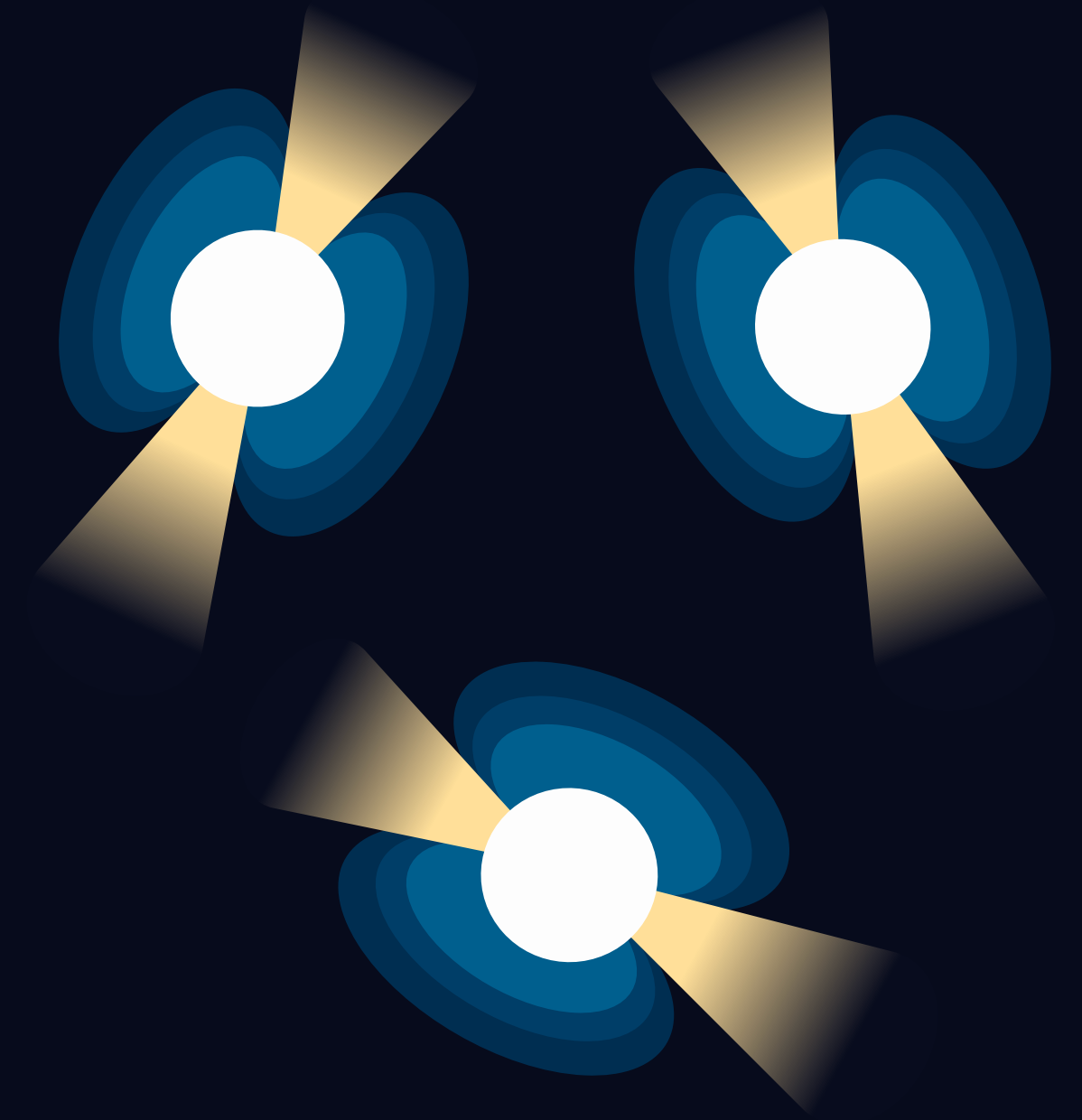


We live in the age of gravitational wave cosmology!

The working principle of a pulsar timing array



Galactic millisecond pulsars

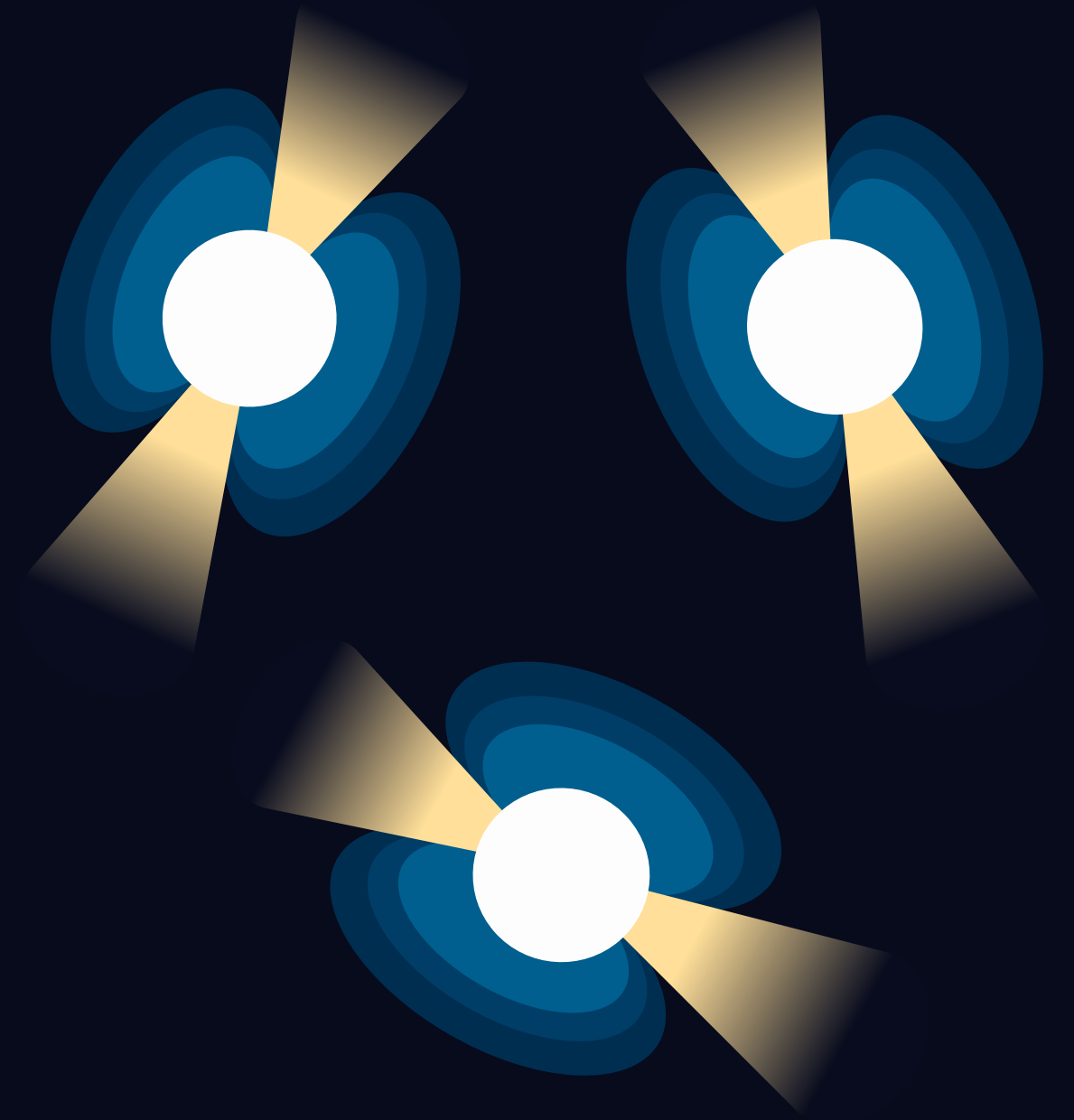


The working principle of a pulsar timing array

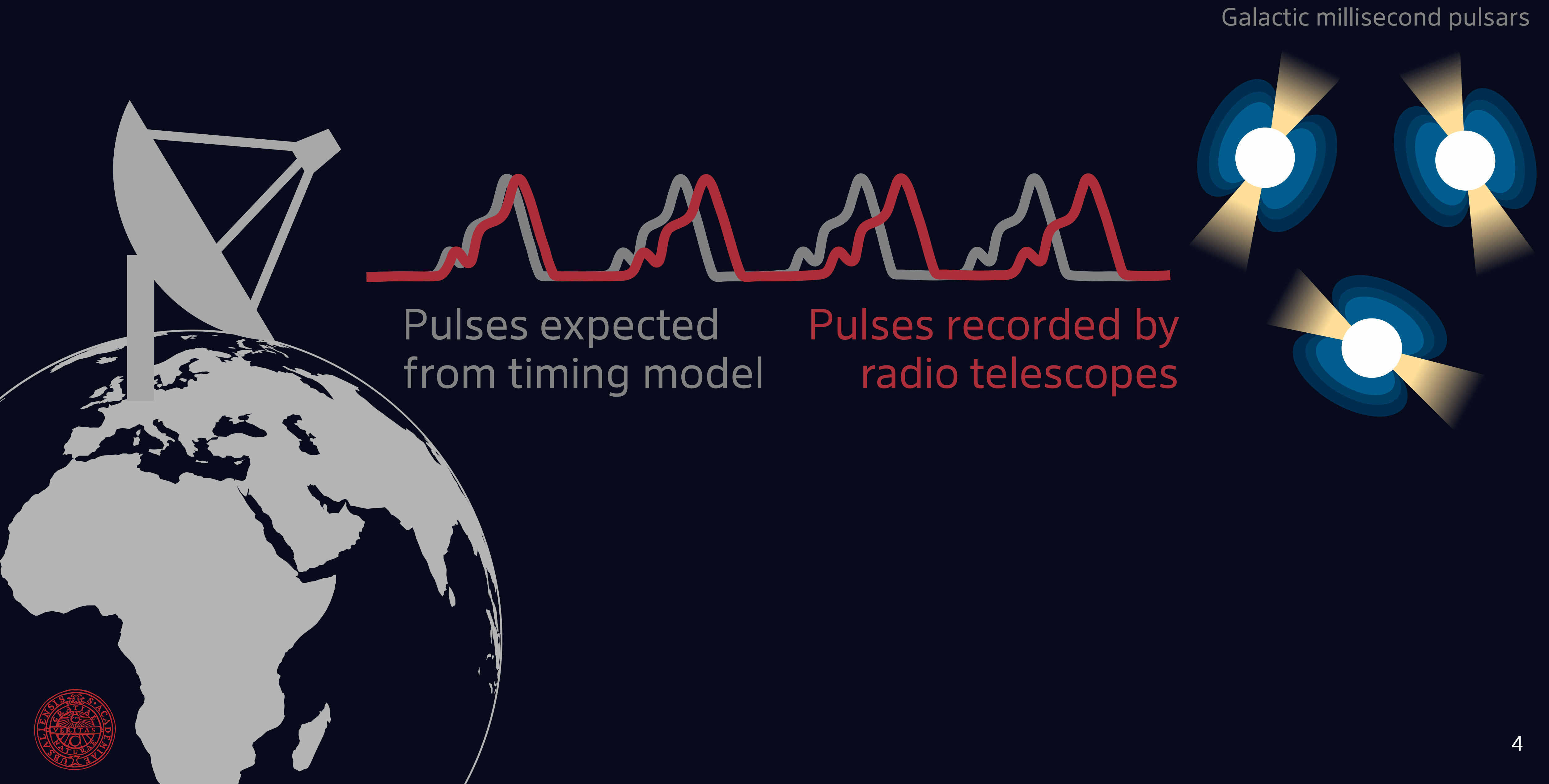


Pulses expected
from timing model

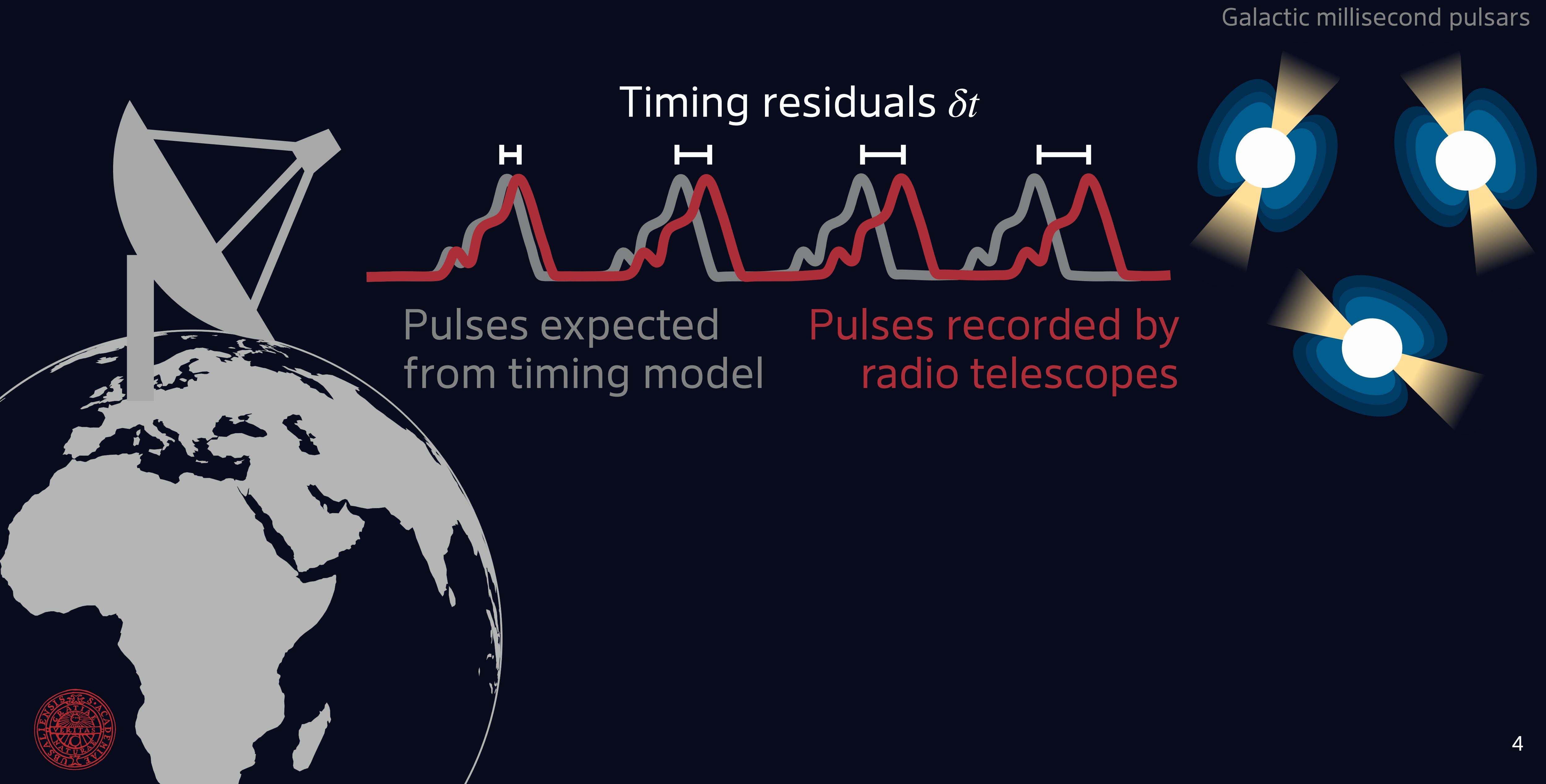
Galactic millisecond pulsars



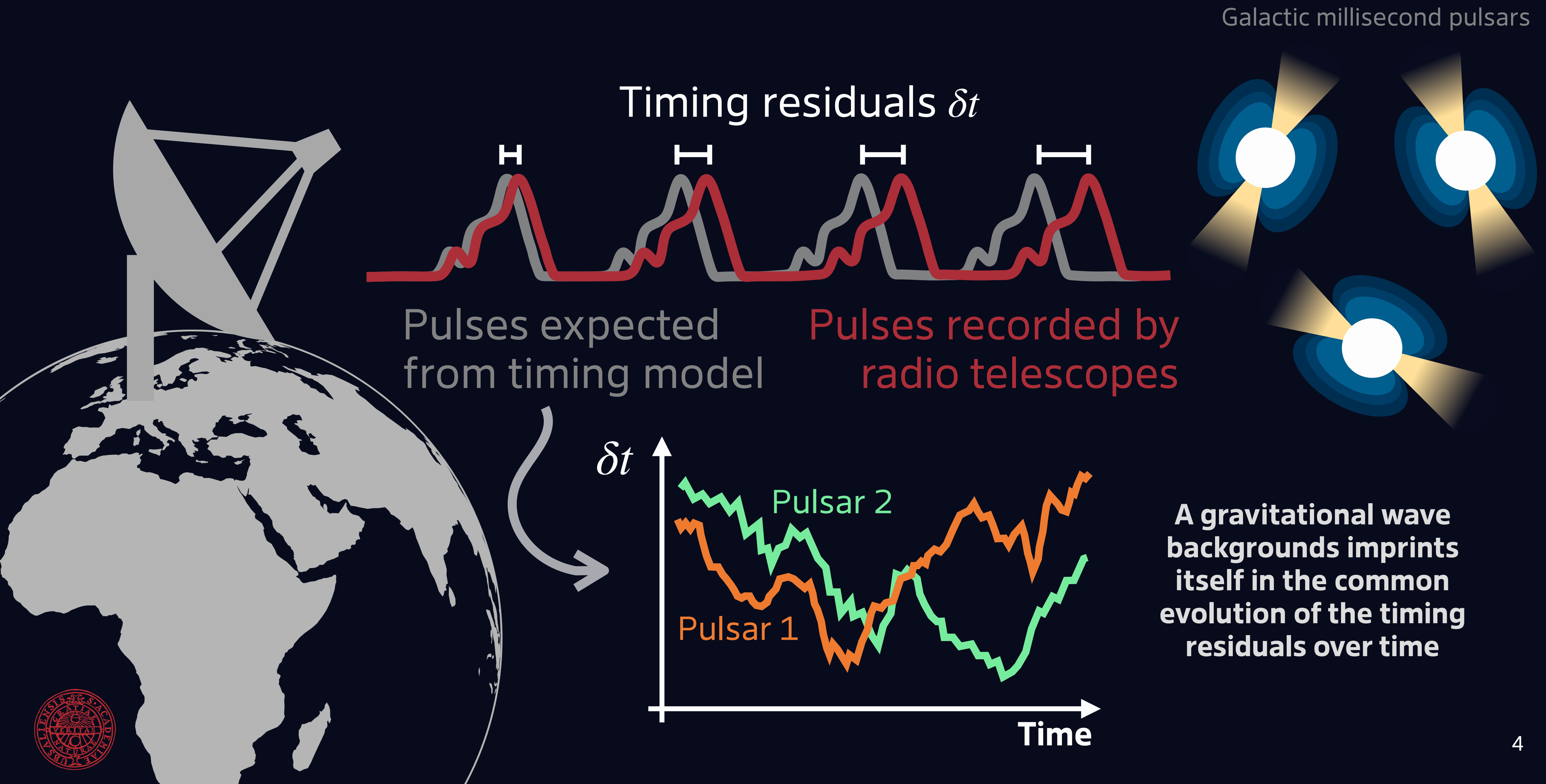
The working principle of a pulsar timing array



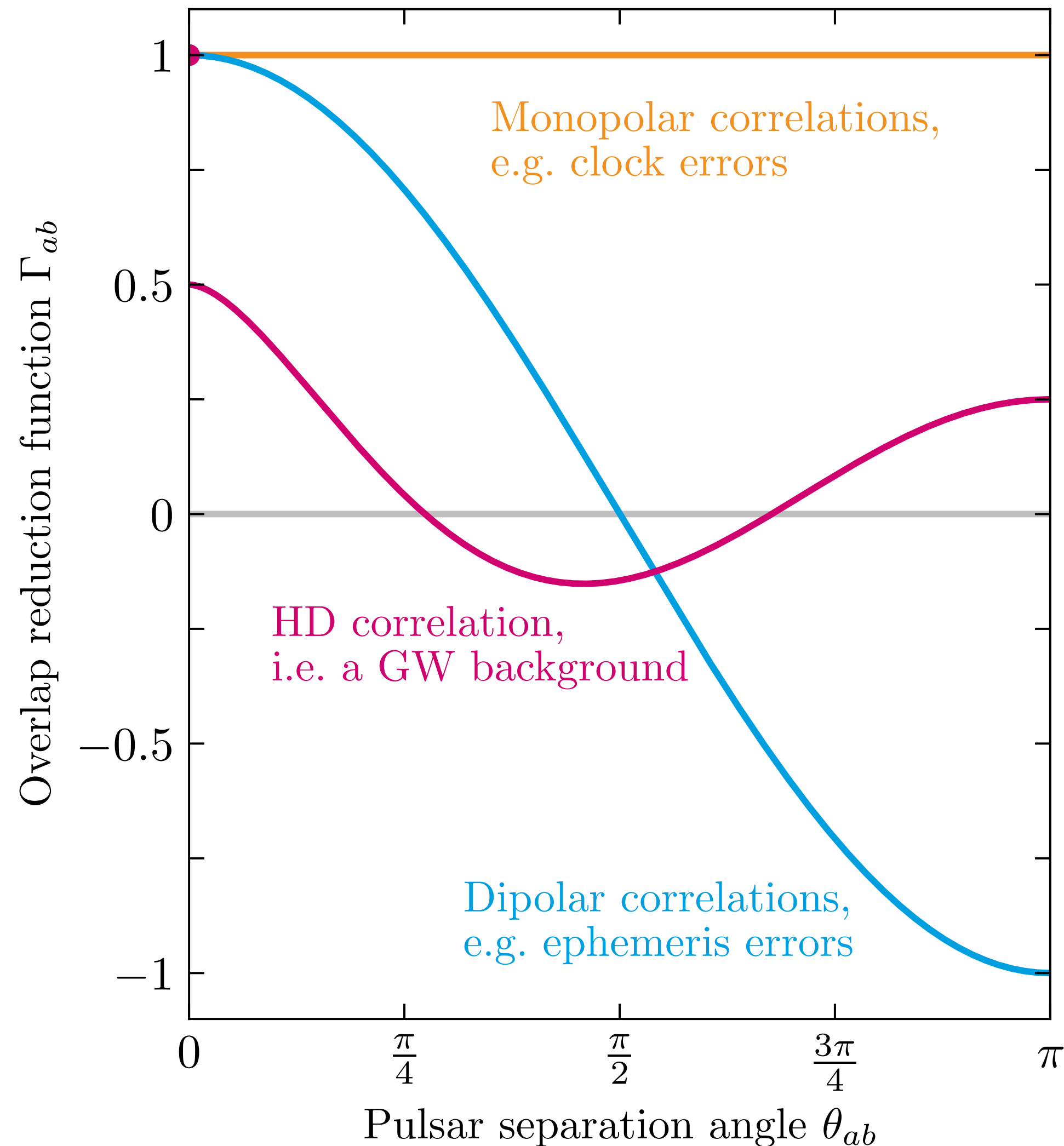
The working principle of a pulsar timing array



The working principle of a pulsar timing array



Searching for the Hellings-Downs correlation

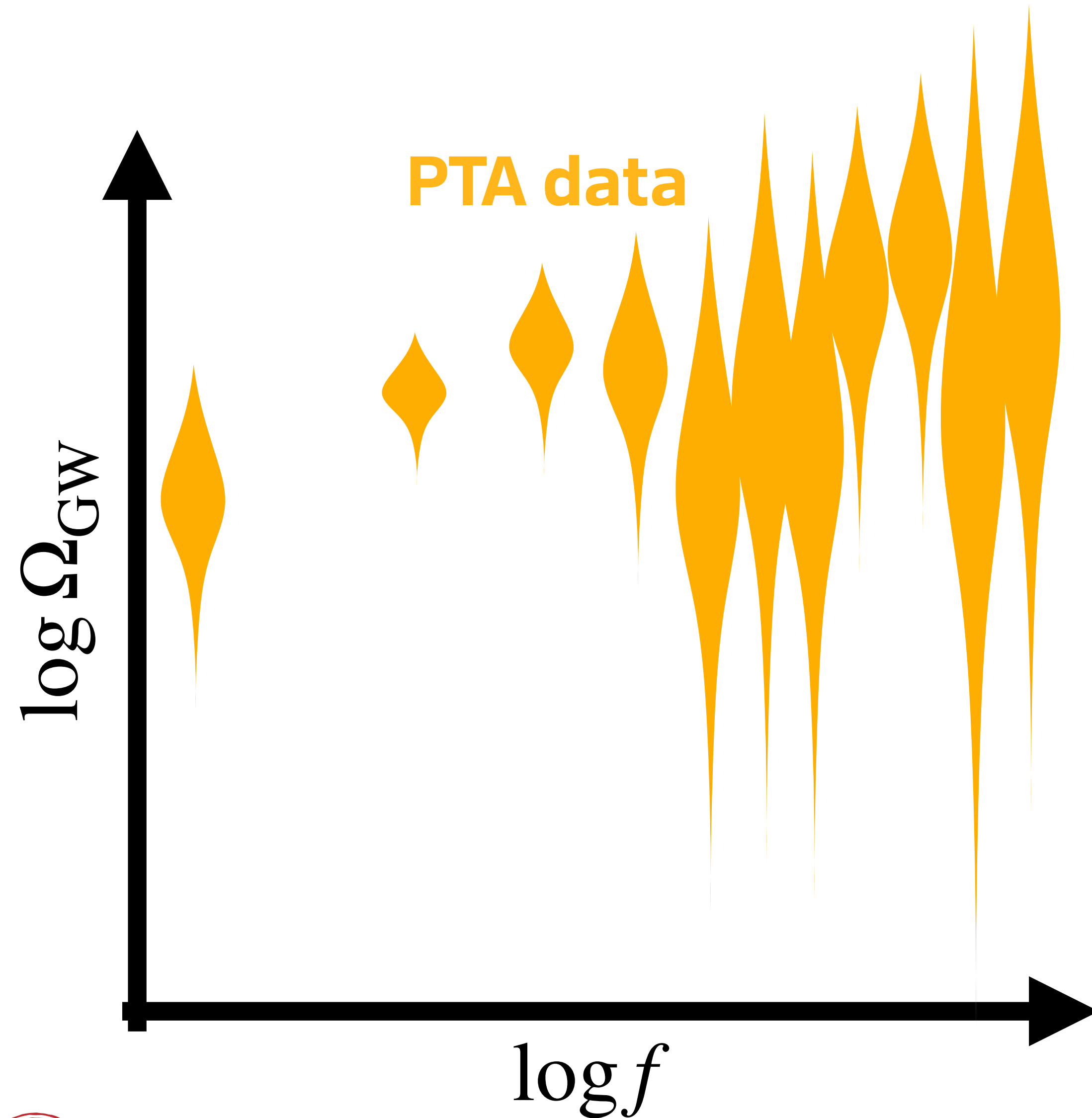


- PTAs found an underlying „common red process“ among $\mathcal{O}(70)$ pulsars
- Signal could have many sources:
 - Pulsars themselves, **Clock errors**, **Ephemeris errors**:
All ruled out with $>5\sigma$ significance
 - **Gravitational wave background**:
3 – 4 σ evidence [NANOGrav, 2023]

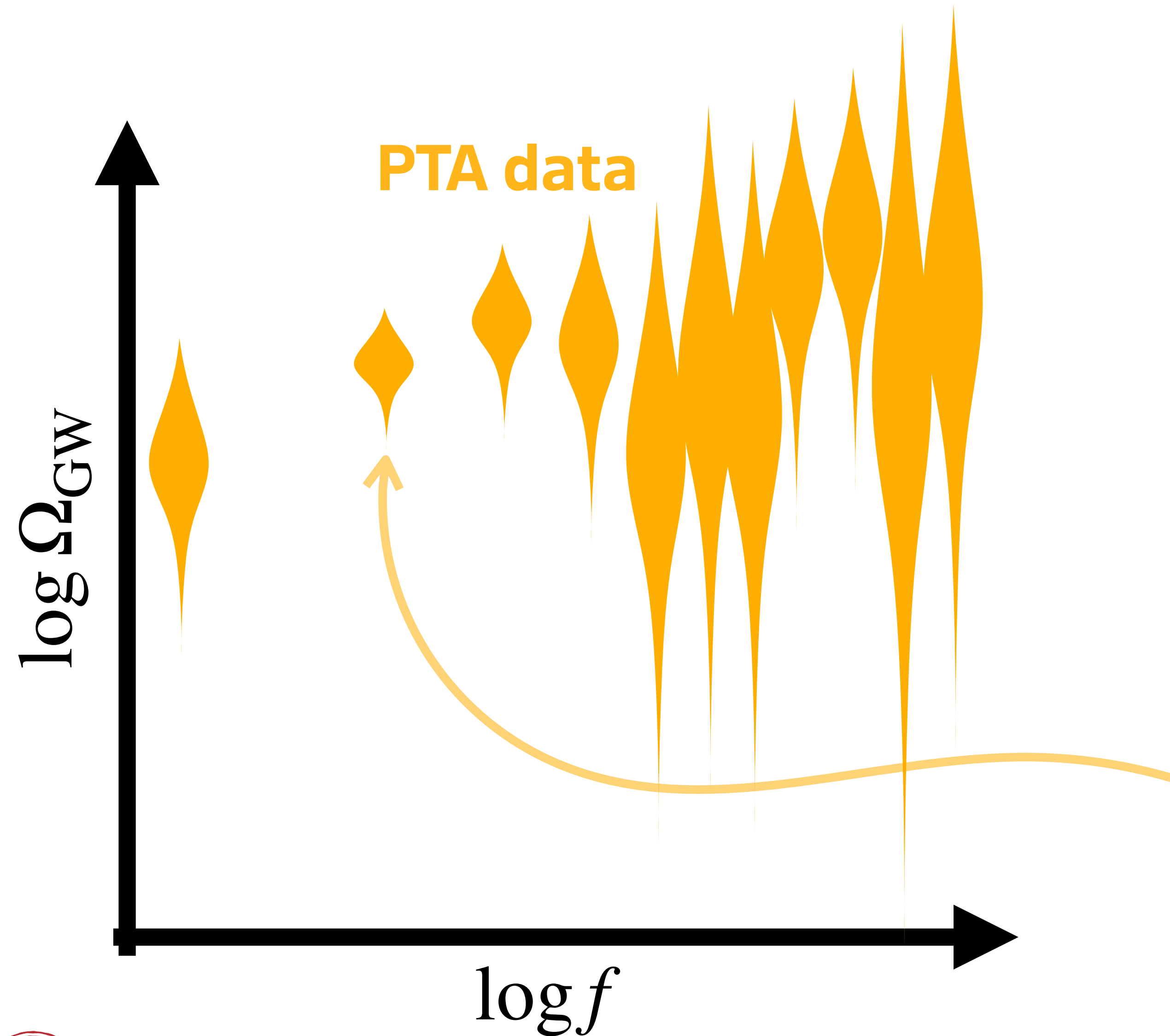


What is the source?

Learning to play the violin



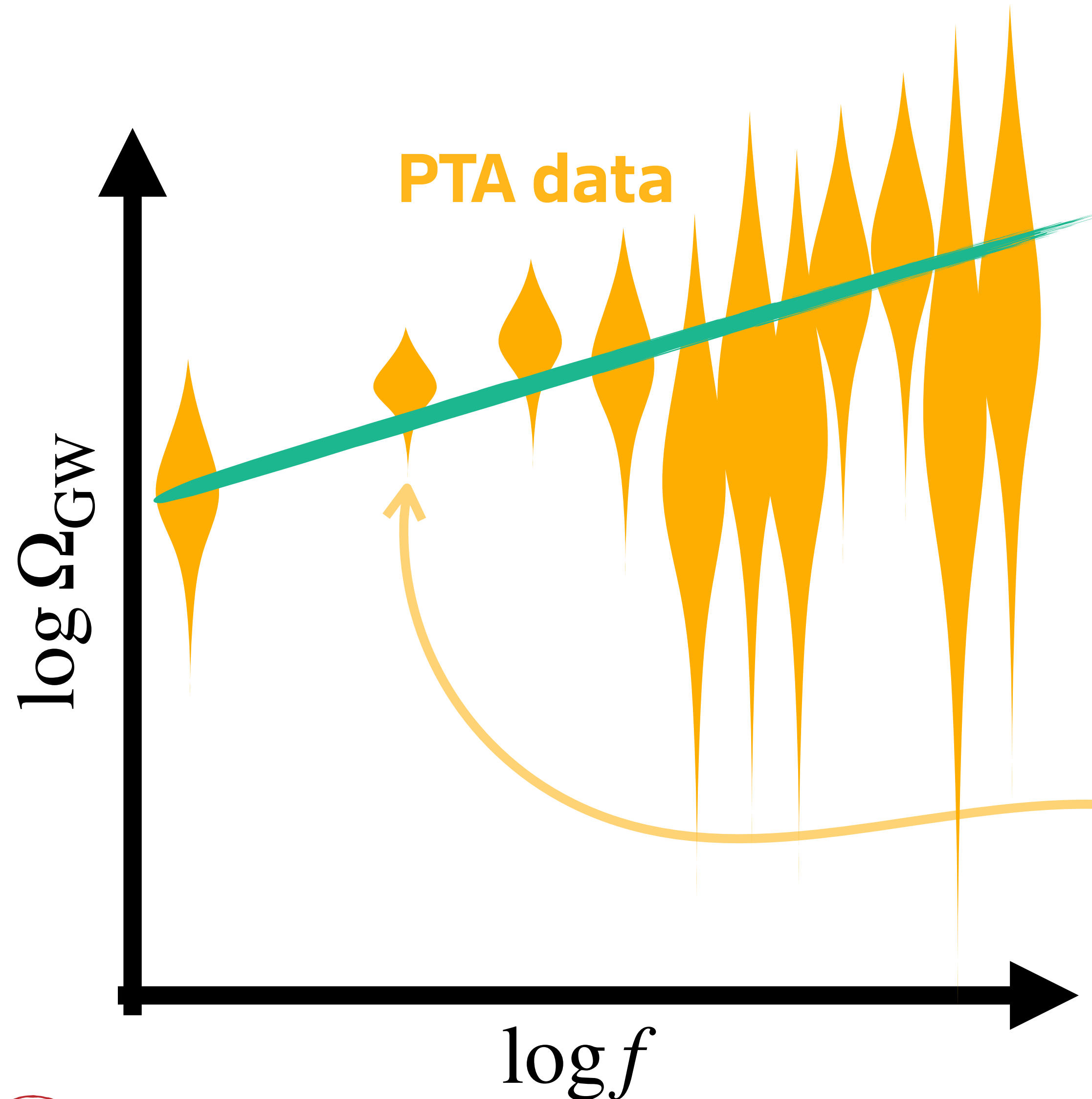
Learning to play the violin



Each „violin“ in the Bayesian spectrogram can be understood as a data point with non-Gaussian error bar, describing the Fourier amplitude of a given frequency.



Learning to play the violin



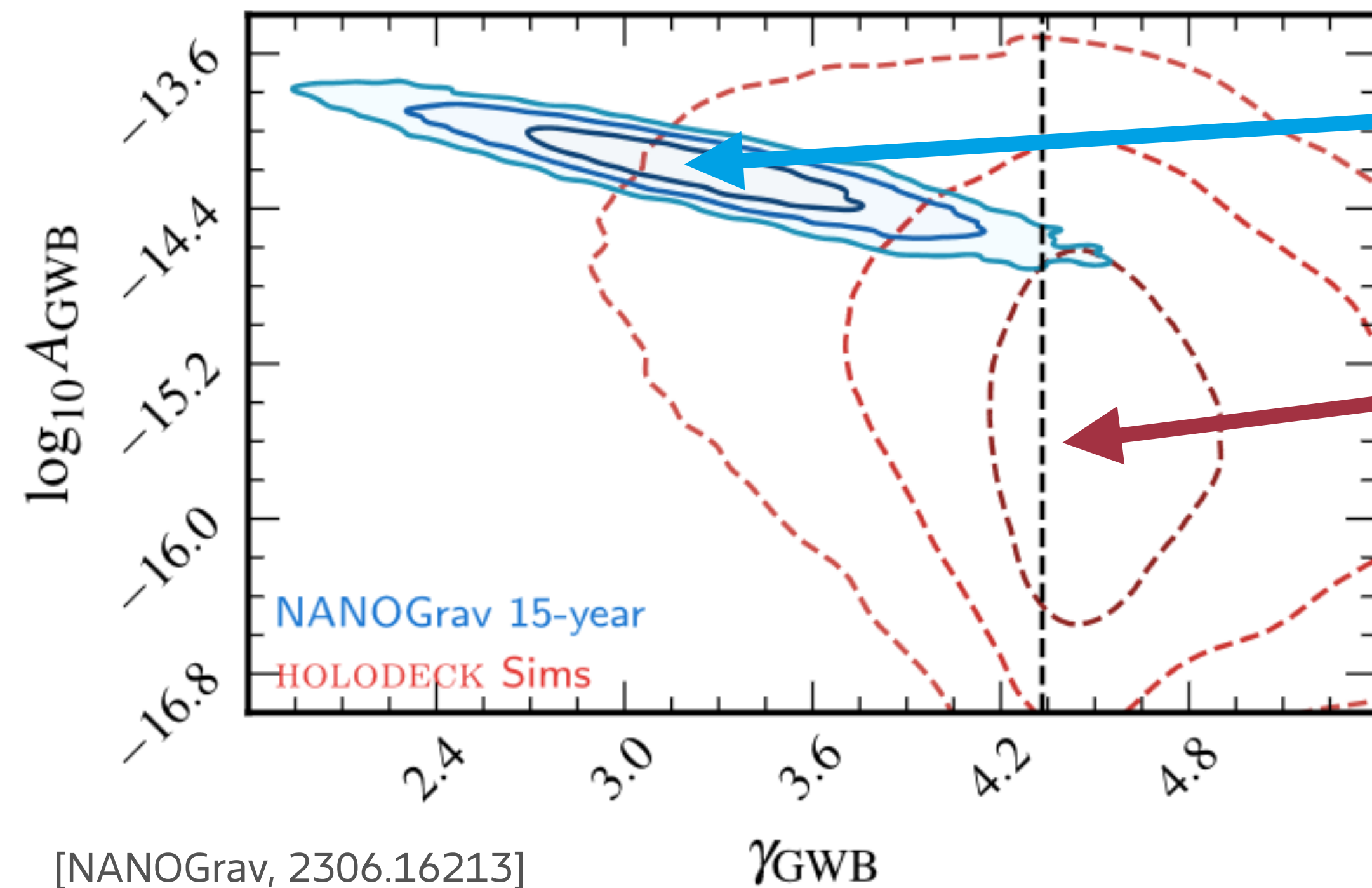
The inferred spectral shape of the GWB is well described by a power law

$$\Omega_{\text{GW}}(f) = \frac{2\pi^2}{3H_0^2} A^2 \left(\frac{f}{1 \text{ yr}^{-1}} \right)^{5-\gamma} \text{yr}^{-2}$$

Each „violin“ in the Bayesian spectrogram can be understood as a data point with non-Gaussian error bar, describing the Fourier amplitude of a given frequency.



Merging supermassive black holes

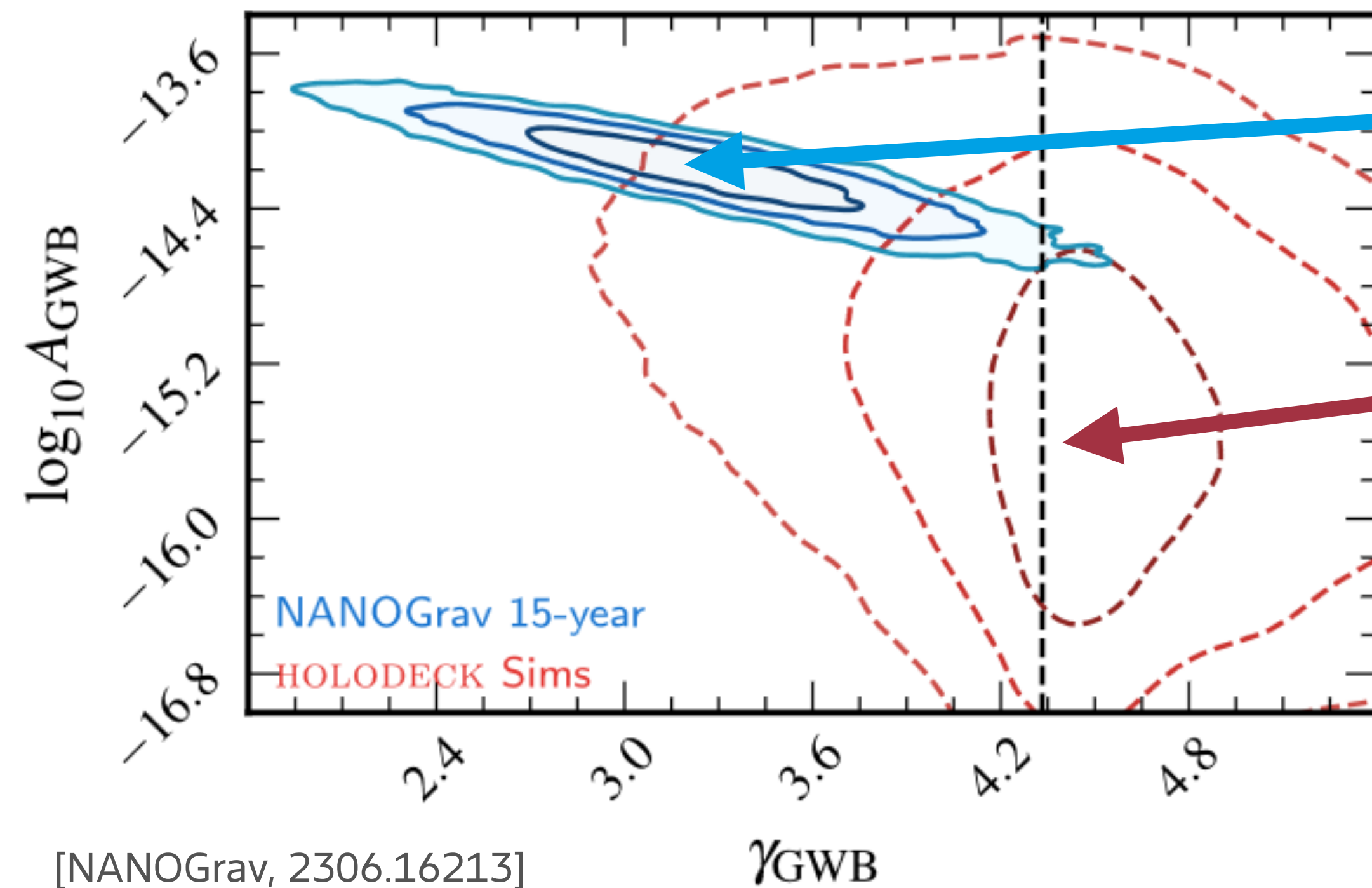


Observed signal follows a power-law spectrum with amplitude A and slope γ

Astrophysical simulations based on realistic BH populations predict much weaker signals with higher γ (more power in low frequencies)



Merging supermassive black holes



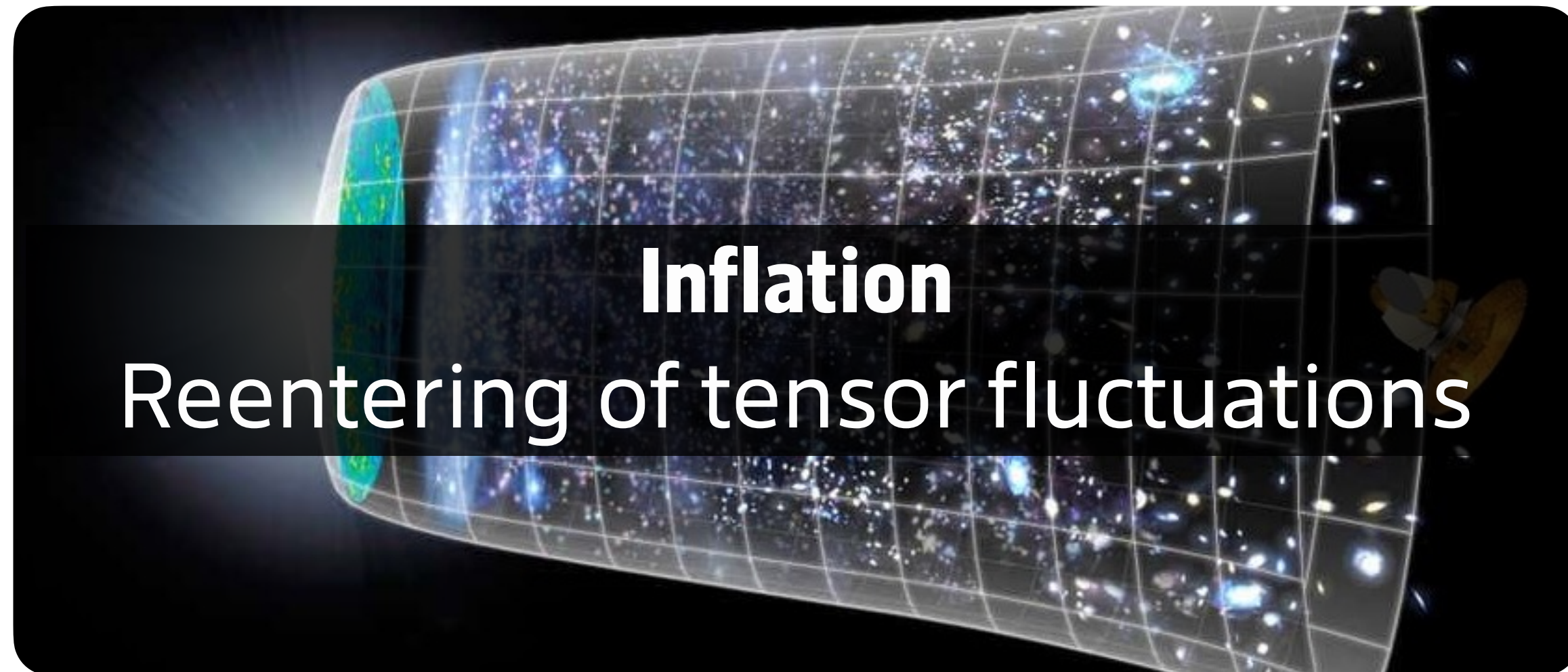
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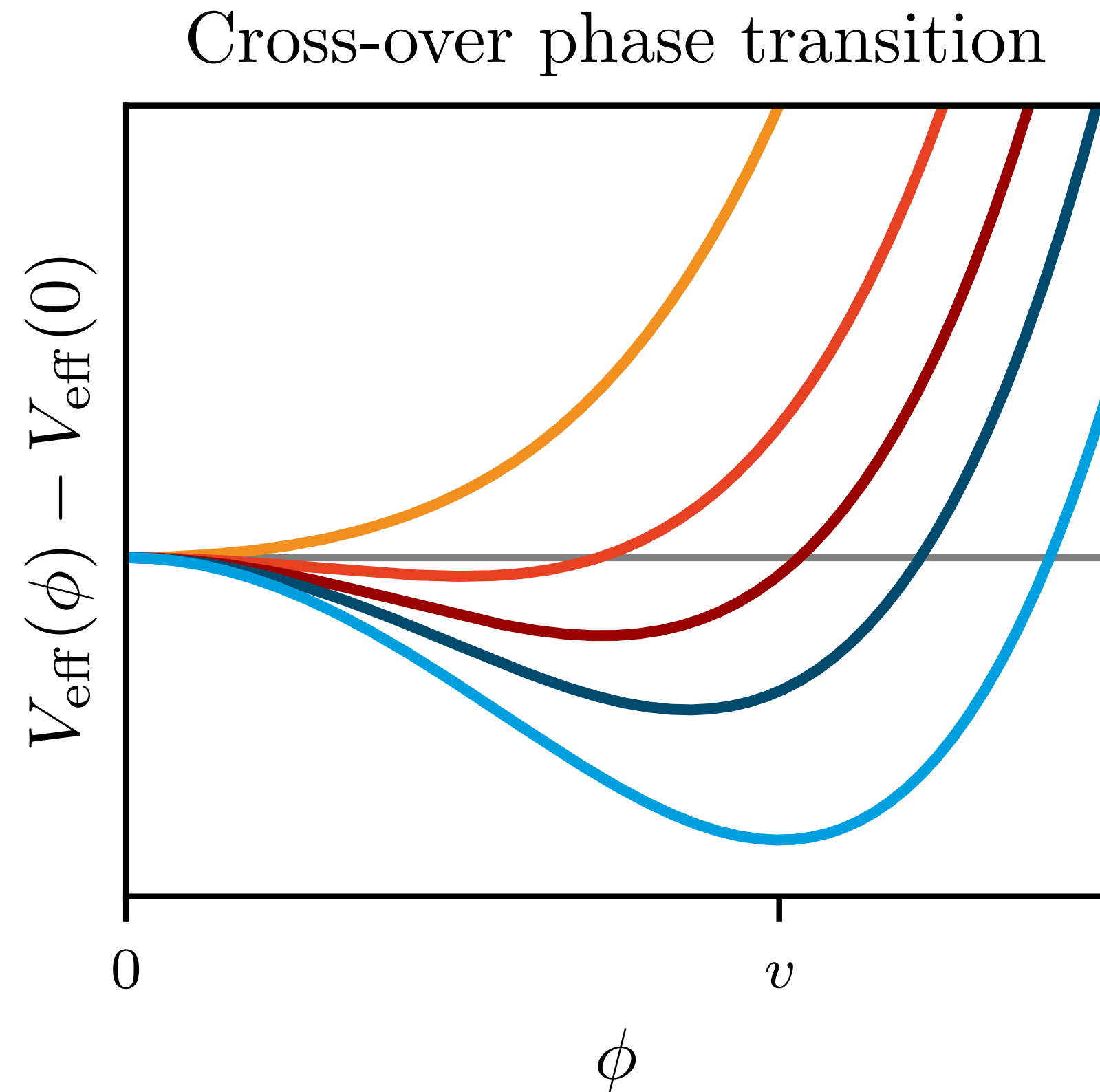
Are there other signal sources?



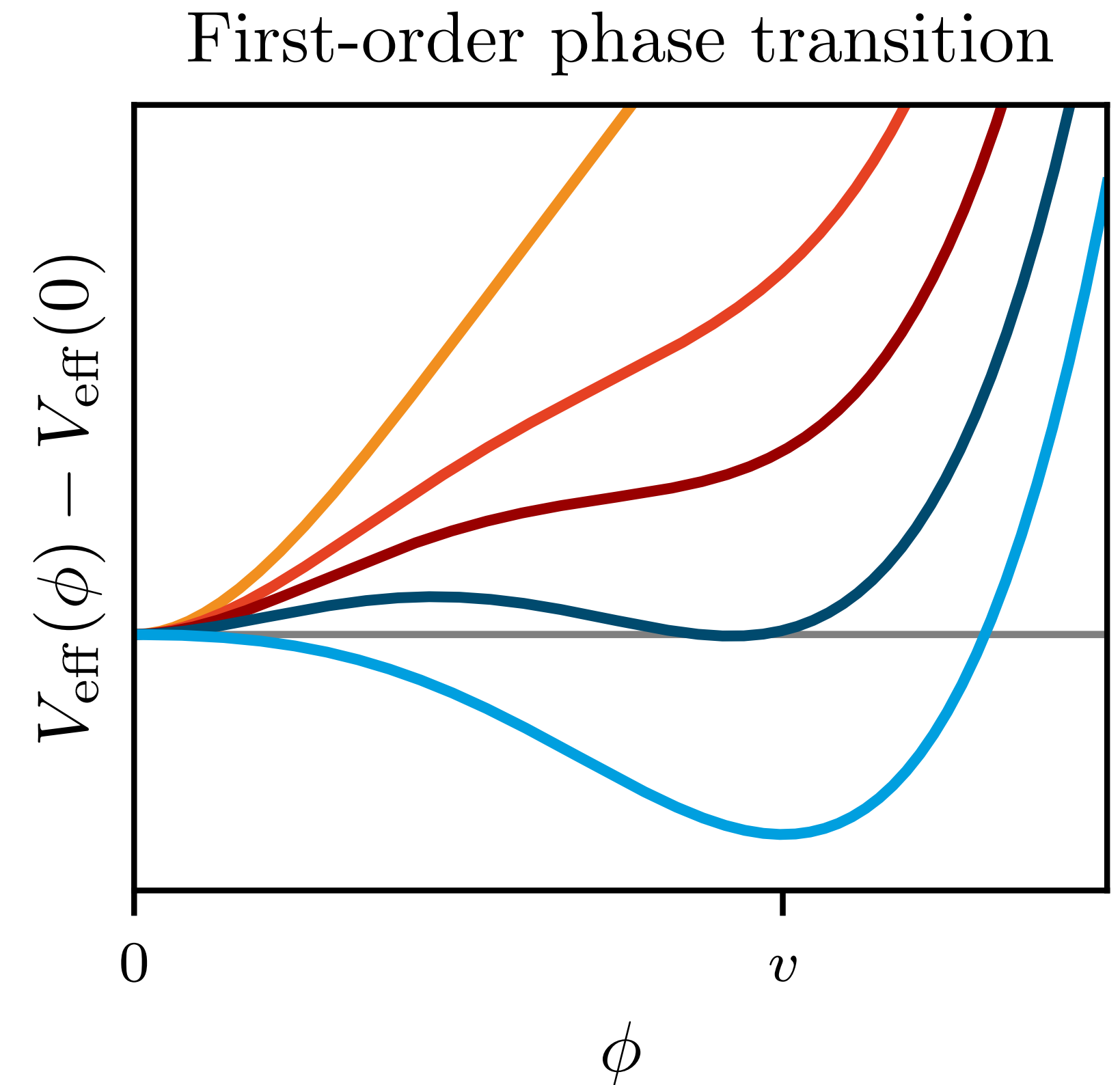
Possible cosmological sources of the PTA signal



First-order phase transitions vs. cross-overs



A scalar field "rolls down" from $\phi = 0$ to $\phi = v$, when the plasma cools from **high temperatures** to **low temperatures**.

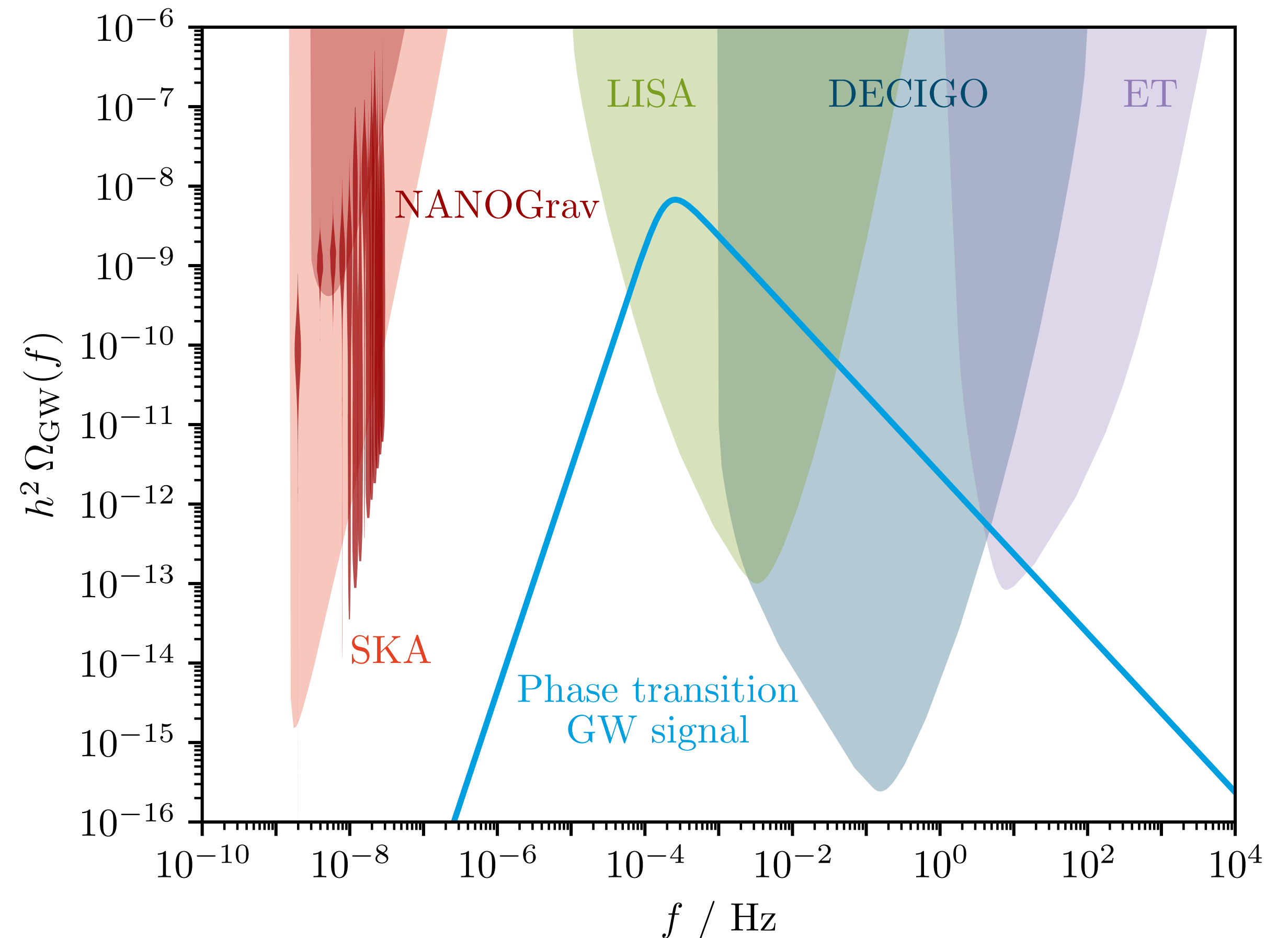
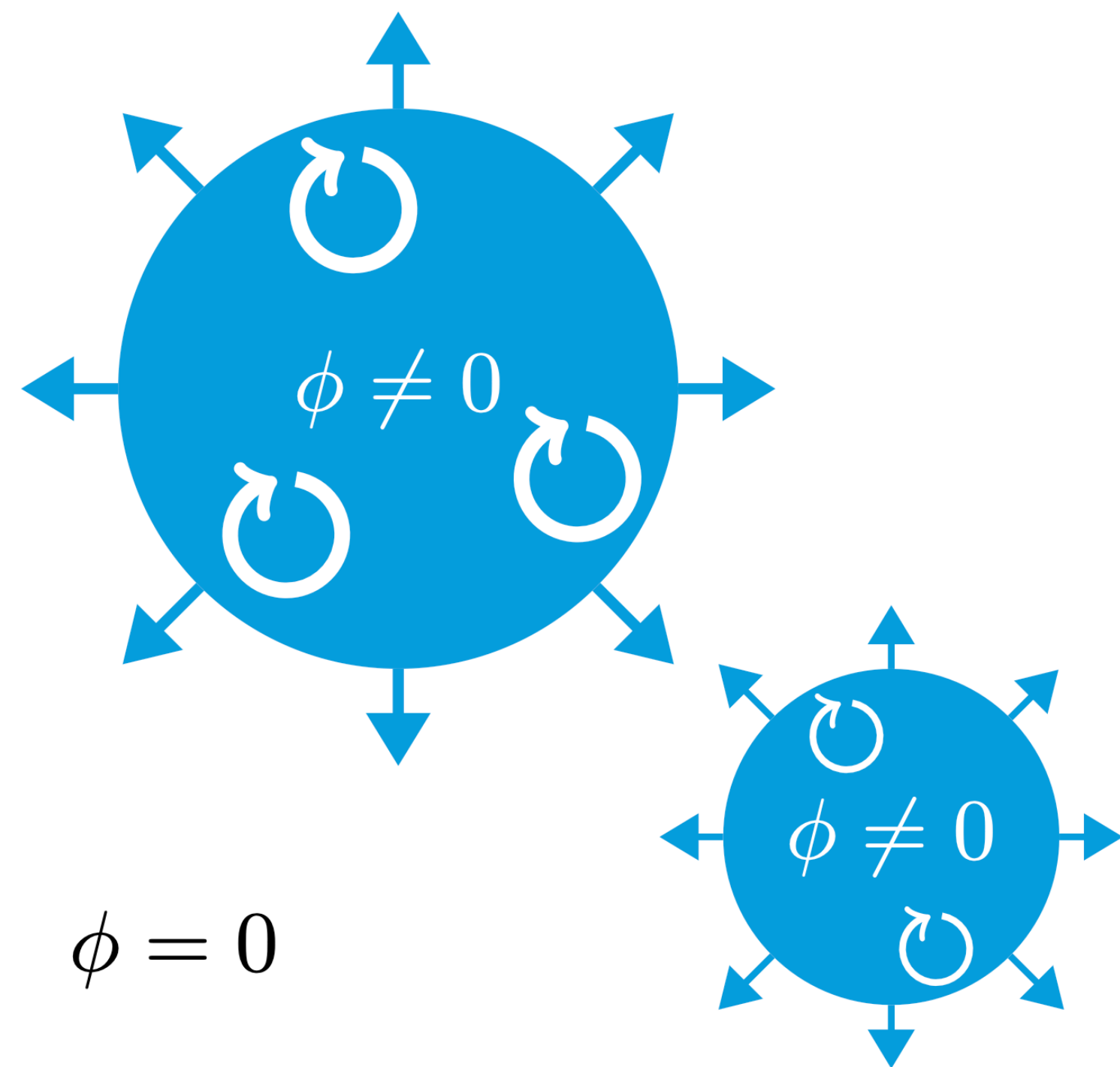


A scalar field tunnels to the true potential minimum $\phi \neq 0$ to minimize its free energy.



First-order phase transitions produce GWs

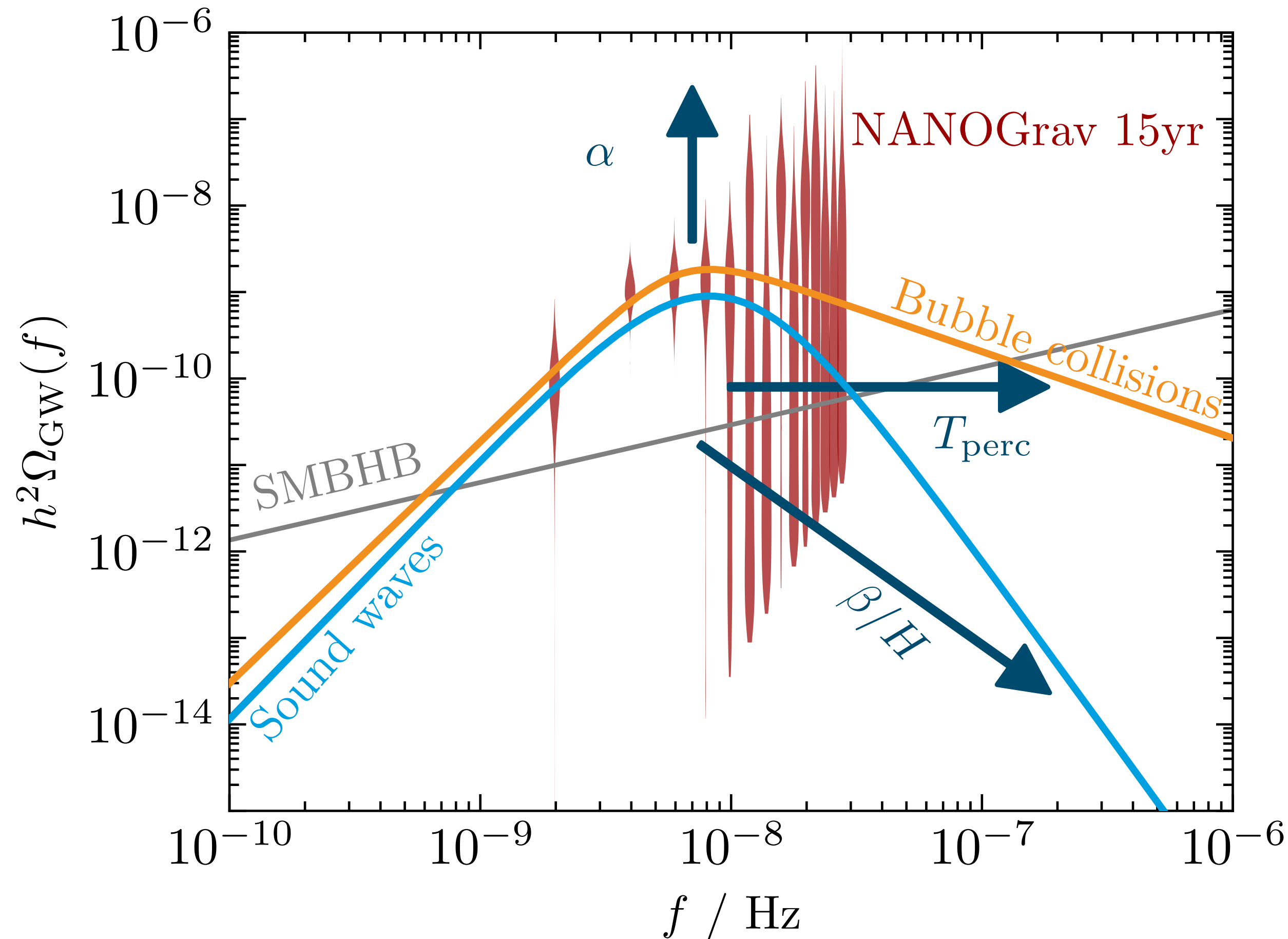
Bubbles of the new phase nucleate, collide and perturb the plasma...



... giving rise to an observable stochastic gravitational wave background.



Parametrization of the GW signal



SMBHB: $A = 10^{-15.5}$, $\gamma = 13/3$

$$h^2 \Omega_{\text{GW}}^{\text{sw}, \text{bw}}(f) \simeq 10^{-6} \left(\frac{\alpha}{\alpha + 1} \right)^2 \left(\frac{H}{\beta} \right)^{1,2} \mathcal{S} \left(\frac{f}{f_{\text{peak}}} \right)$$

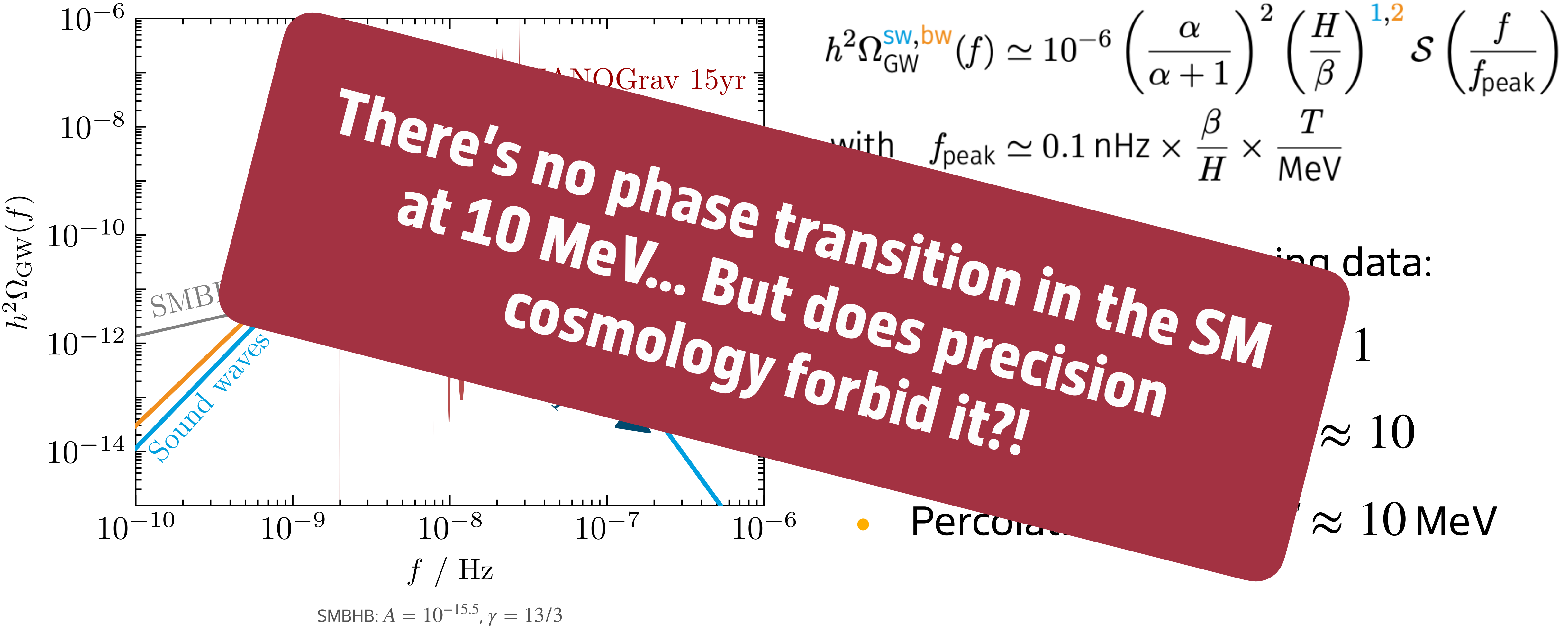
$$\text{with } f_{\text{peak}} \simeq 0.1 \text{ nHz} \times \frac{\beta}{H} \times \frac{T}{\text{MeV}}$$

To fit the new pulsar timing data:

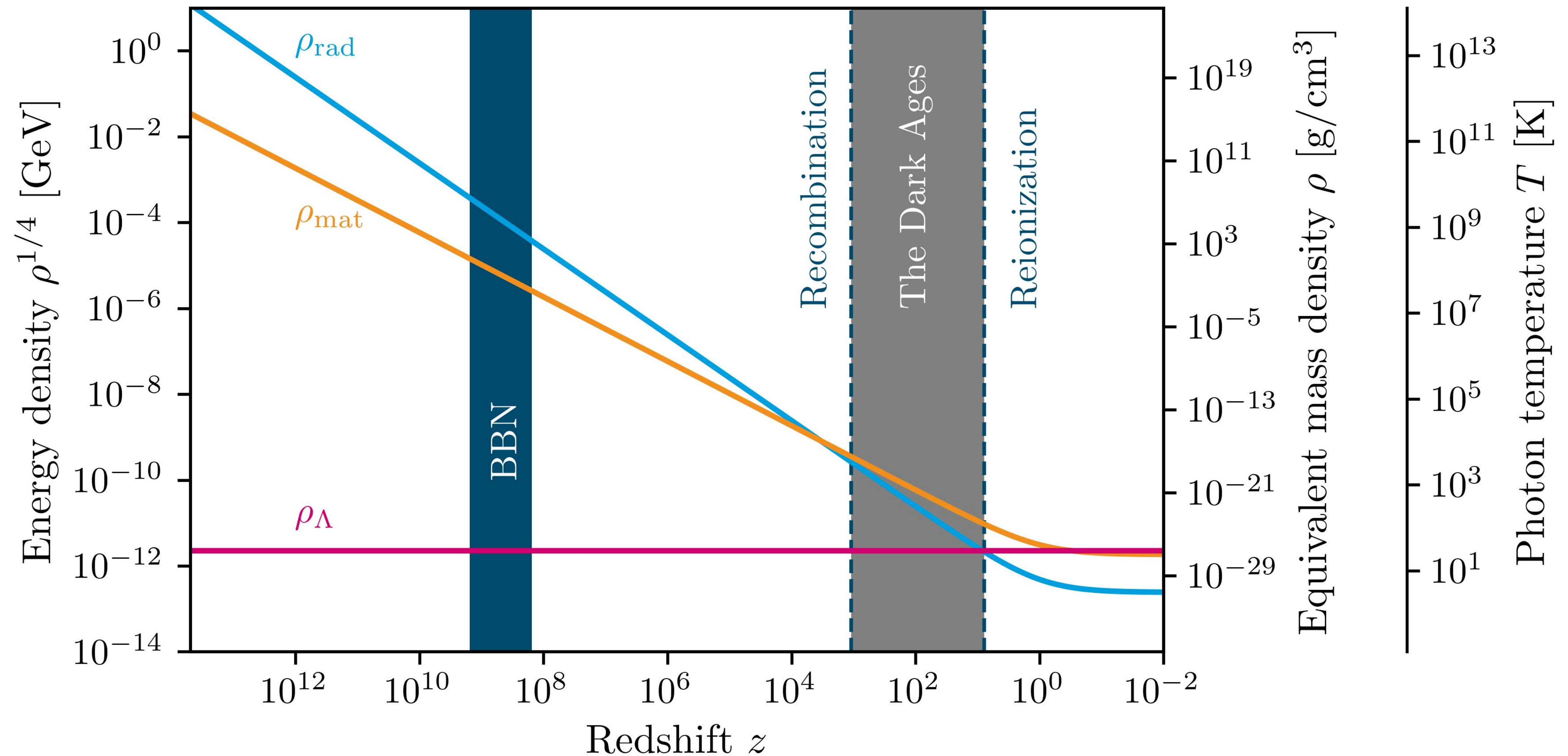
- Strong transitions, $\alpha \gtrsim 1$
- Slow transitions, $\beta/H \approx 10$
- Percolation around $T \approx 10 \text{ MeV}$



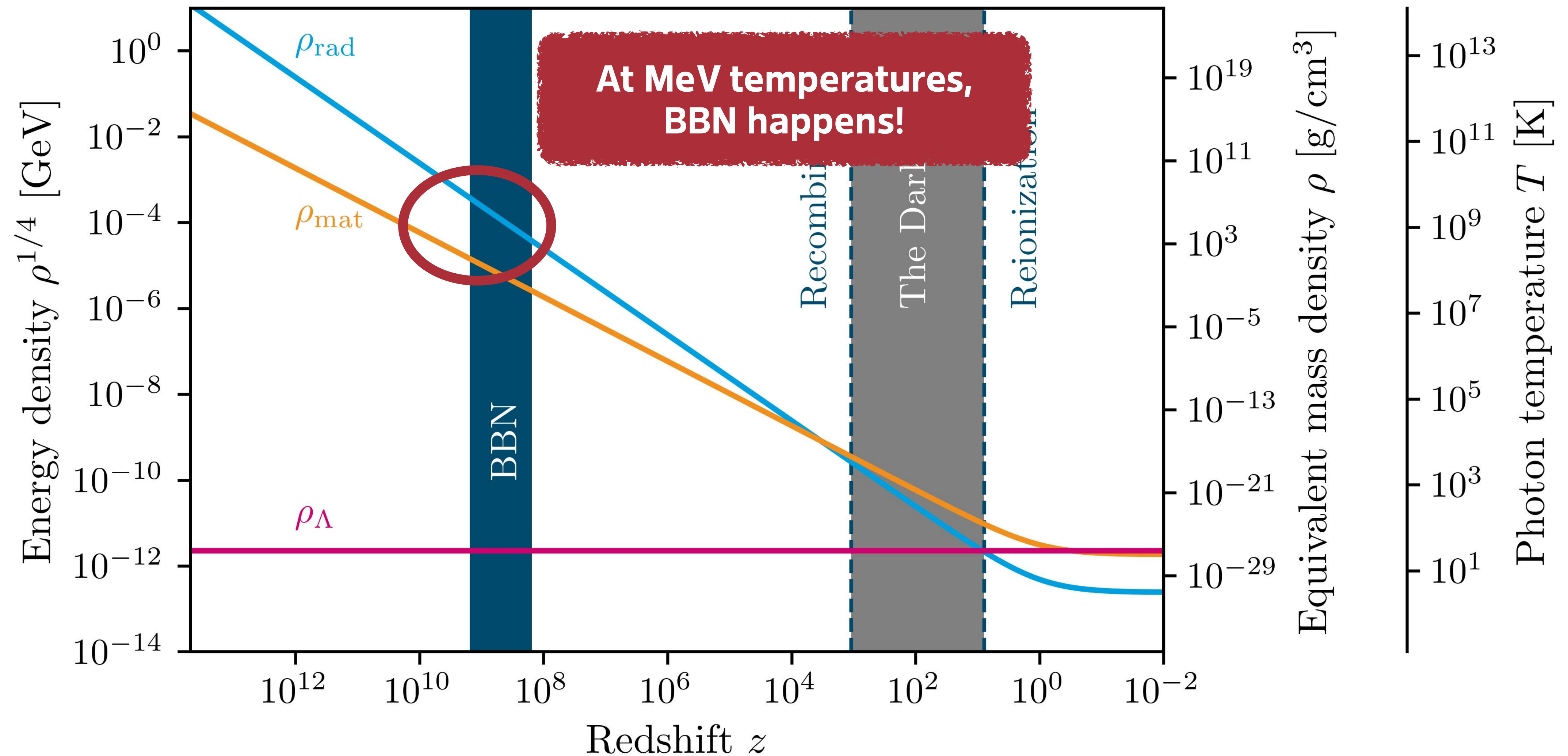
Parametrization of the GW signal



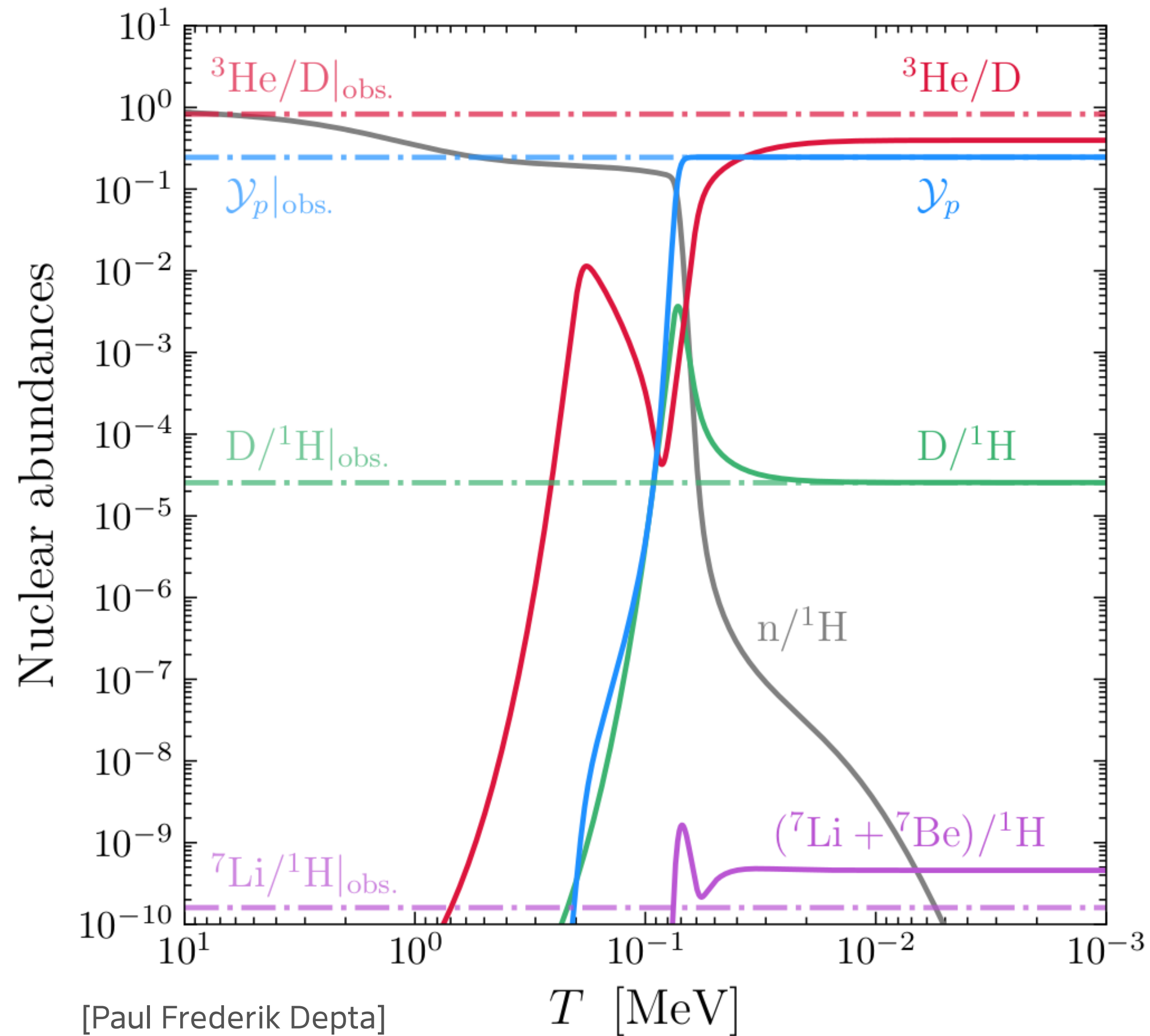
A brief history of time



A brief history of time



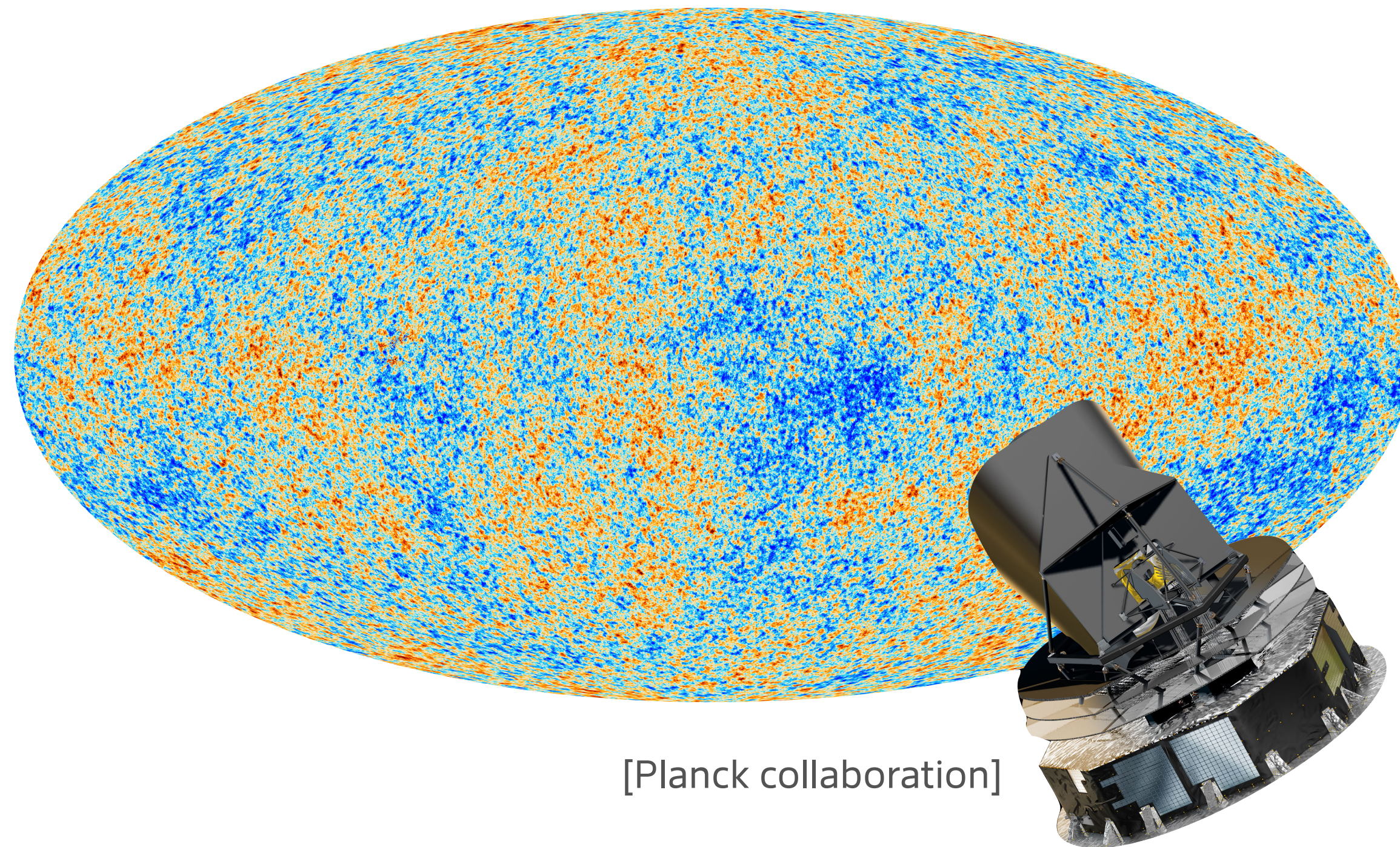
Big Bang Nucleosynthesis and the CMB



- Observation of primordial light element abundances in good agreement with standard BBN
- $N_{\text{eff}}^{\text{BBN}} = 2.898 \pm 0.141$



Big Bang Nucleosynthesis and the CMB



- Observation of primordial light element abundances in good agreement with standard BBN
- $N_{\text{eff}}^{\text{BBN}} = 2.898 \pm 0.141$
- $N_{\text{eff}}^{\text{CMB}} = 2.99 \pm 0.17$
- Consistent with 3 SM neutrinos



Big Bang Nucleosynthesis and the CMB

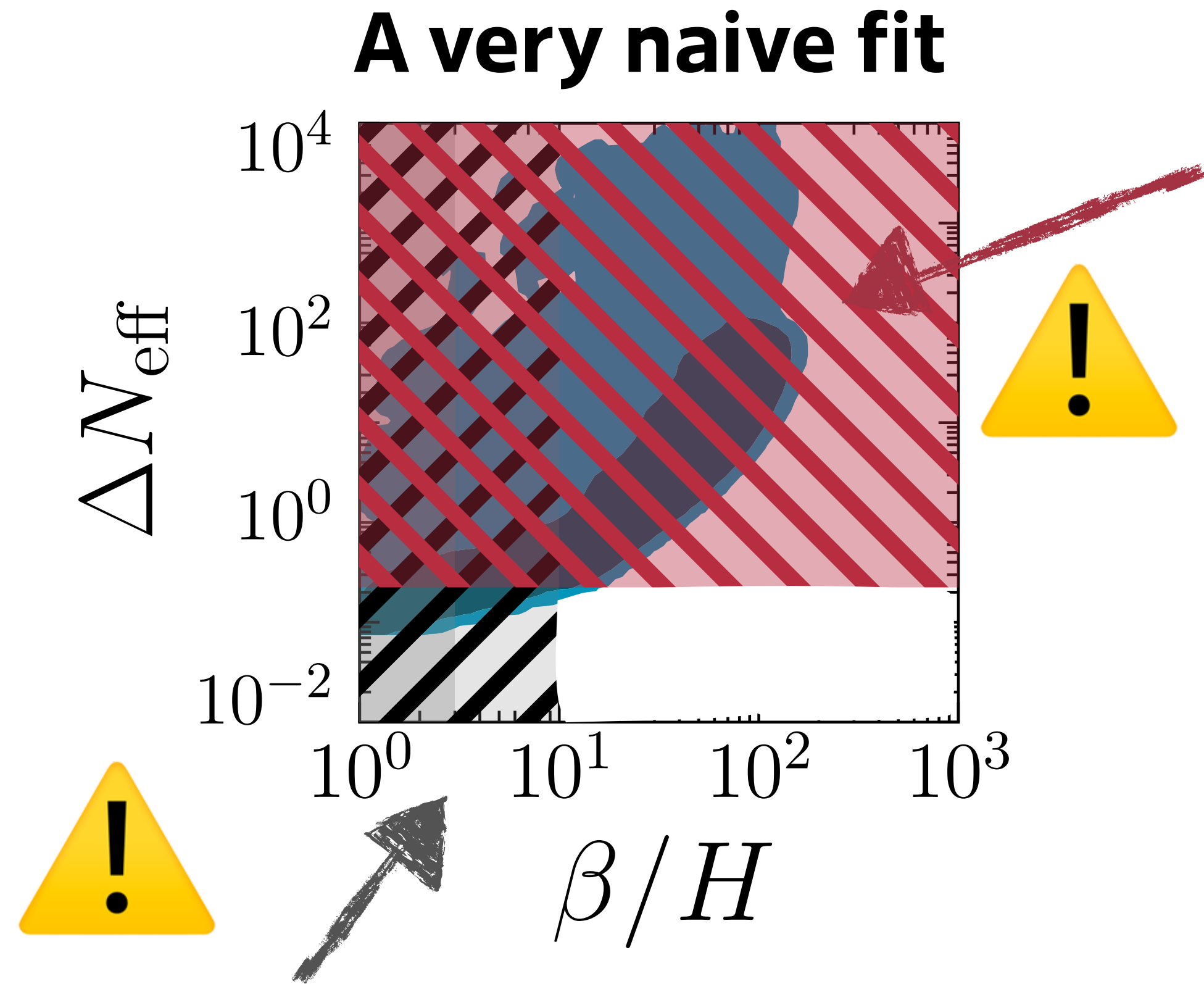
- Observation of primordial fluctuations in the CMB

We only need to get rid of extra energy in the dark sector before BBN to allow for a phase transition at the 10 MeV scale 😊

- Consistent with 3 SM neutrinos



A dark sector without portal couplings



The liberated vacuum energy remains in the dark sector. A good fit would require enormous

$$\Delta N_{\text{eff}} \gg 0.22$$

Giant „Hubble“ bubble sizes would be needed, violating causality & questioning validity of GW predictions

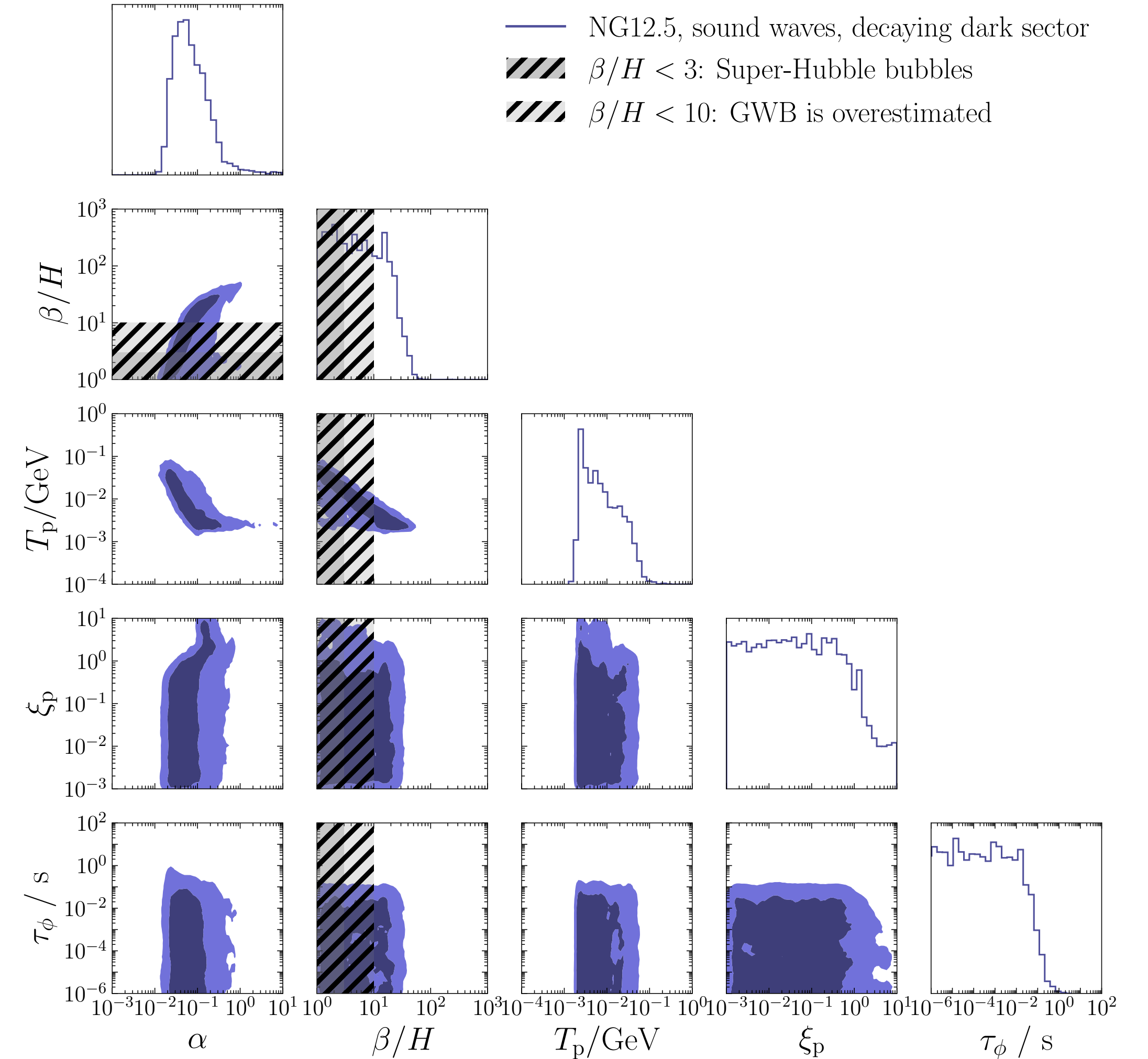
[CT et al, JCAP 11 (2023) 053]



The dark sector must die for the GWs to live...



If the dark sector decays before BBN, a great fit to PTA data can be achieved!



[CT et al, JCAP 11 (2023) 053]



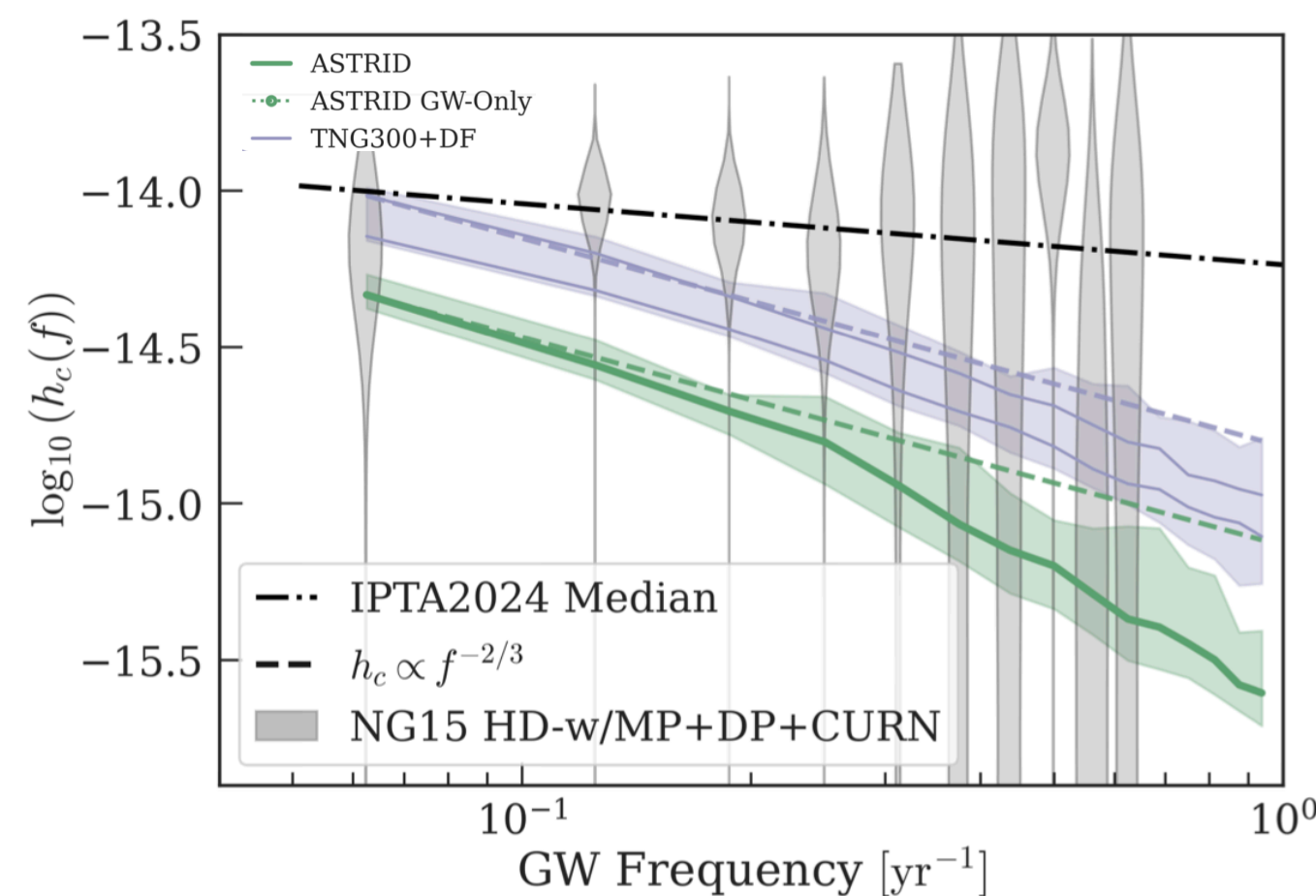
New PTA data: higher peak frequency and slope

[NANOGrav, PPTA, EPTA, CPTA, InPTA, Meerkat]

Solution to the final parsec problem?

[Chiaberge+, 2501.18730]

What happened since July 2023?



N-Body simulations: SMBHB unable to account for full GW signal

[Chen+, 2502.01024]

More constraints than just ΔN_{eff} ?

CT+ [JCAP 08 (2025) 062]

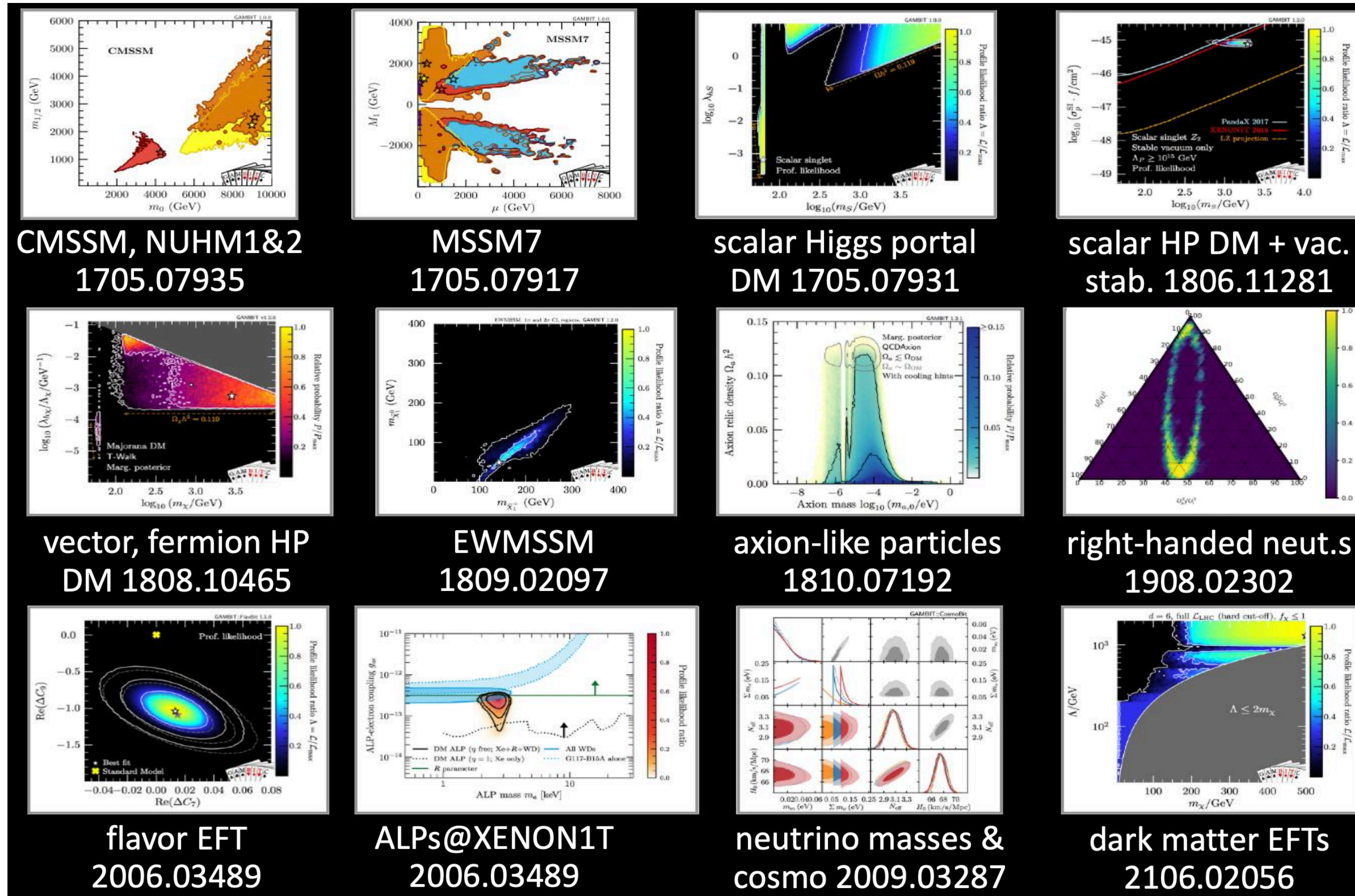
Investigation of specific dark sector models

[2412.16282, 2501.11619, 2501.14986, 2501.15649, 2502.04108, ...]

Rest of this talk and my own focus



GAMBIT: from Lagrangians to Likelihoods

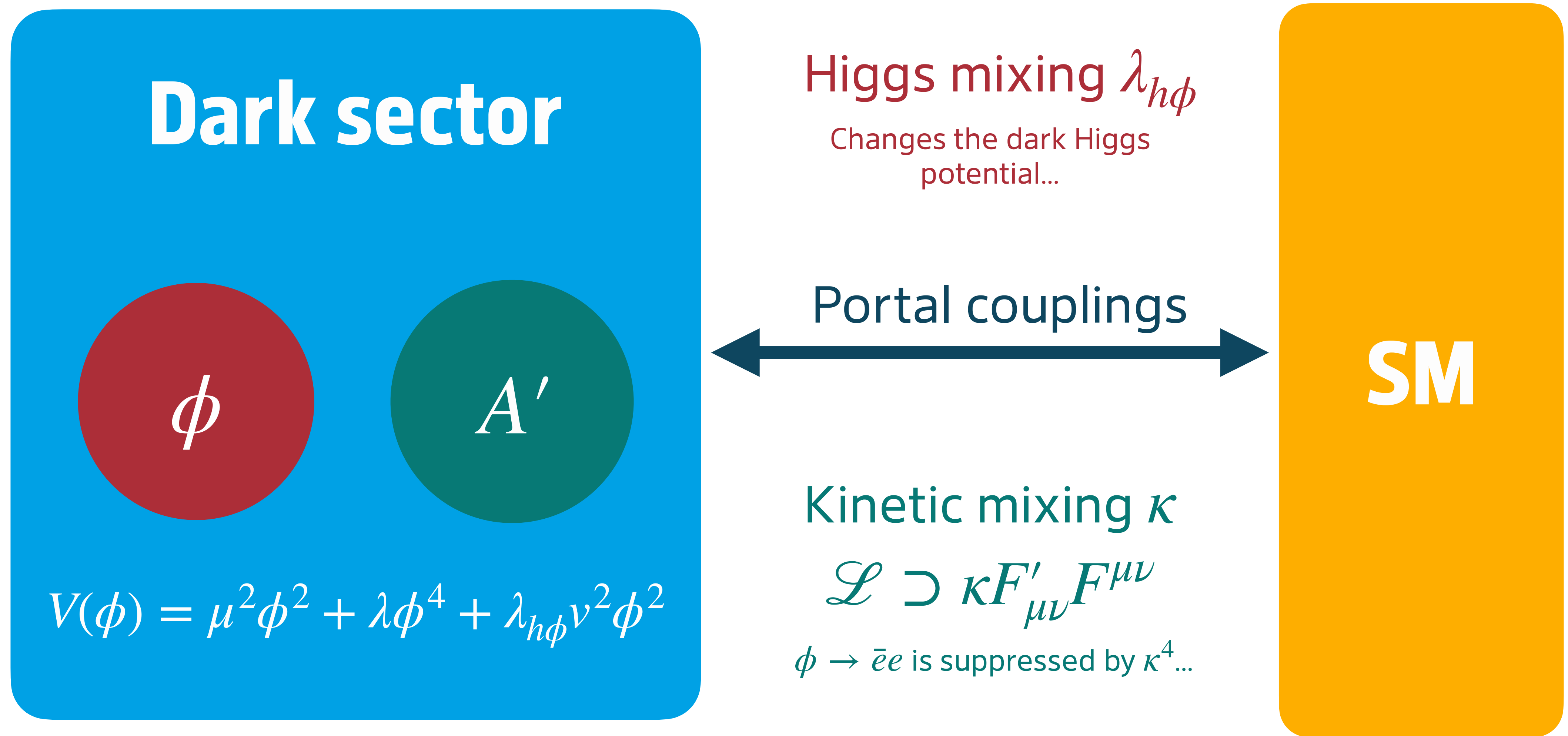


To combine BBN + CMB,
direct and indirect DM
detection, bullet cluster
and beam dump
constraints: **GAMBIT**

Slide by C. Balázs @ SUSY 2021



A minimal dark sector setup



See 2412.16282, 2501.11619, 2501.15649, 2501.14986
by Banik, Gonçalves, Costa, Li et al.



A minimal dark sector setup

Dark sector

This model is flawed. Hard (impossible?)
to avoid cosmological constraints and
fine-tuning...

$V(\phi)$

Higgs mixing λ

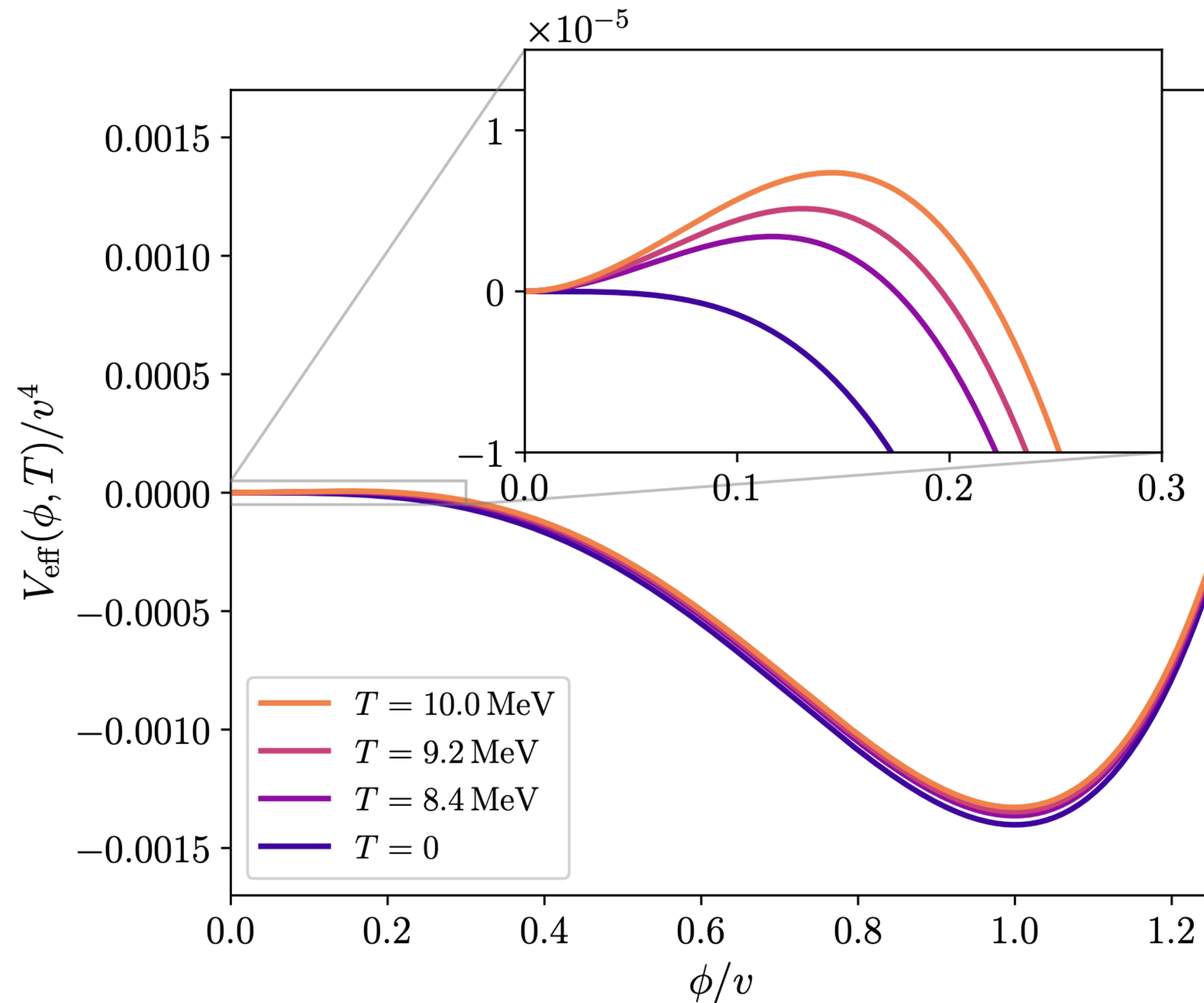
$$\mathcal{L} \supset \kappa F'_{\mu\nu} F^{\mu\nu}$$

$\phi \rightarrow \bar{e}e$ is suppressed by κ^4 ...

See 2412.16282, 2501.11619, 2501.15649, 2501.14986
by Banik, Gonçalves, Costa, Li et al.



Interlude: How to be supercool 😎



Note: This is not the *only* way to achieve strong supercooling. Watch out for my upcoming paper together with Jonas, Kai, Thomas and Torsten! :)

$$V_{\text{tree}}(\phi) = \lambda\phi^4$$

Quantum and thermal corrections

$$V_{\text{eff}}(\phi, T) \supset \lambda\phi^4 \log\left(\frac{T}{v}\right)$$

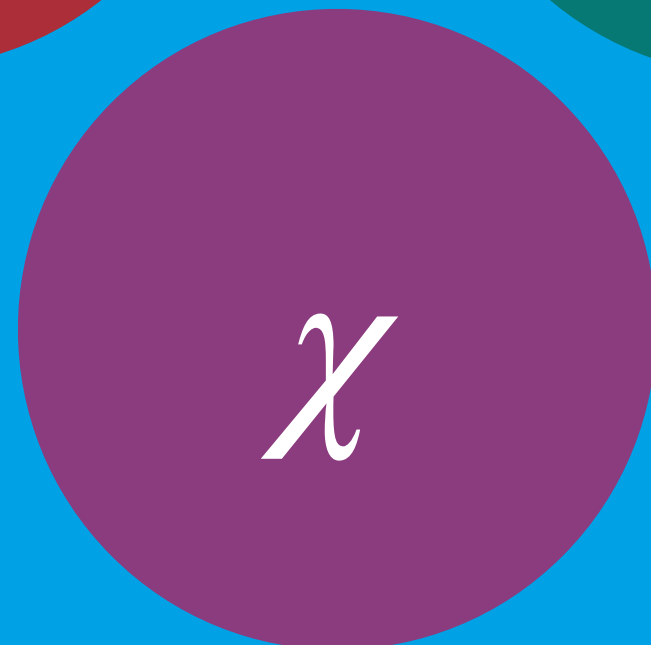
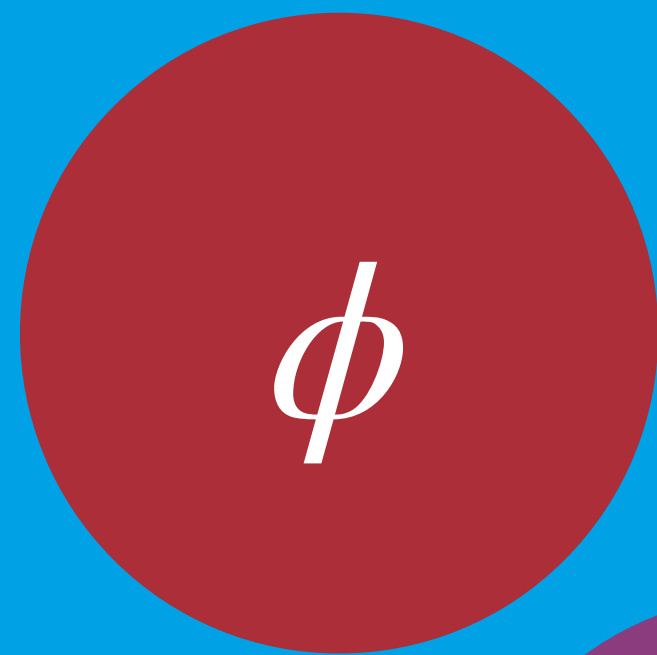
Loop-induced barrier down until very low temperatures, i.e. strong supercooling



A conformal dark sector incl. dark matter candidate

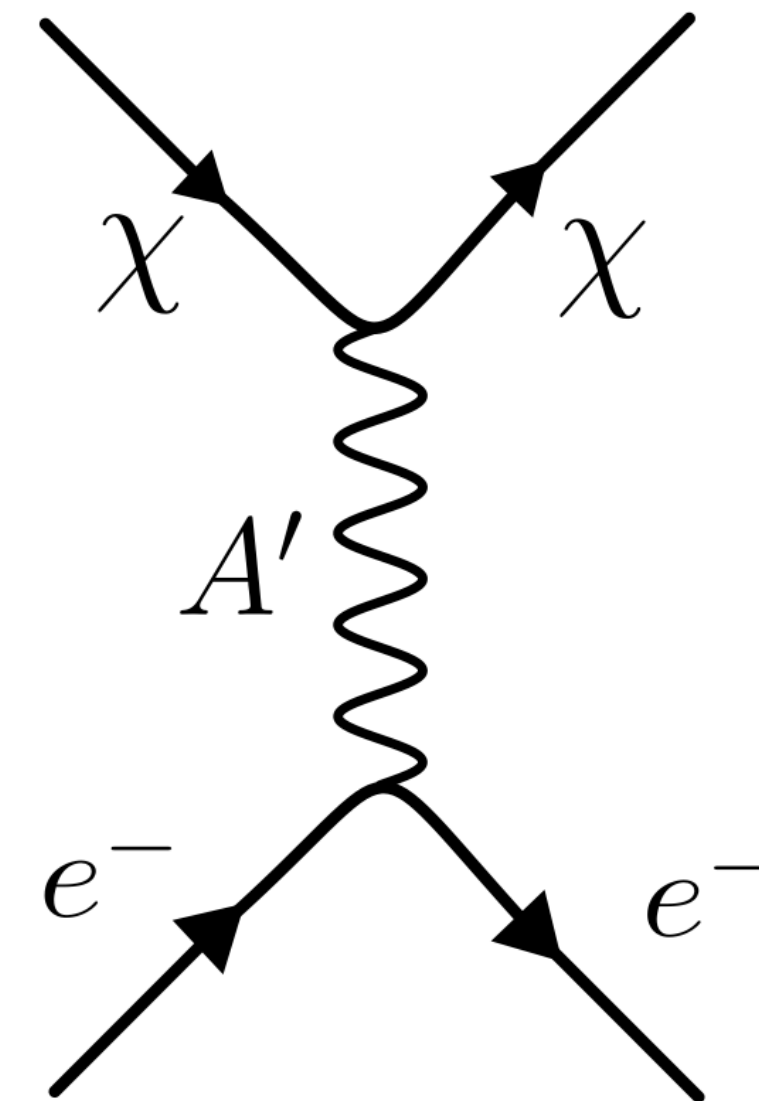


Dark sector



$$V(\phi) = \mu^2 \phi^2 + \lambda \phi^4 + \lambda_{h\phi} v^2 \phi^2$$

Kinetic mixing κ



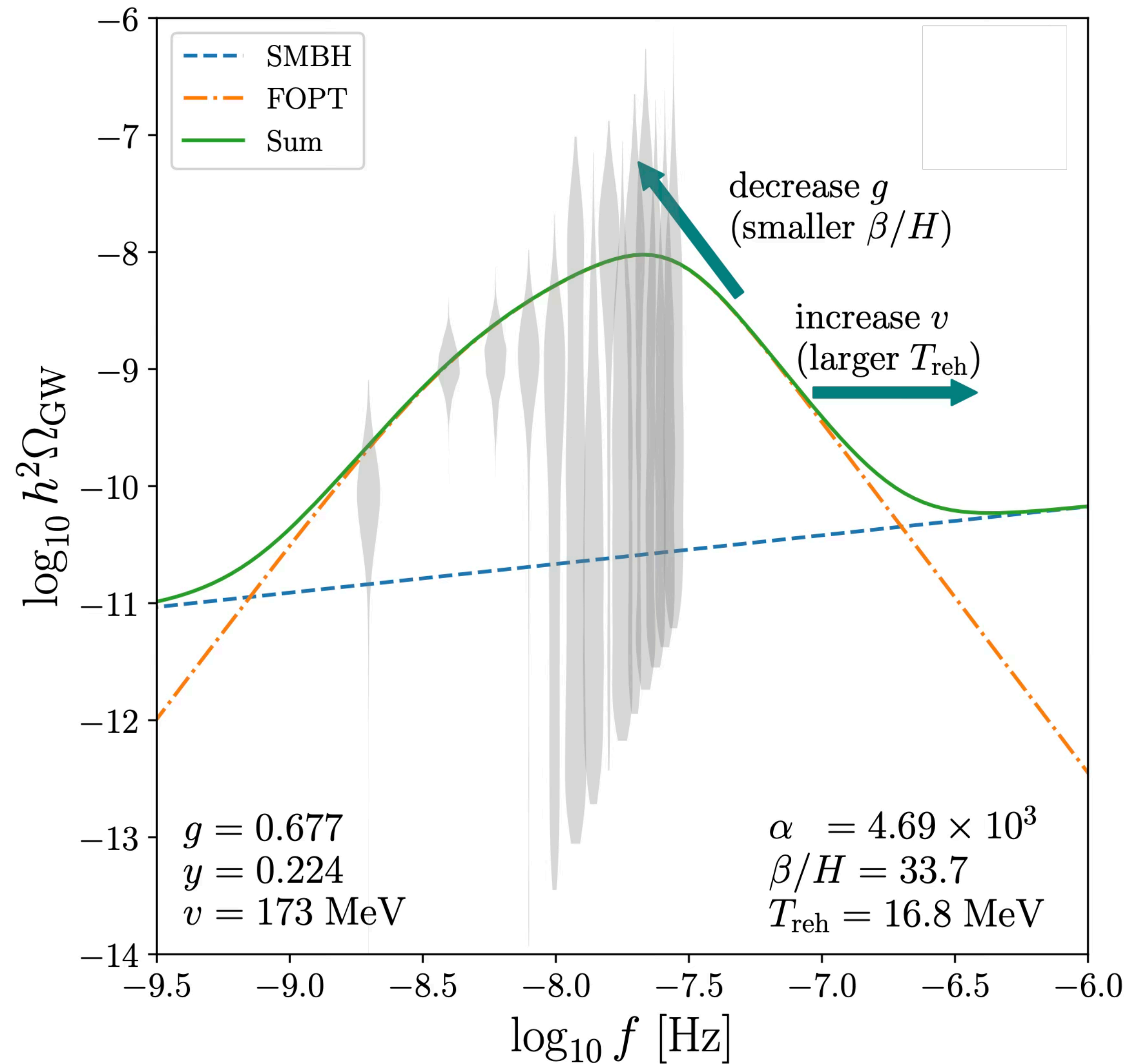
Thermalization becomes easy!

SM

CT+ [JCAP 08 (2025) 062]



All constraints can be circumvented



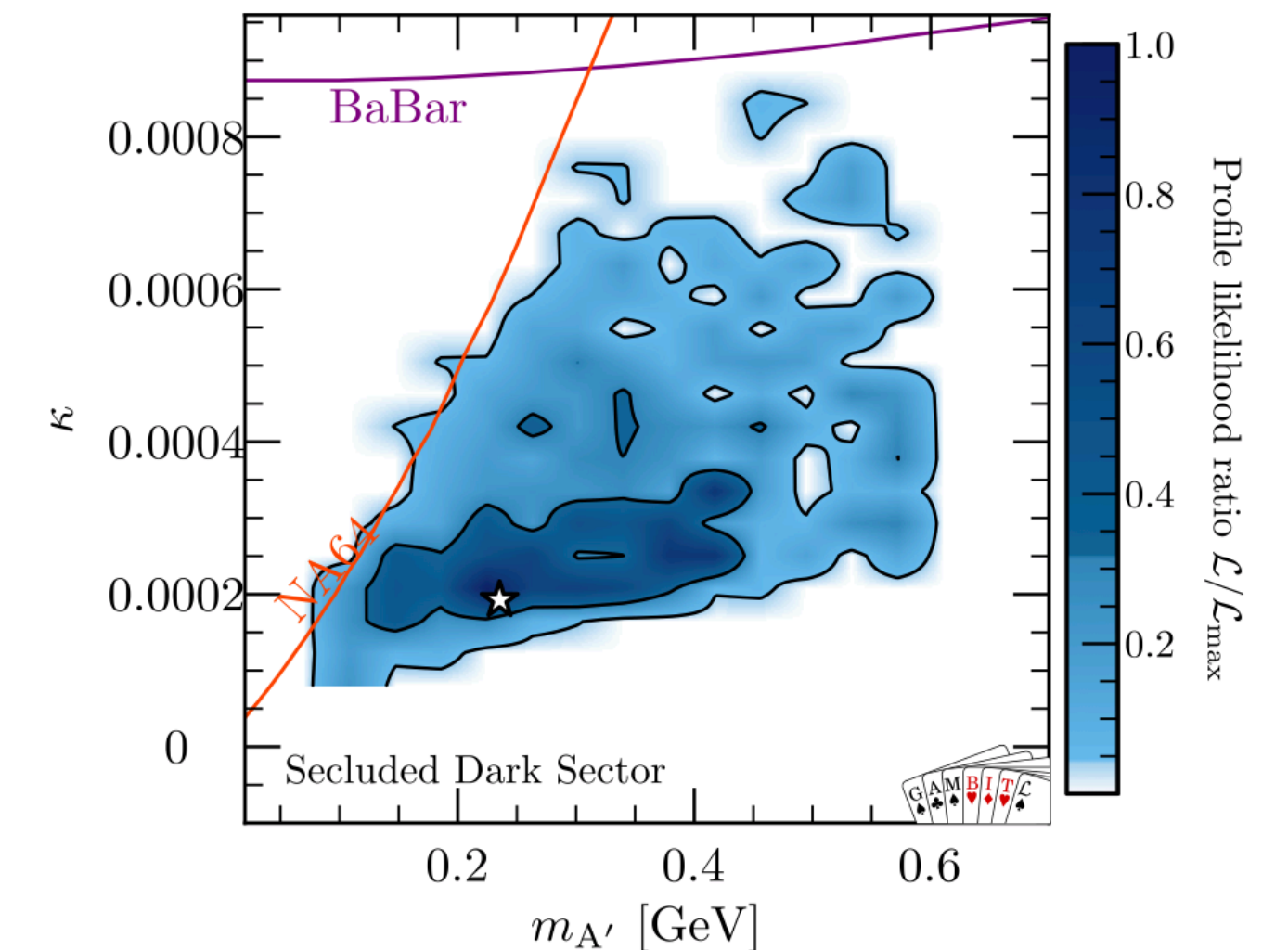
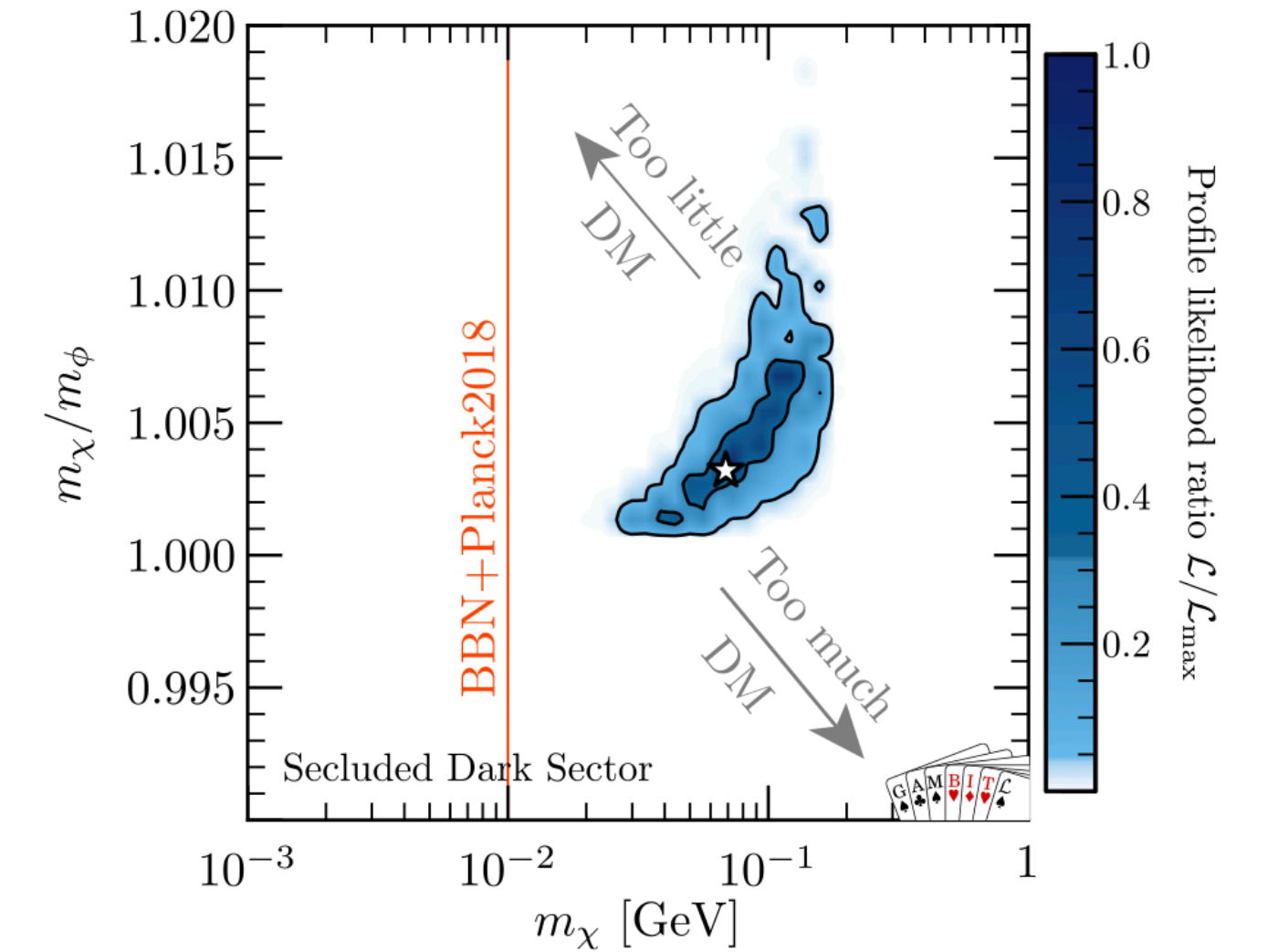
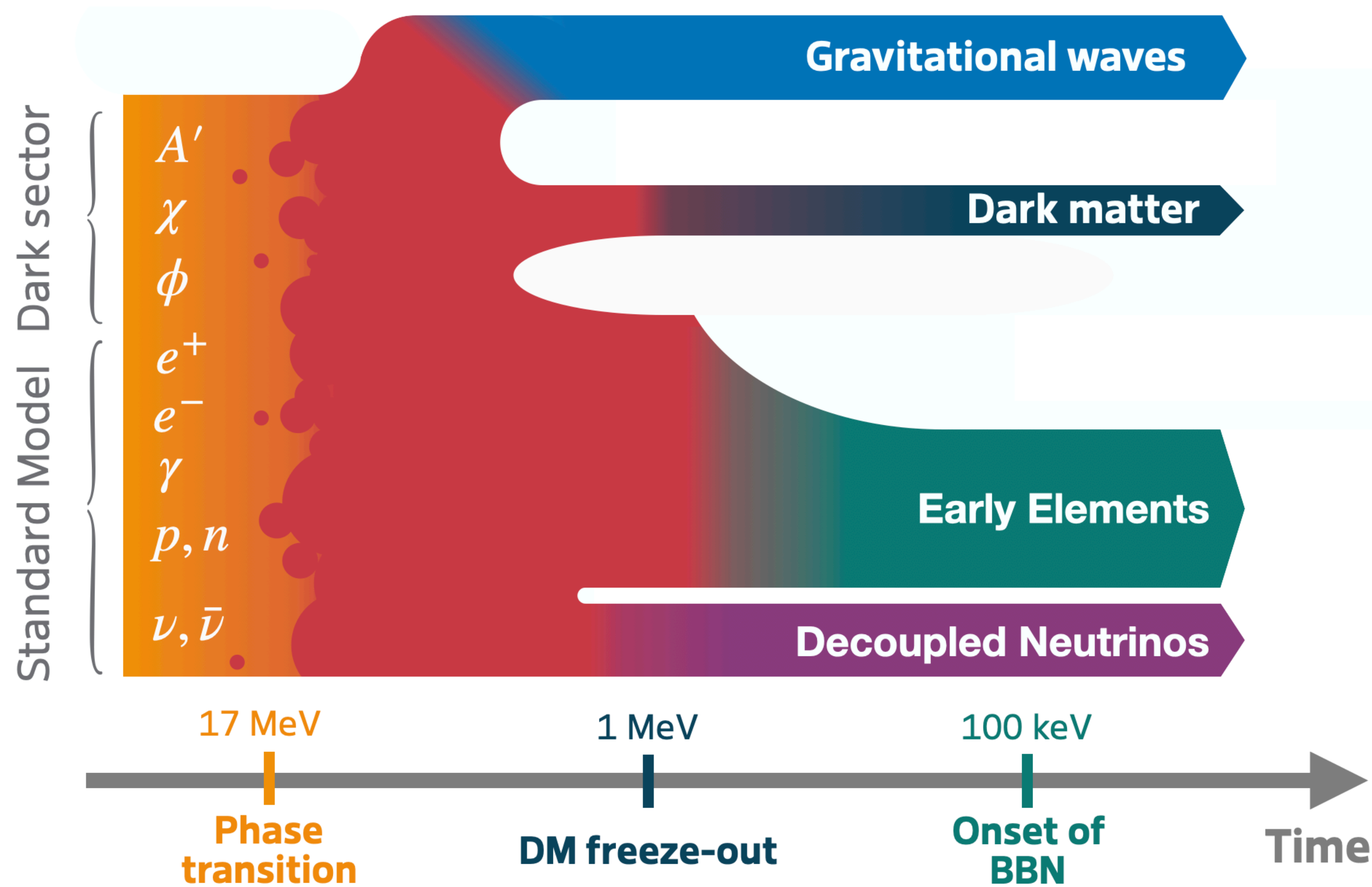
Global fit found parameter space with

- 100% of observed DM relic density
- Loud phase transition on top of „standard“ SMBH background
- Negligible impact on BBN and CMB
- No relevant direct + indirect detection + bullet cluster constraints
- Testable LDMX/Belle-II/NA64 prediction:

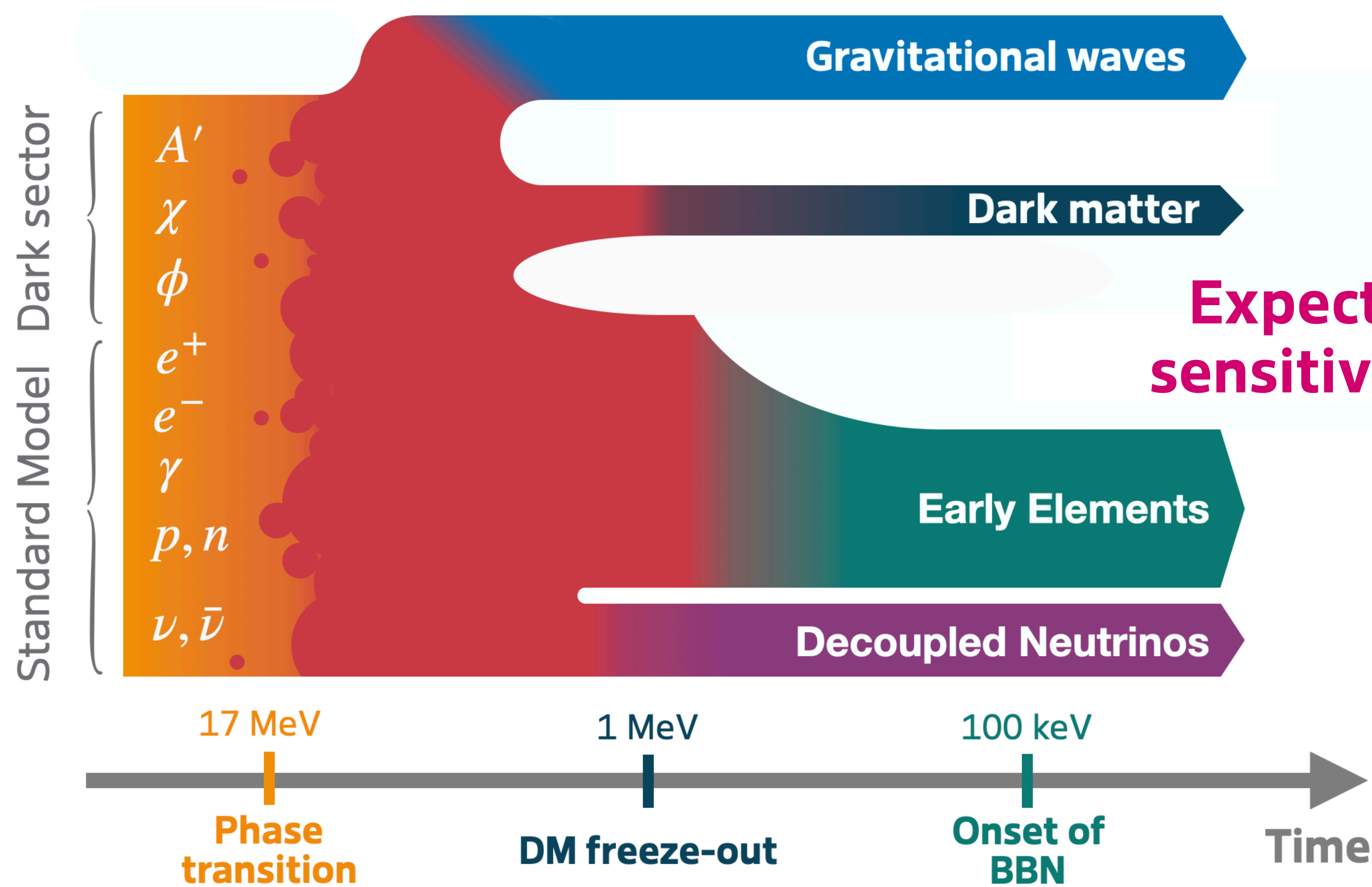
$$m_{A'} = 100 - 200 \text{ MeV}, \kappa \simeq 10^{-4}$$



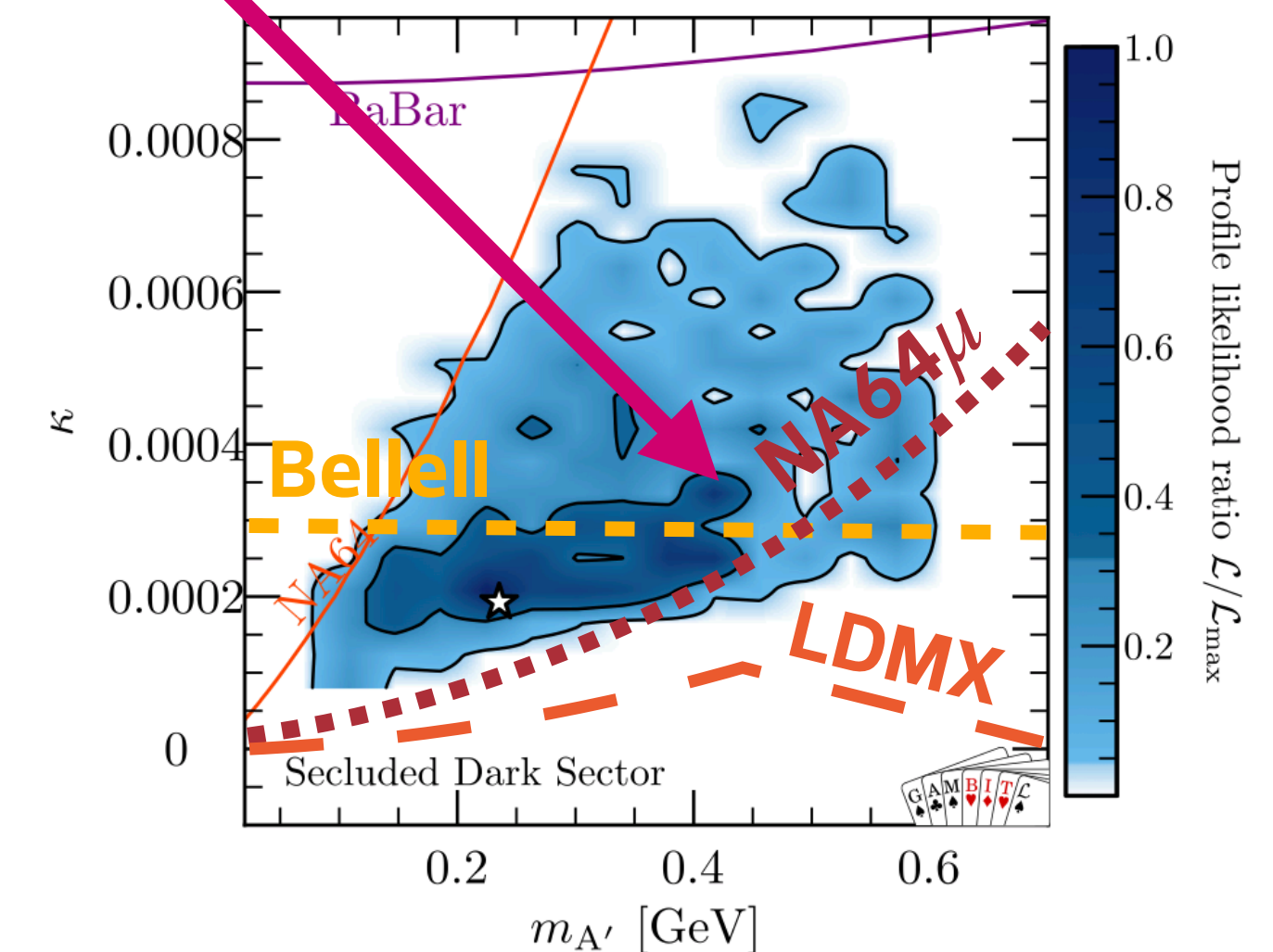
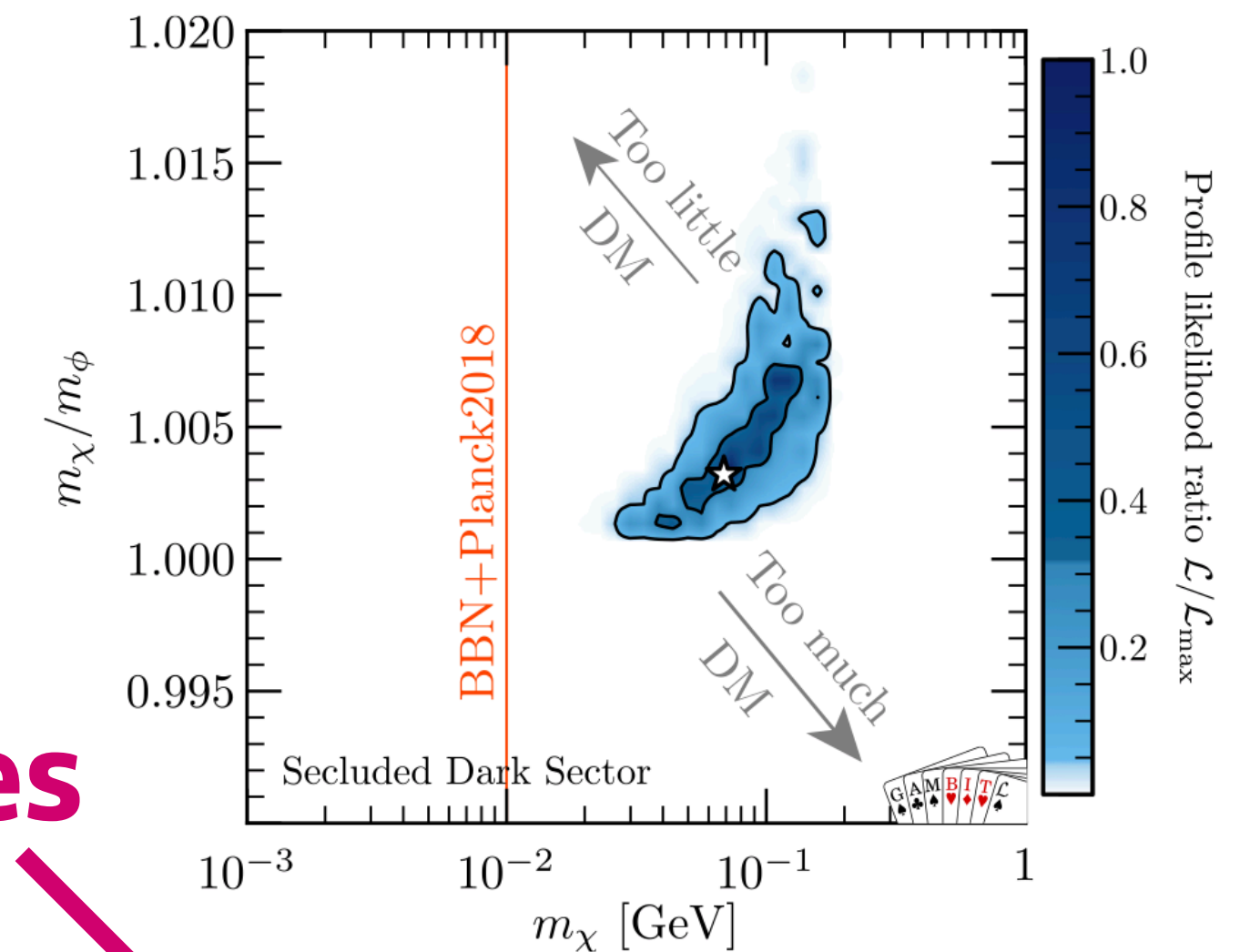
How does our scenario evade all available constraints?



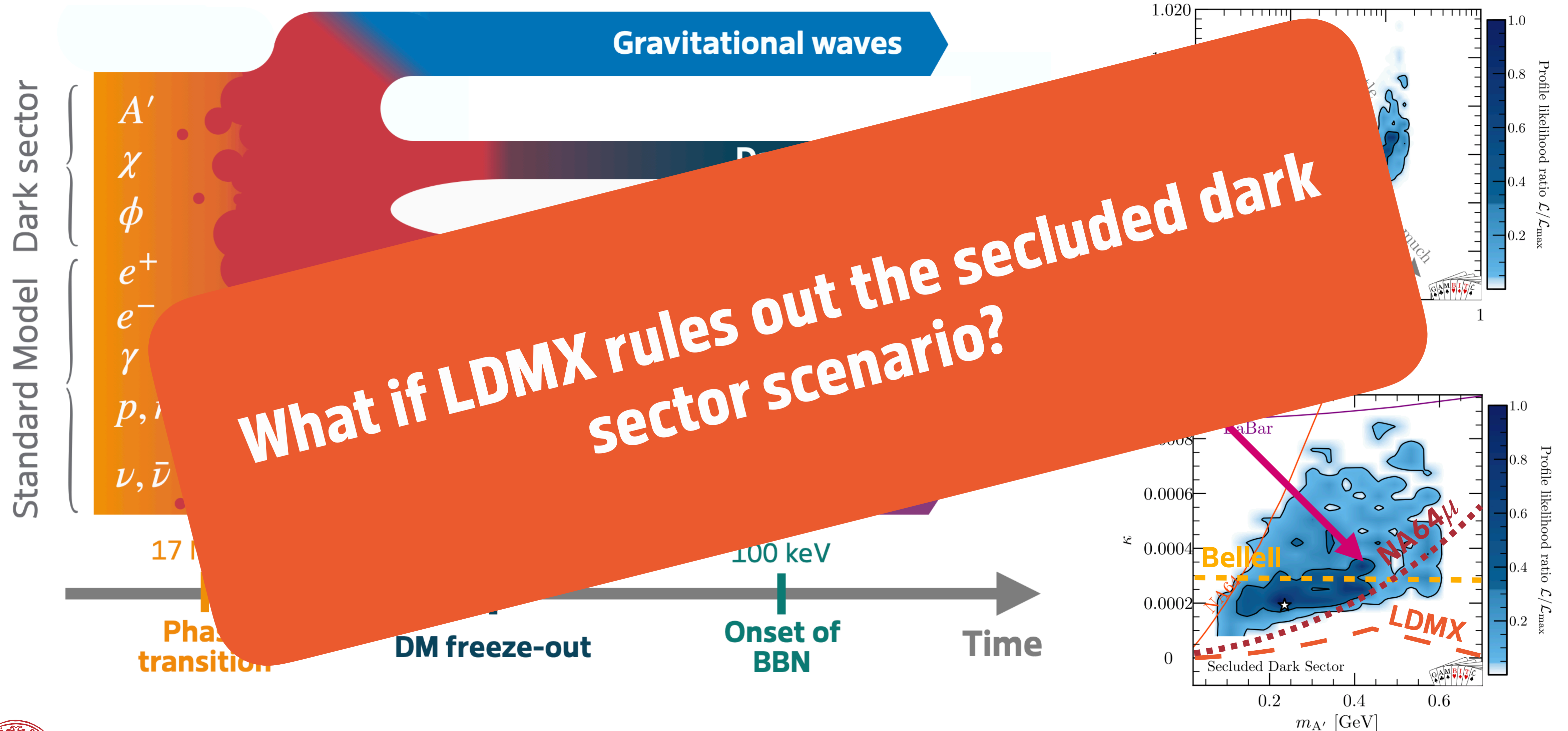
How does our scenario evade all available constraints?



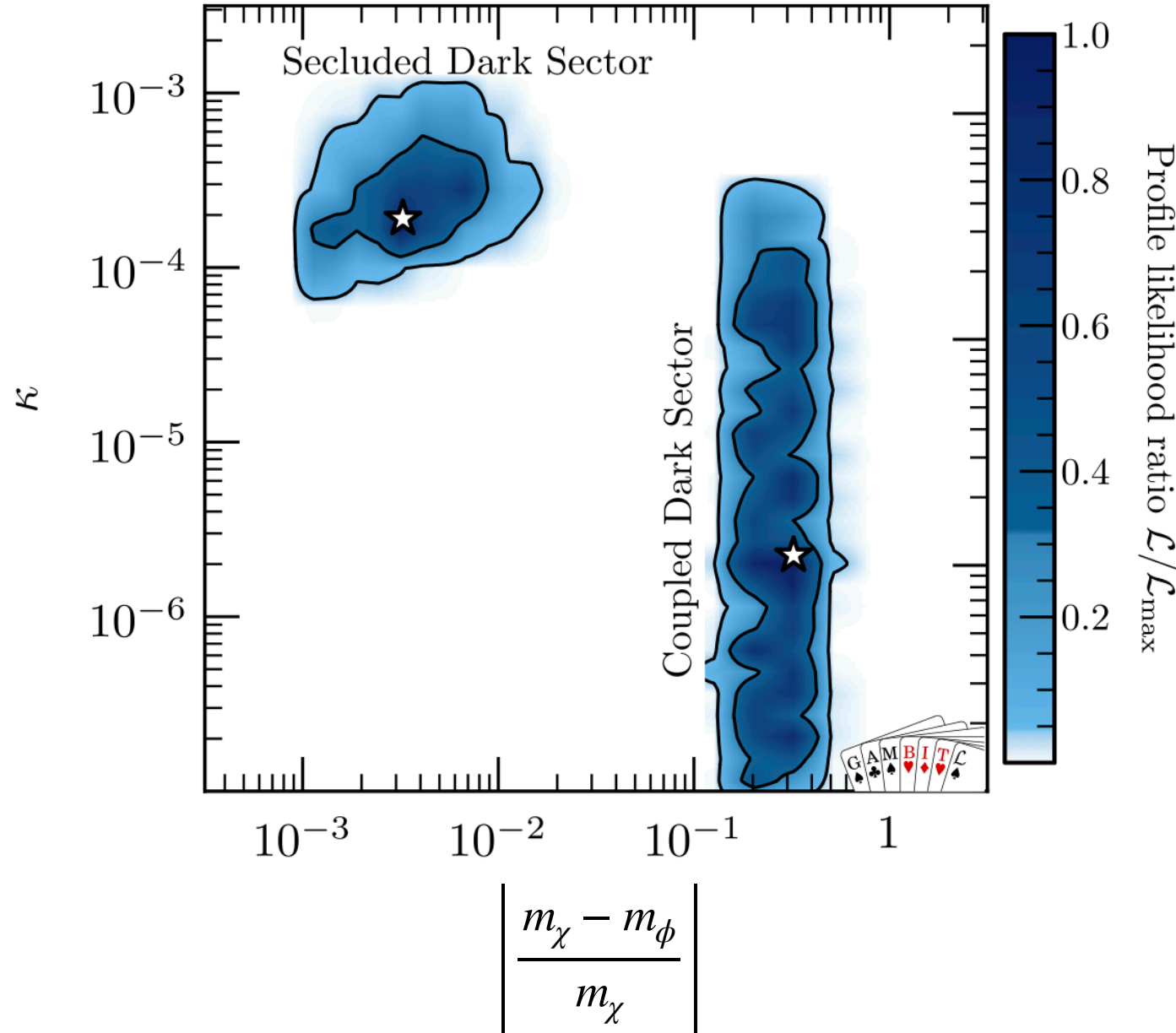
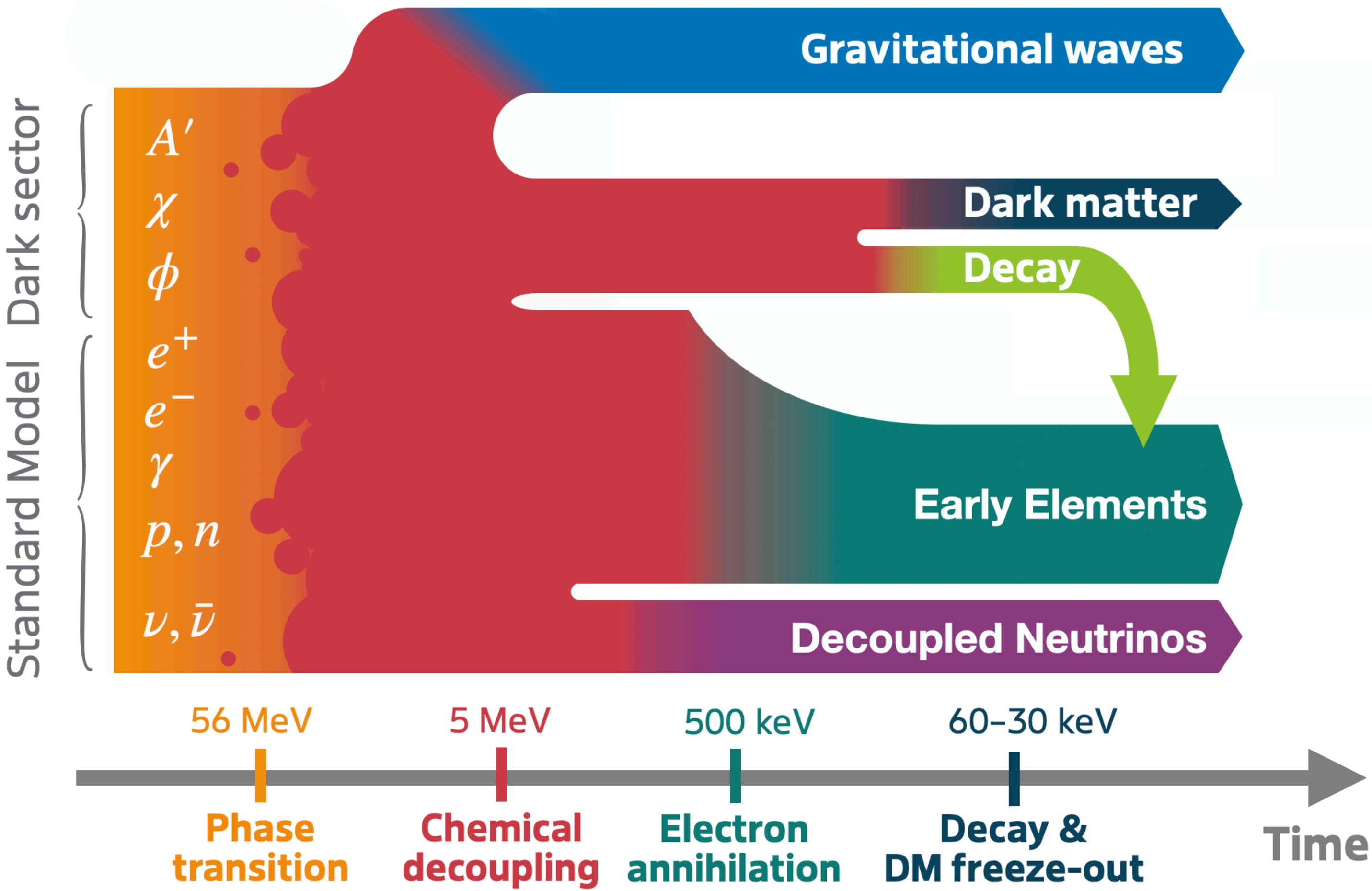
Expected sensitivities



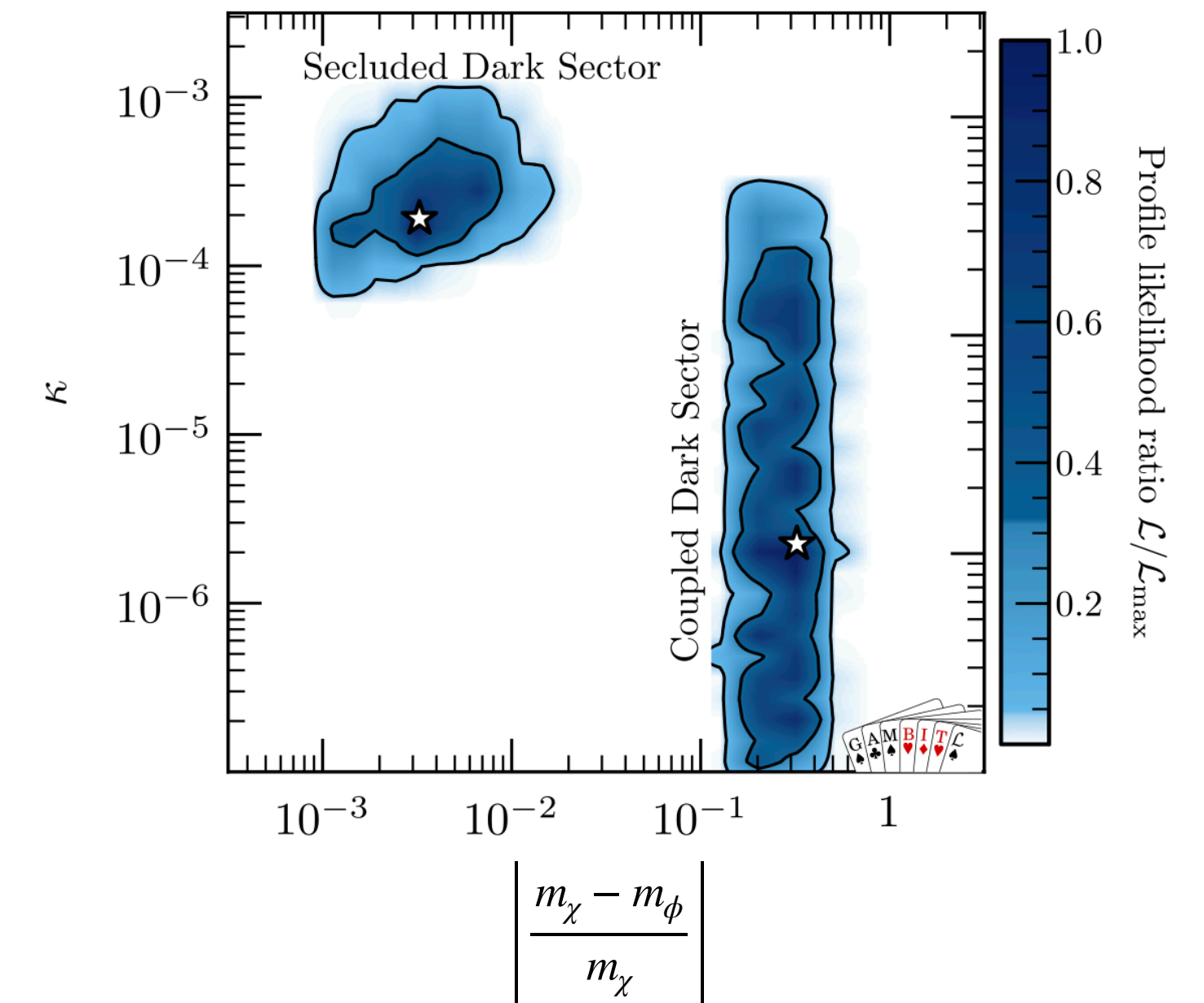
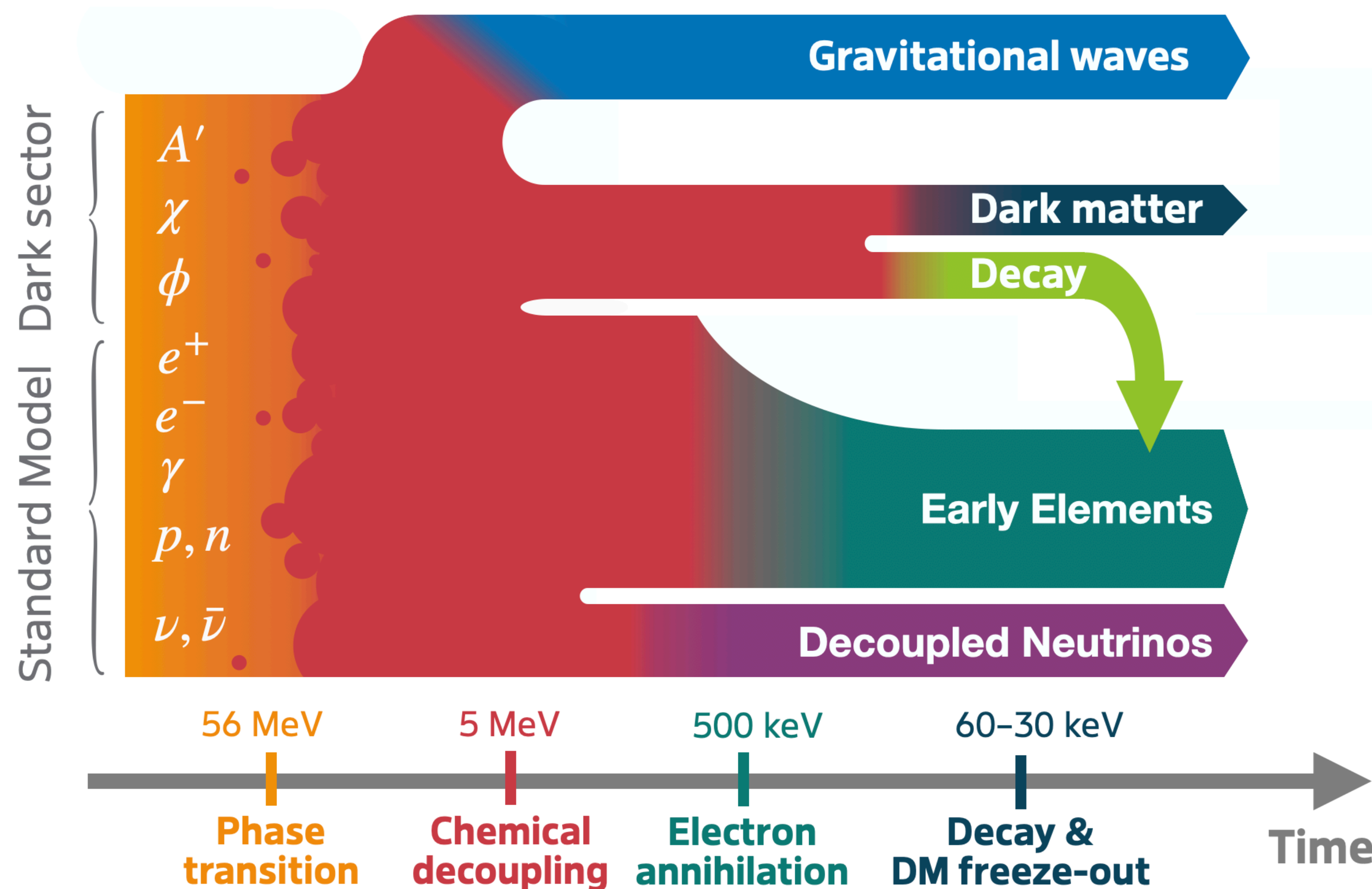
How does our scenario evade all available constraints?



Coupled DS scenario: incl dim-6 operator for $\phi \rightarrow ee$



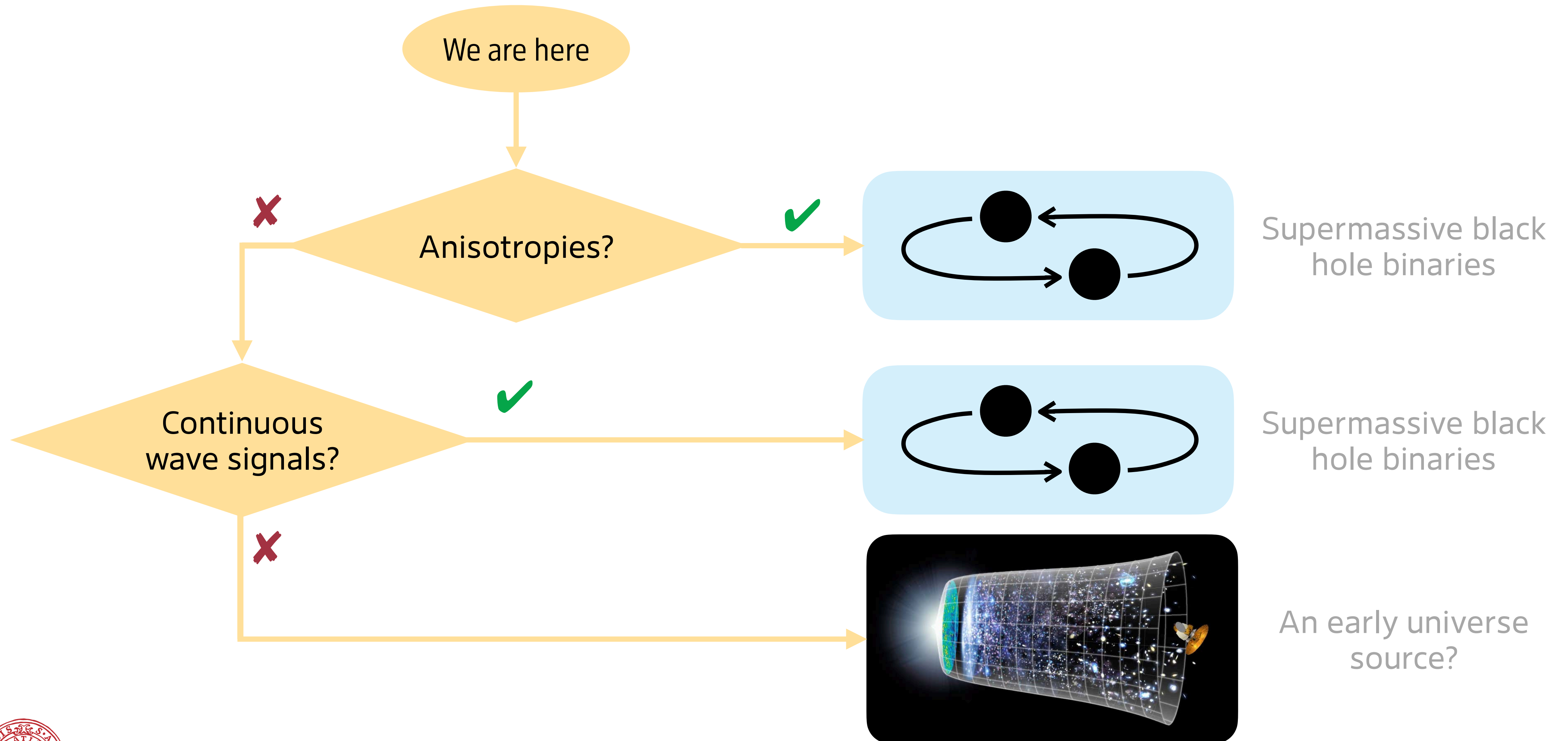
Coupled DS scenario: incl dim-6 operator for $\phi \rightarrow ee$



$\phi \rightarrow ee$ decays through a dim-6 operator open up the parameter space and save the model from potential future constraints



Grande finale: Quo vadis pulsar timing?



Time for a commercial break

In case you want to test your own phase transition models...

Welcome to TransitionListener v2.0!

Config

Type

Model

Output

Format

Description

SinglePoint

models/TL_conformal_dark_u1.py

scans/example_point/

txt

example point, conformal U(1) model

Scan parameters

Parameter

Value

g

0.7

v_GeV

0.1

y

0.01

Starting analysis of example point, conformal U(1) model

Input parameters

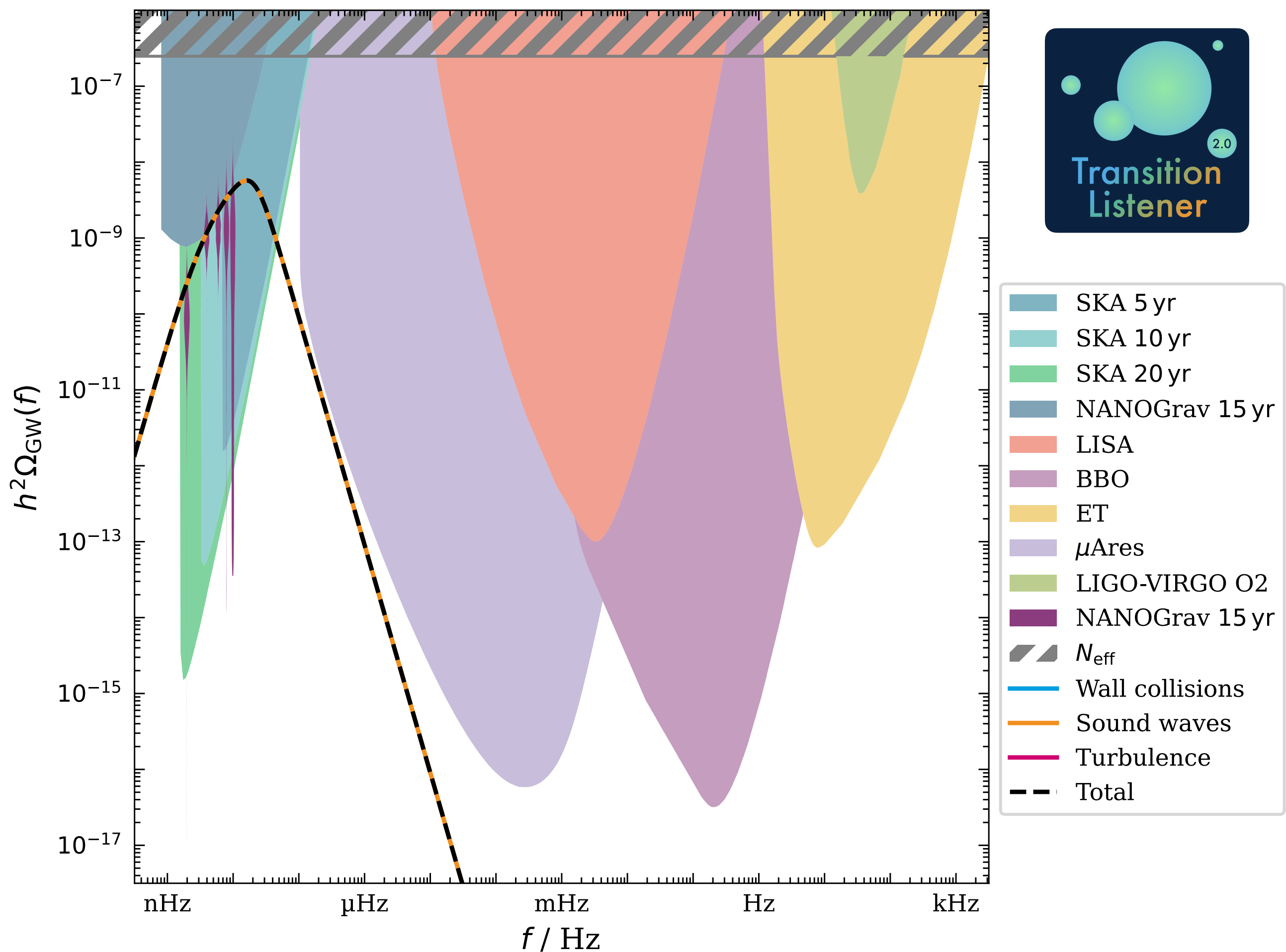
| Parameter | Value |
|-----------|------------------|
| g | 7.0000000000e-01 |
| y | 1.0000000000e-02 |
| v_GeV | 1.0000000000e-01 |

Derived parameters

| Parameter | Value |
|-----------|------------------|
| lambda | 1.6790420728e-02 |

Zero-temperature mass spectrum

| Particle | Type | Mass [GeV] |
|----------|---------|------------------|
| m_phi | boson | 2.2443542988e-02 |
| m_varphi | boson | 1.2957785586e-02 |
| m_A_T | boson | 7.0000000000e-02 |
| m_A_L | boson | 7.0000000000e-02 |
| m_psi1 | fermion | 7.0710678119e-04 |
| m_psi2 | fermion | 7.0710678119e-04 |



[Ongoing work Jonas Matuszak, code release very soon]

An example for the output of TransitionListener



After removing redundant phases, 2 phases remain.

Found 2 phases:

Phase 0

| Parameter | Value |
|-----------------|----------------------|
| Tmin / GeV | 2.35253655e-13 |
| Tmax / GeV | 0.025860343165319342 |
| phi(Tmin) / GeV | [0.1] |
| phi(Tmax) / GeV | [0.07745474] |

Phase 1

| Parameter | Value |
|-----------------|-------------------|
| Tmin / GeV | 2.35253655e-13 |
| Tmax / GeV | 0.25 |
| phi(Tmin) / GeV | [-4.13835065e-10] |
| phi(Tmax) / GeV | [-2.06018231e-07] |

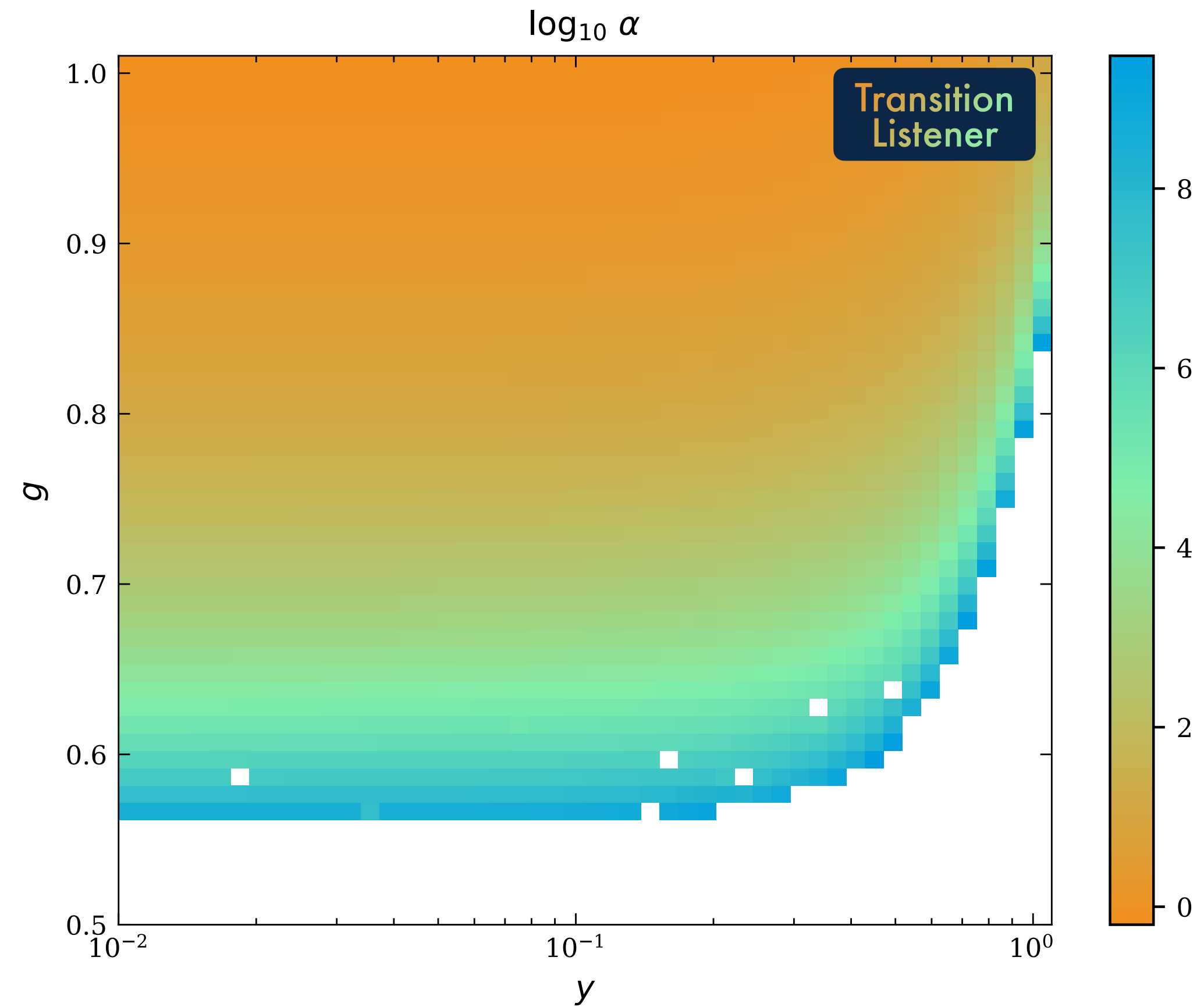
| FULL GW PARAMETERS | |
|--------------------------|--------------------|
| Parameter | Value |
| alpha | 5.1244e+02 |
| alpha_e | 5.1263e+02 |
| alpha_eq | 9.9747e+00 |
| alpha_hyd | 5.1244e+02 |
| alpha_inf | 1.1566e+00 |
| alpha_p | 5.1237e+02 |
| alpha_theta | 5.1244e+02 |
| betaH_from_RH | 6.2224e+01 |
| betaH_perc | 6.3285e+01 |
| c_s | 5.8587e-01 |
| c_s_bro | 5.8587e-01 |
| c_s_sym | 5.7748e-01 |
| coupled_hydrodynamics | True |
| D | 1 |
| g0 | 2 |
| g_eff_tot_reh | 1.4174e+01 |
| h0 | 3.9100e+00 |
| h_eff_tot_reh | 1.4161e+01 |
| kappa_phi | 0 |
| kappa_sw | 9.9164e-01 |
| kappa_turb | 0.0000e+00 |
| RH | 7.1120e-02 |
| step | 1 |
| Tcrit_SM_GeV | 2.1734e-02 |
| Tf_SM_GeV | 2.1215e-03 |
| Tnuc_SM_GeV | 2.6768e-03 |
| total_steps | 1 |
| Tperc | 2.2124e+01 |
| Tperc_SM_GeV | 2.2124e-03 |
| Treh | 101.39173177184342 |
| Treh_SM_GeV | 1.0139e-02 |
| v_wall | 1 |
| xi_crit | 4.3499e+00 |
| Warnings | |
| betaH_small | False |
| no_perc_splines | False |
| not_T0_global_min | False |
| too_weak_to_compute_perc | False |

| SNR VALUES AND OBSERVABILITY | | | |
|------------------------------|------------|------------------------------------|-------------|
| Detector | SNR | Should have been observed already? | Observable? |
| SKA_5_yrs | 7.0490e+03 | | ✓ |
| SKA_10_yrs | 8.6512e+04 | | ✓ |
| SKA_20_yrs | 6.5400e+05 | | ✓ |
| EPTA_18_yrs | 1.2500e+00 | ✓ | |
| NANOGrav_11_yrs | 3.7351e+00 | ✓ | |
| NANOGrav_15_yrs | 4.7029e+00 | ✗ | |
| LISA | 1.4366e-08 | | ✗ |
| B-DECIGO | 8.4122e-09 | | ✗ |
| DECIGO | 1.1909e-08 | | ✗ |
| BBO | 1.1978e-08 | | ✗ |
| ET | 9.4051e-09 | | ✗ |
| muAres | 5.8147e+00 | | ✗ |
| HLV_02 | 4.8743e-28 | ✗ | |
| HLVK_design | 3.3682e-26 | | ✗ |

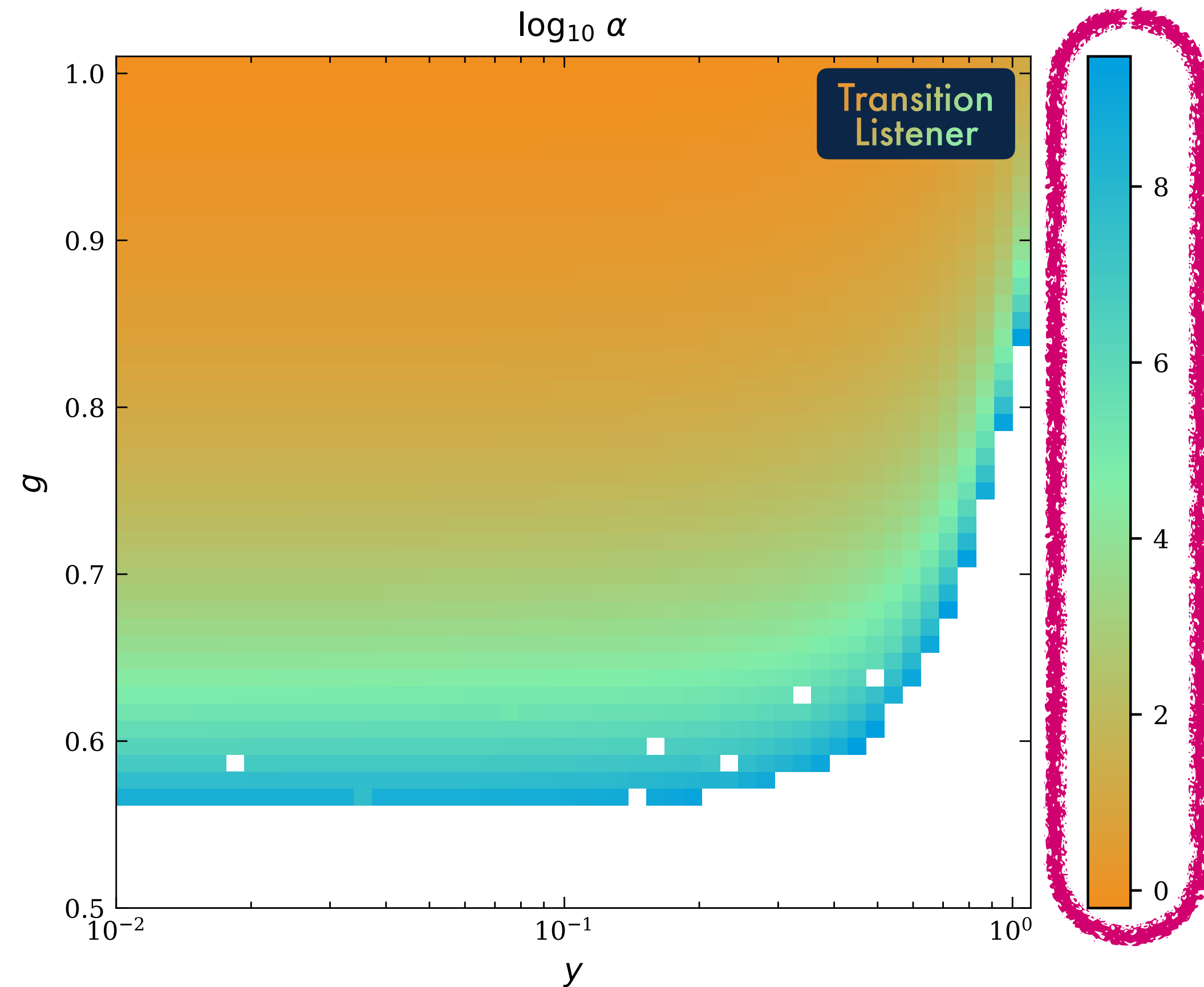
| LOG LIKELIHOODS FOR PULSAR TIMING ARRAYS | | | | | | |
|--|------|----------|---------|--------|------|------------|
| PTA | Bins | Variant | lnL | Δ lnL | σ | Within 3σ? |
| NANOGrav 15yr | 14 | PTArcade | -47.19 | -55.94 | 0.00 | ✓ |
| | 14 | mock | -110.02 | 6.89 | 3.71 | |
| | 14 | smooth | -47.19 | -55.94 | 0.00 | |
| NANOGrav 15yr | 5 | PTArcade | -52.95 | 23.40 | 6.84 | ✗ |
| | 5 | mock | -35.02 | 5.47 | 3.31 | |
| | 5 | smooth | -35.02 | 5.47 | 3.31 | |
| NANOGrav 12.5yr | 5 | PTArcade | -69.00 | 32.11 | 8.01 | ✗ |
| | 5 | mock | -45.02 | 8.13 | 4.03 | |
| | 5 | smooth | -45.02 | 8.13 | 4.03 | |
| IPTA DR2 | 13 | PTArcade | -31.93 | -73.74 | 0.00 | ✓ |
| | 13 | mock | -115.02 | 9.35 | 4.32 | |
| | 13 | smooth | -31.93 | -73.74 | 0.00 | |



If you're not convinced yet...



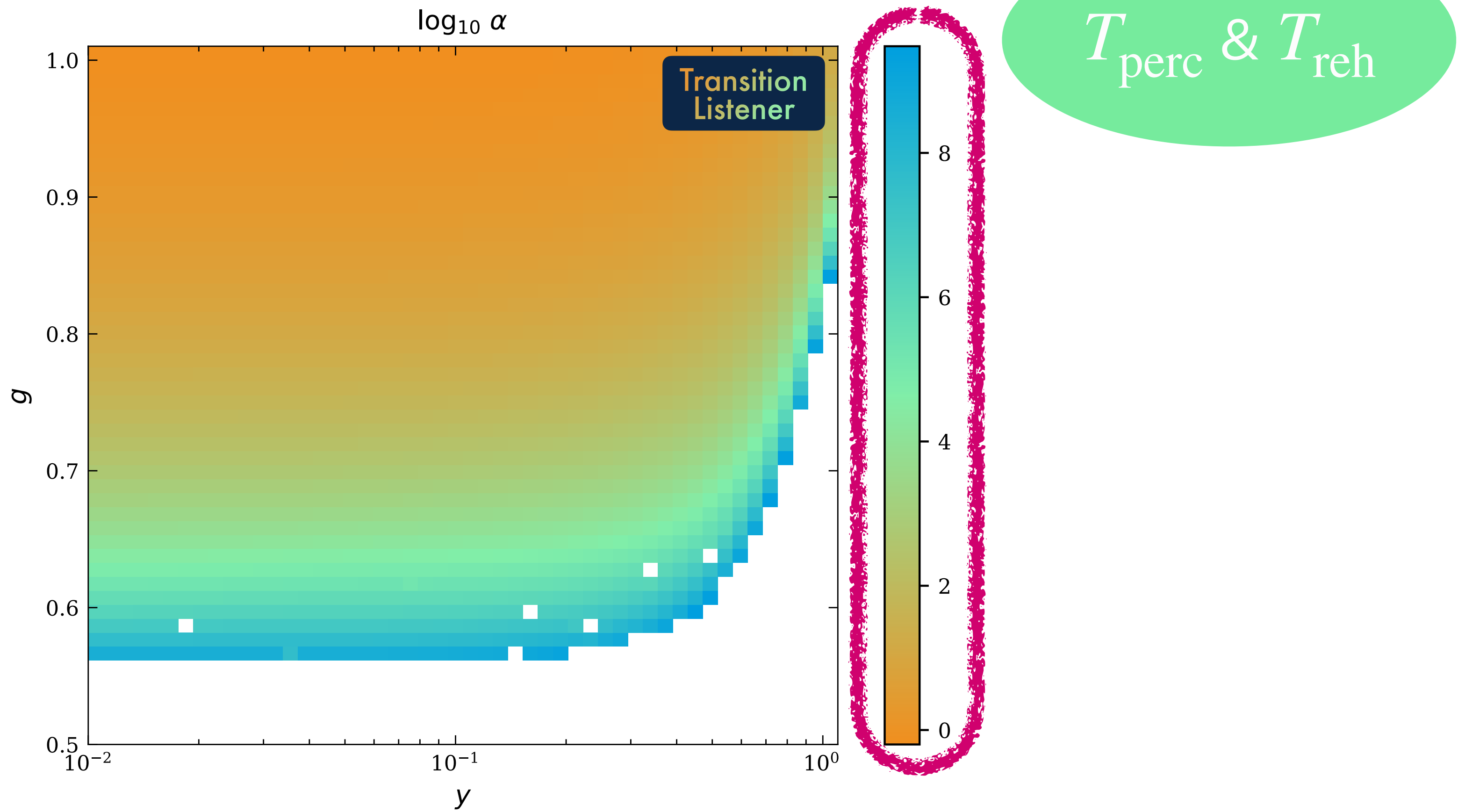
If you're not convinced yet...



Extreme supercooling with $\alpha = 10^{10}$ ✓



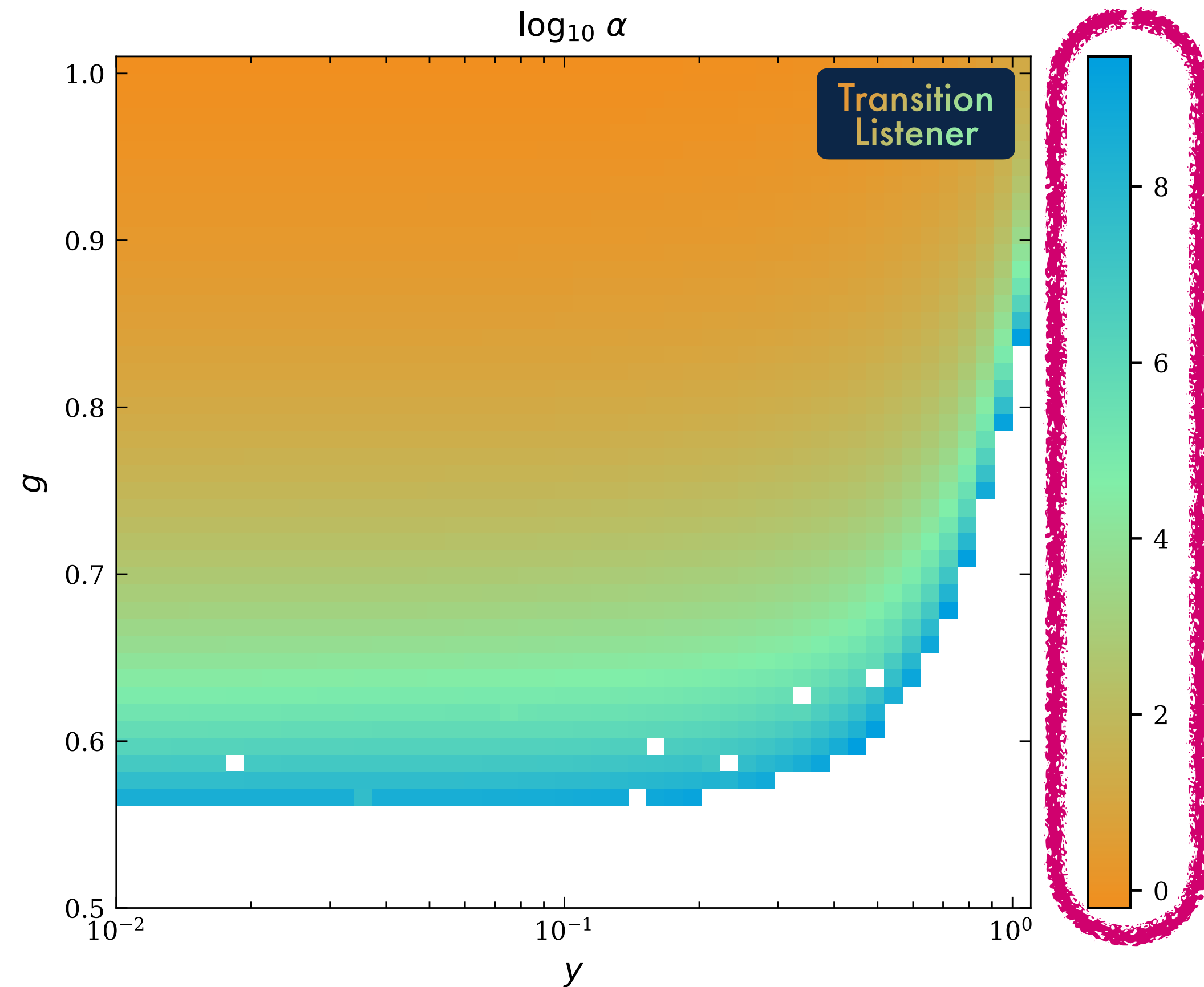
If you're not convinced yet...



Extreme supercooling with $\alpha = 10^{10}$ ✓



If you're not convinced yet...



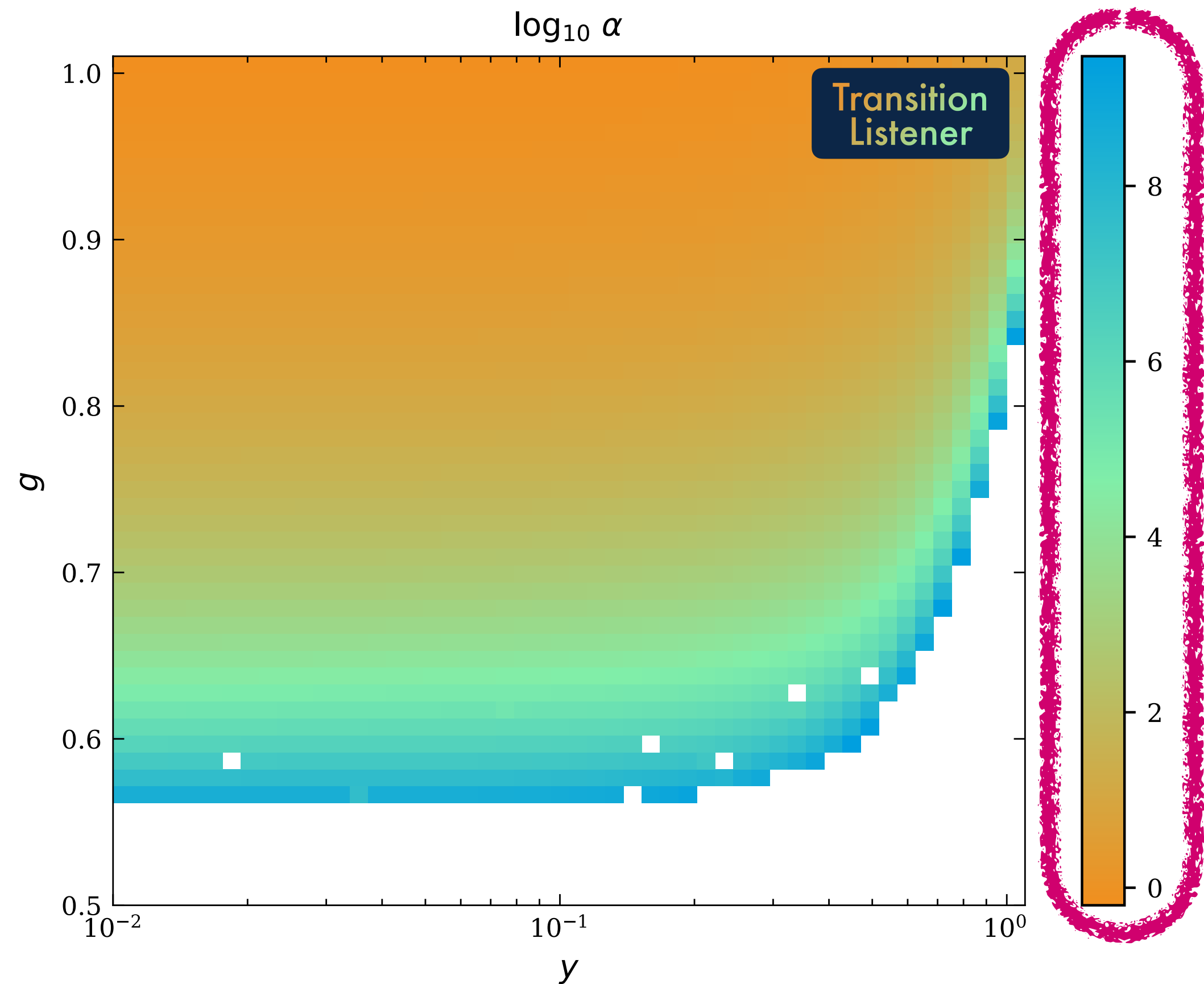
$T_{\text{perc}} \& T_{\text{reh}}$

Incl.
SM, SMEFT, dark
sectors, ...

Extreme supercooling with $\alpha = 10^{10}$ ✓



If you're not convinced yet...



$T_{\text{perc}} \text{ \& } T_{\text{reh}}$

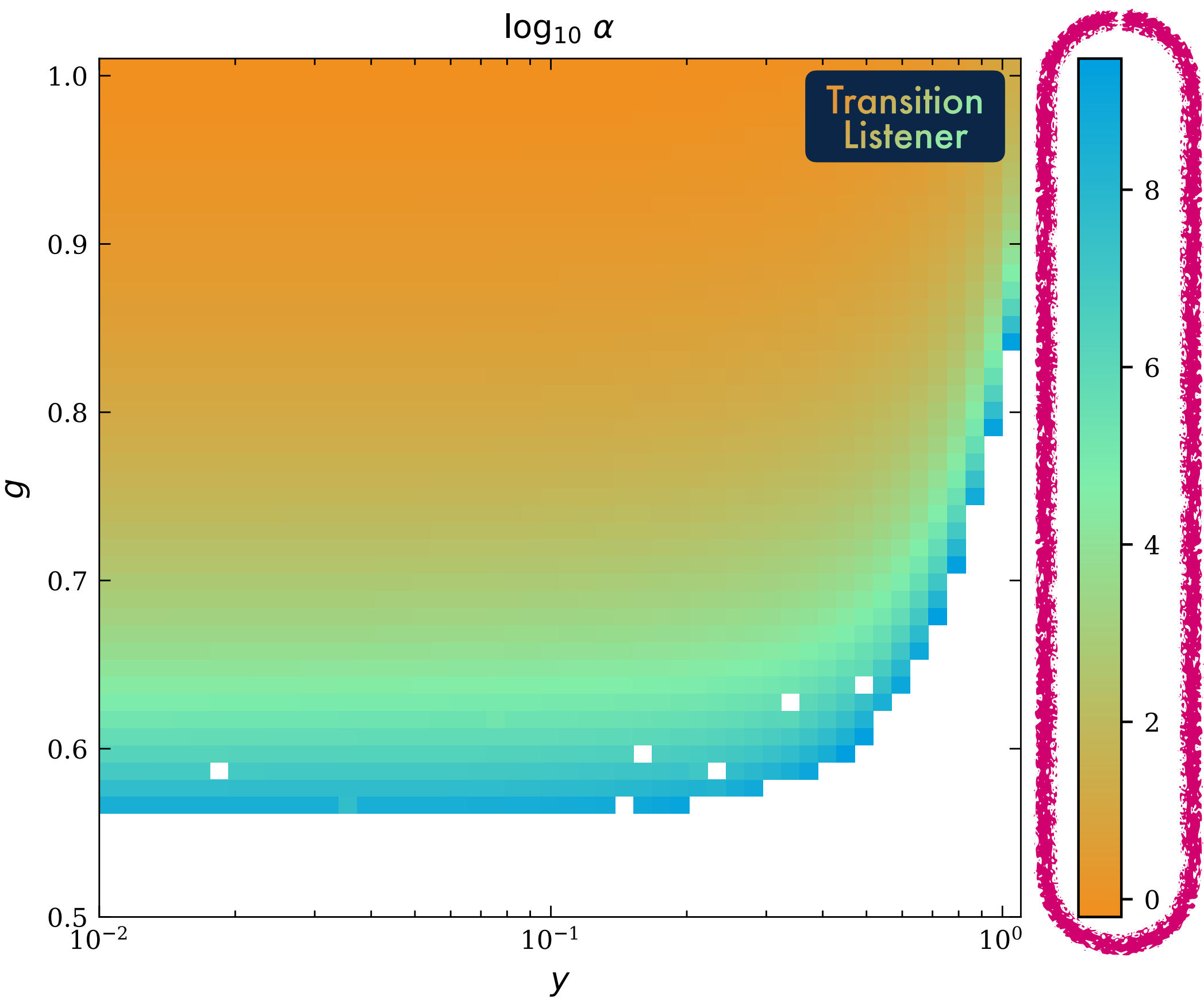
ν_{wall}

Incl.
SM, SMEFT, dark
sectors, ...

Extreme supercooling with $\alpha = 10^{10}$ ✓



If you're not convinced yet...



$T_{\text{perc}} \ \& \ T_{\text{reh}}$

Documentation

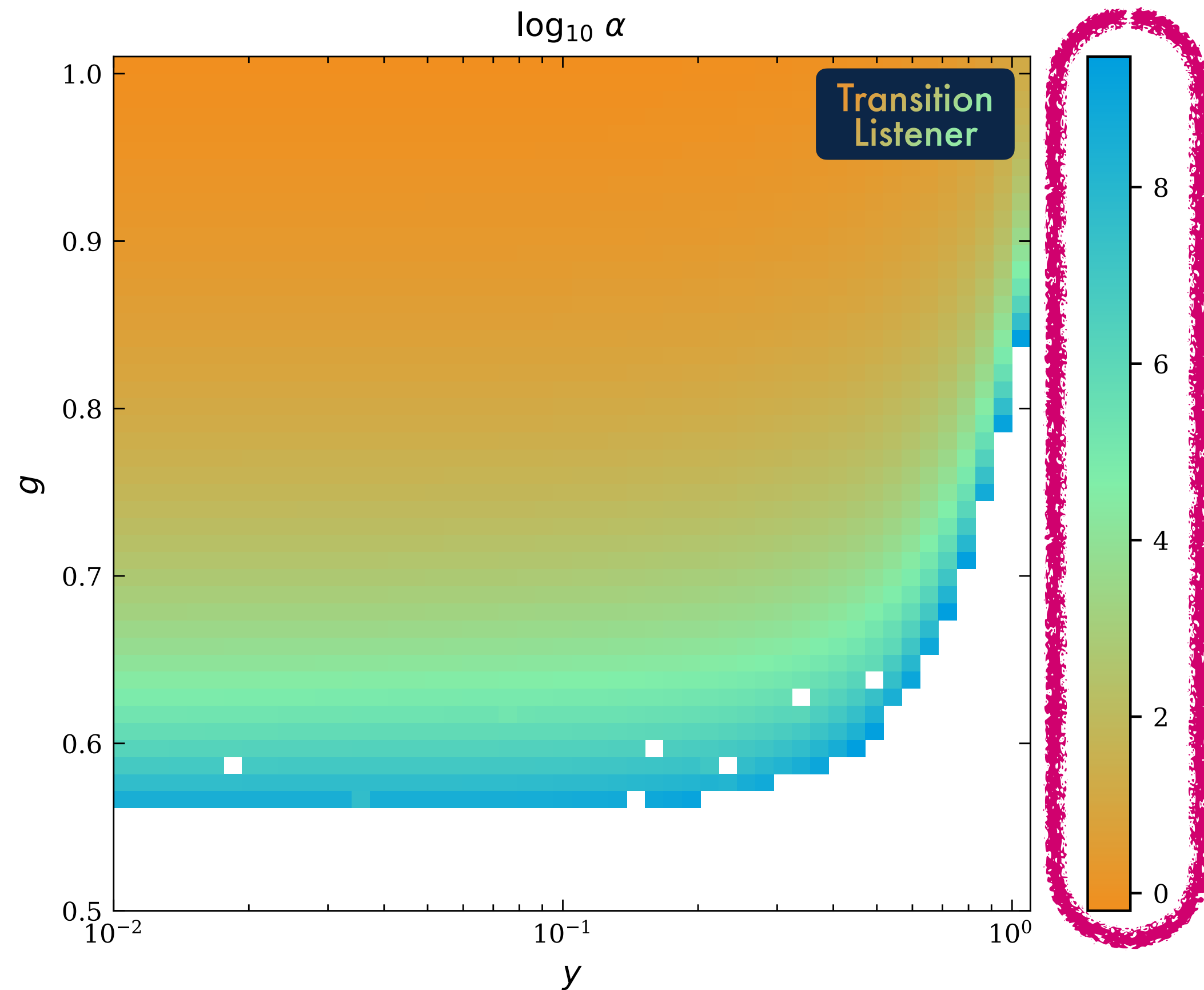
ν_{wall}

Incl.
SM, SMEFT, dark
sectors, ...

Extreme supercooling with $\alpha = 10^{10}$ ✓



If you're not convinced yet...



$T_{\text{perc}} \& T_{\text{reh}}$

Documentation

Proper error
handling

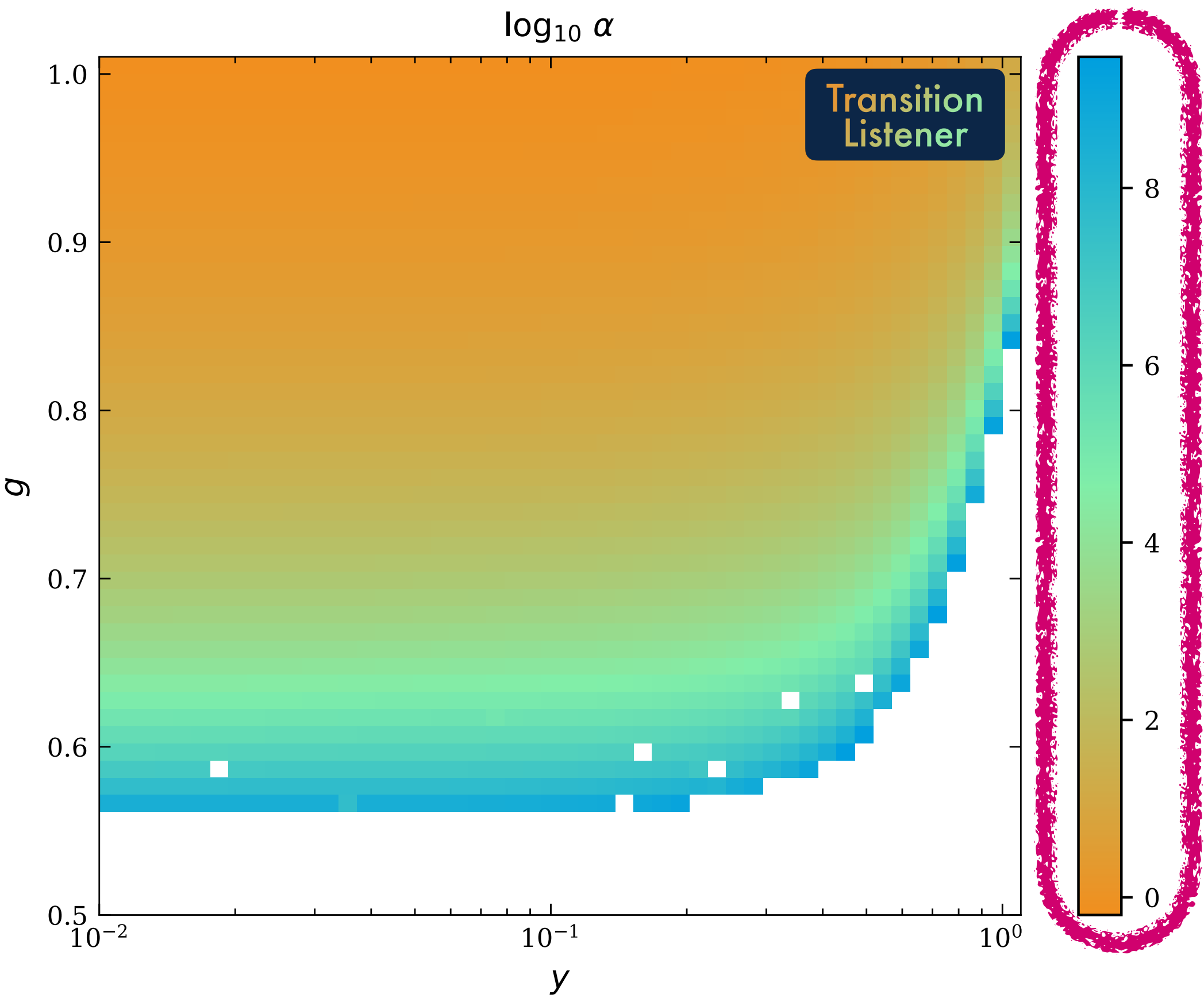
ν_{wall}

Incl.
SM, SMEFT, dark
sectors, ...

Extreme supercooling with $\alpha = 10^{10}$ ✓



If you're not convinced yet...



$T_{\text{perc}} \ \& \ T_{\text{reh}}$

Documentation

Proper error handling

Not just EWSB

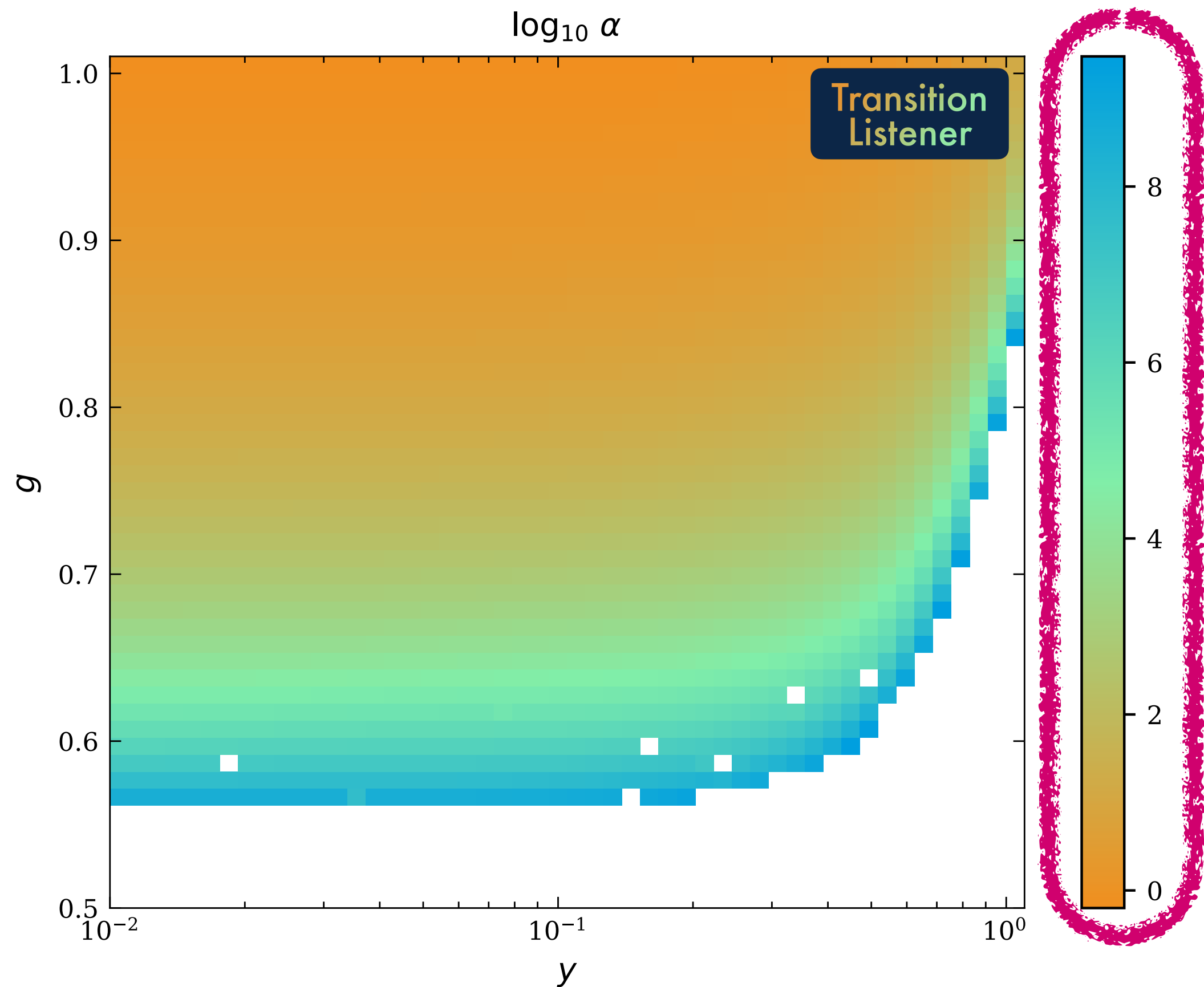
ν_{wall}

Incl.
SM, SMEFT, dark
sectors, ...

Extreme supercooling with $\alpha = 10^{10}$ ✓



If you're not convinced yet...



$T_{\text{perc}} \text{ \& } T_{\text{reh}}$

Documentation

Proper error handling

Not just EWSB

Several Higgs fields

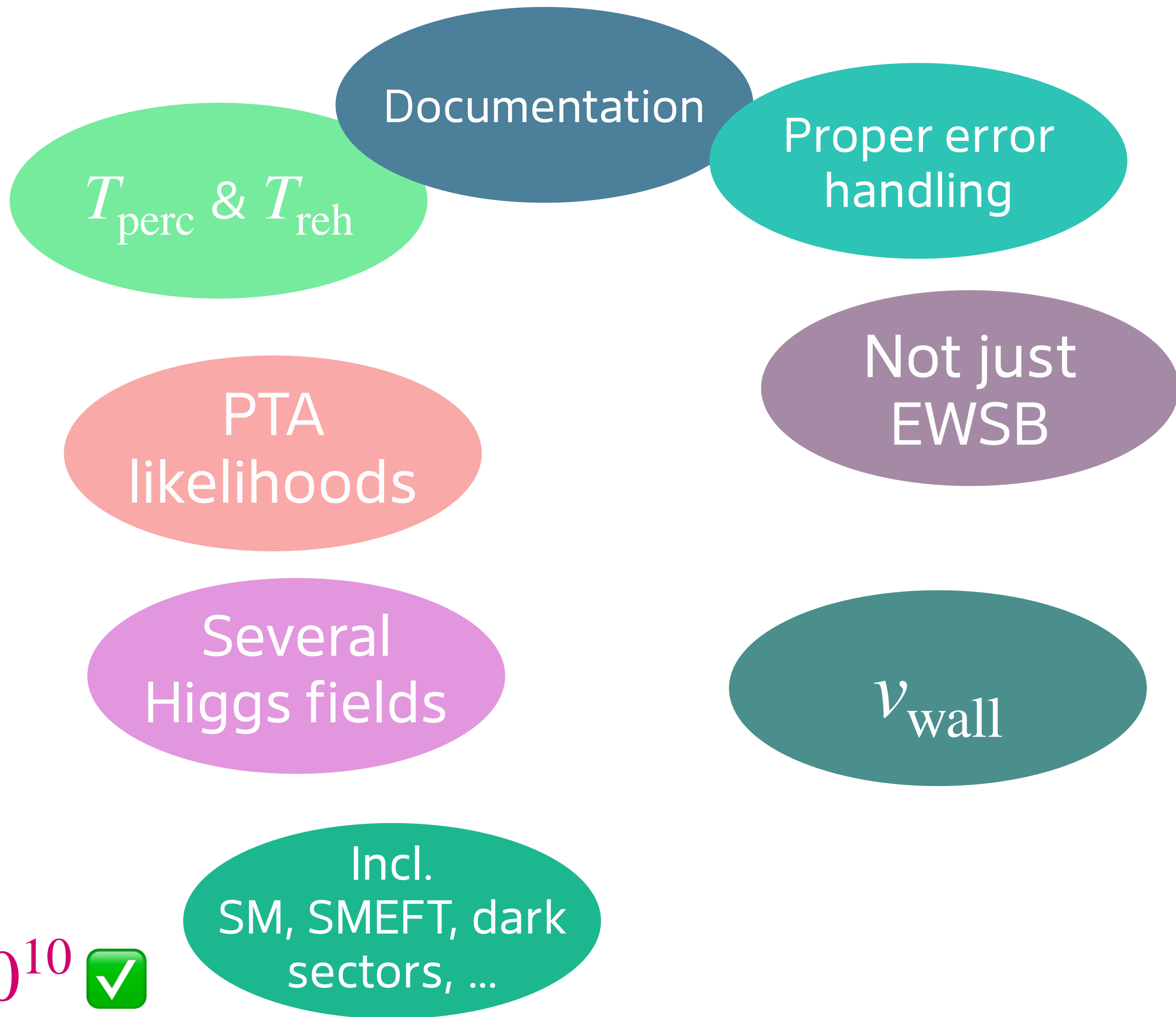
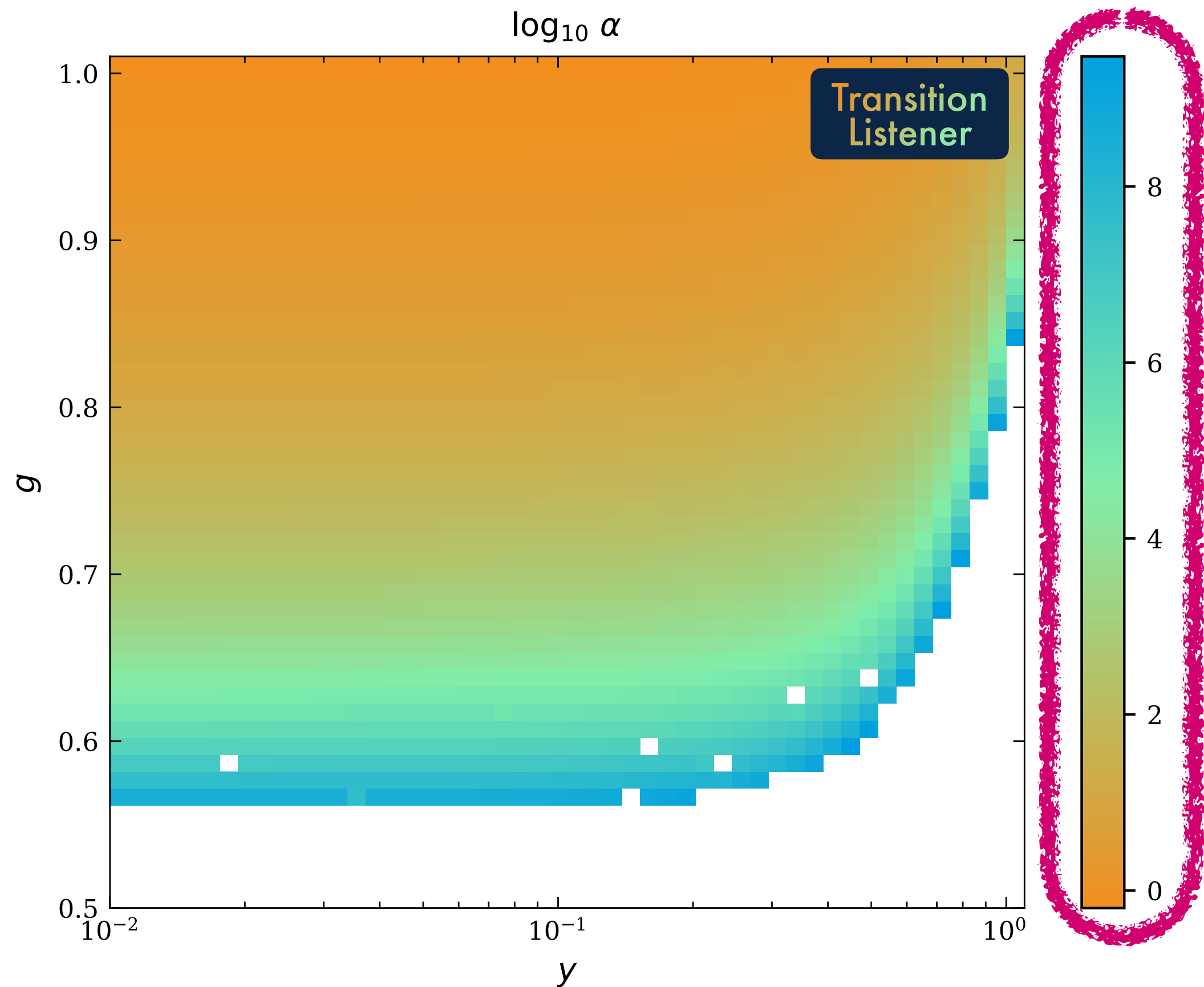
ν_{wall}

Incl. SM, SMEFT, dark sectors, ...

Extreme supercooling with $\alpha = 10^{10}$ ✓



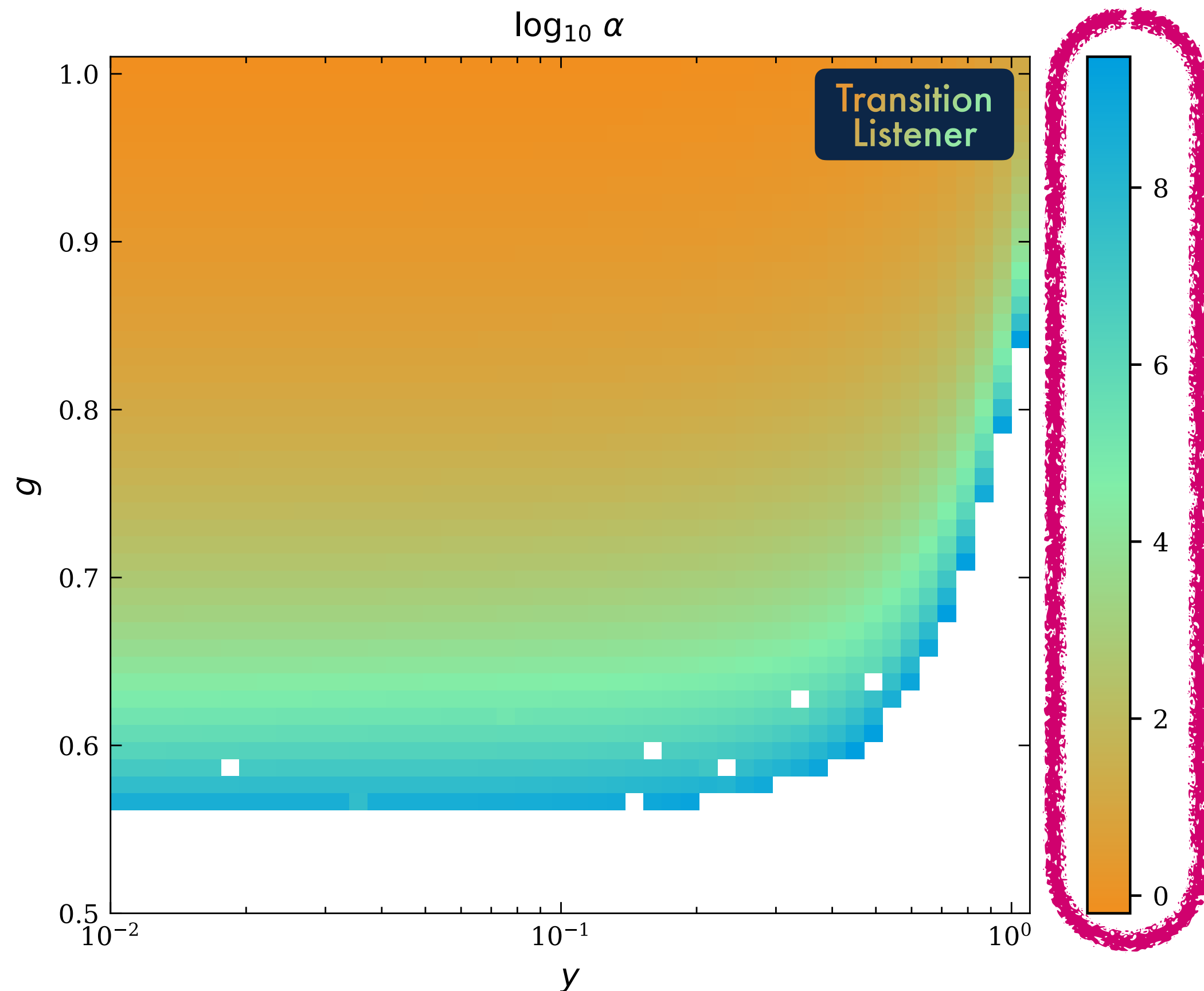
If you're not convinced yet...



Extreme supercooling with $\alpha = 10^{10}$ ✓



If you're not convinced yet...

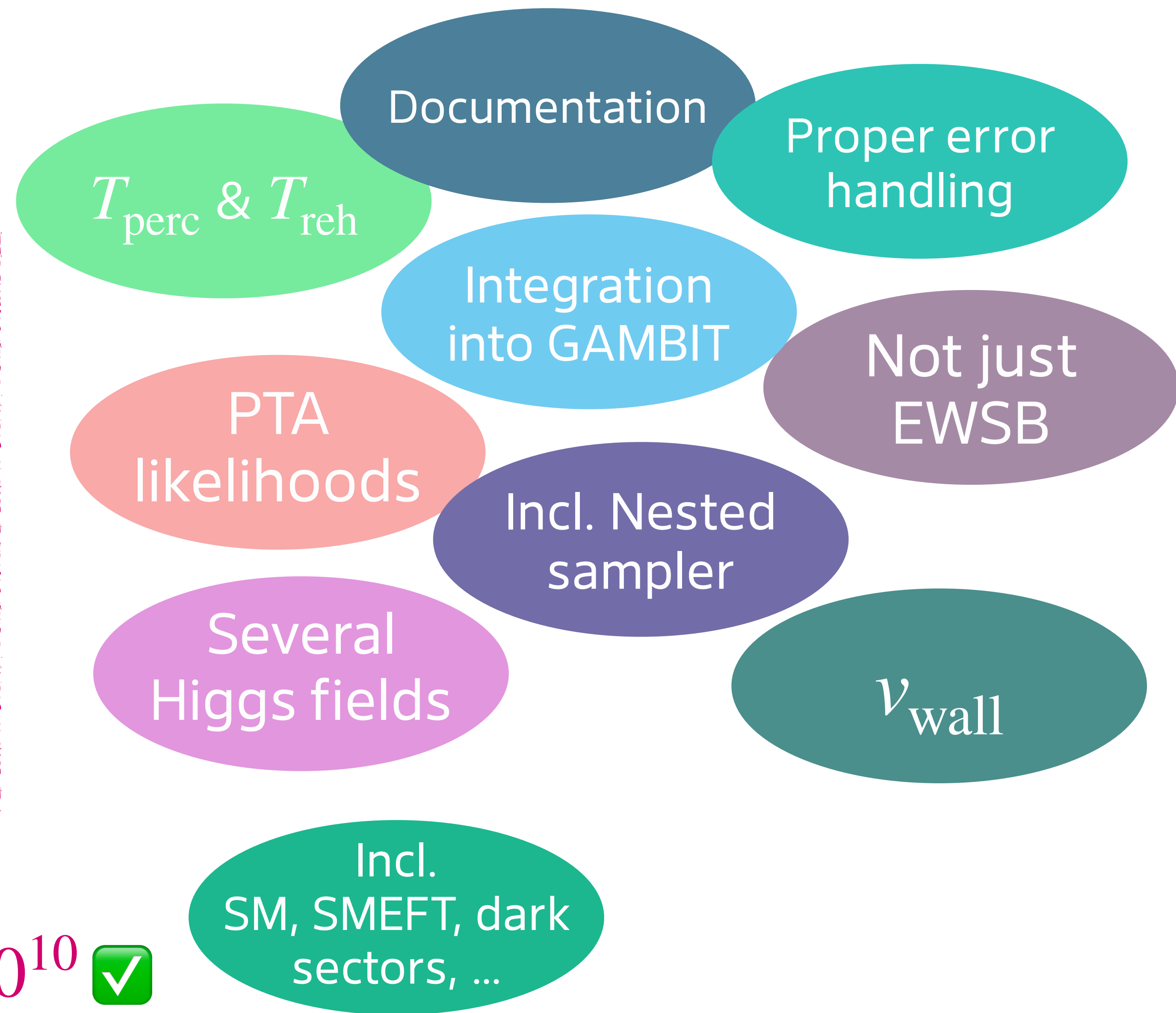
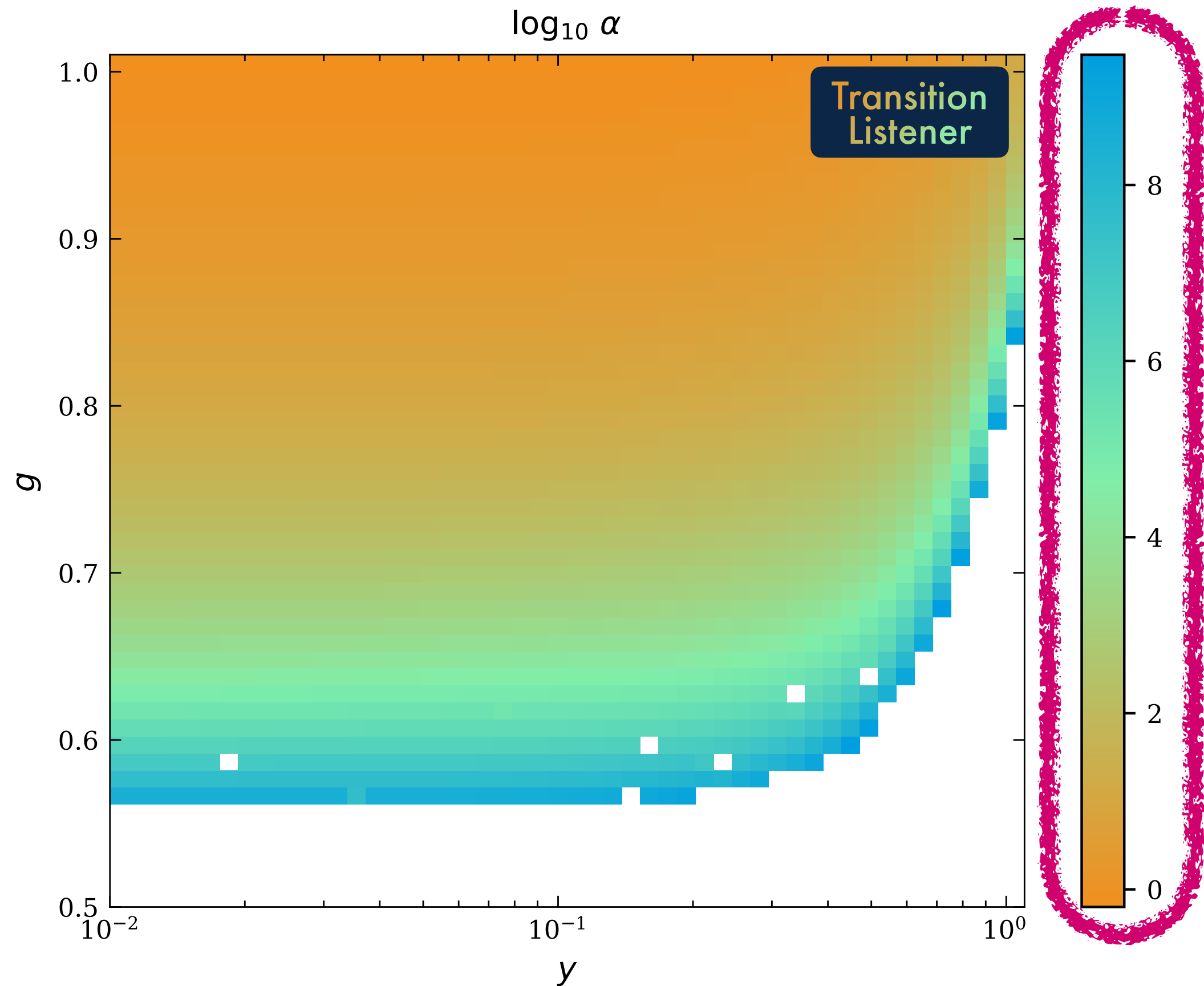


- $T_{\text{perc}} \text{ \& } T_{\text{reh}}$
- Documentation
- Proper error handling
- PTA likelihoods
- Not just EWSB
- Incl. Nested sampler
- Several Higgs fields
- ν_{wall}
- Incl. SM, SMEFT, dark sectors, ...

Extreme supercooling with $\alpha = 10^{10}$ ✓



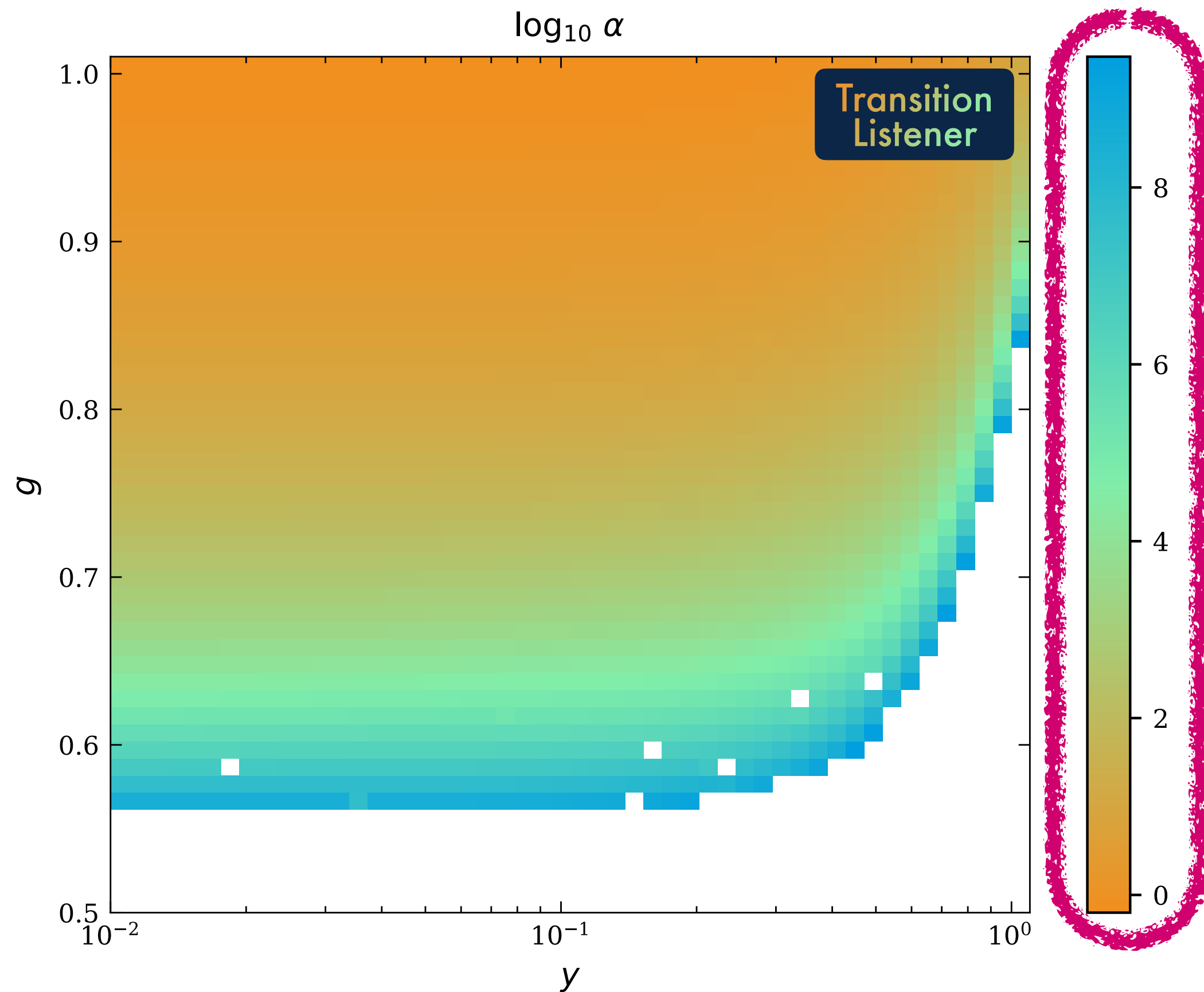
If you're not convinced yet...



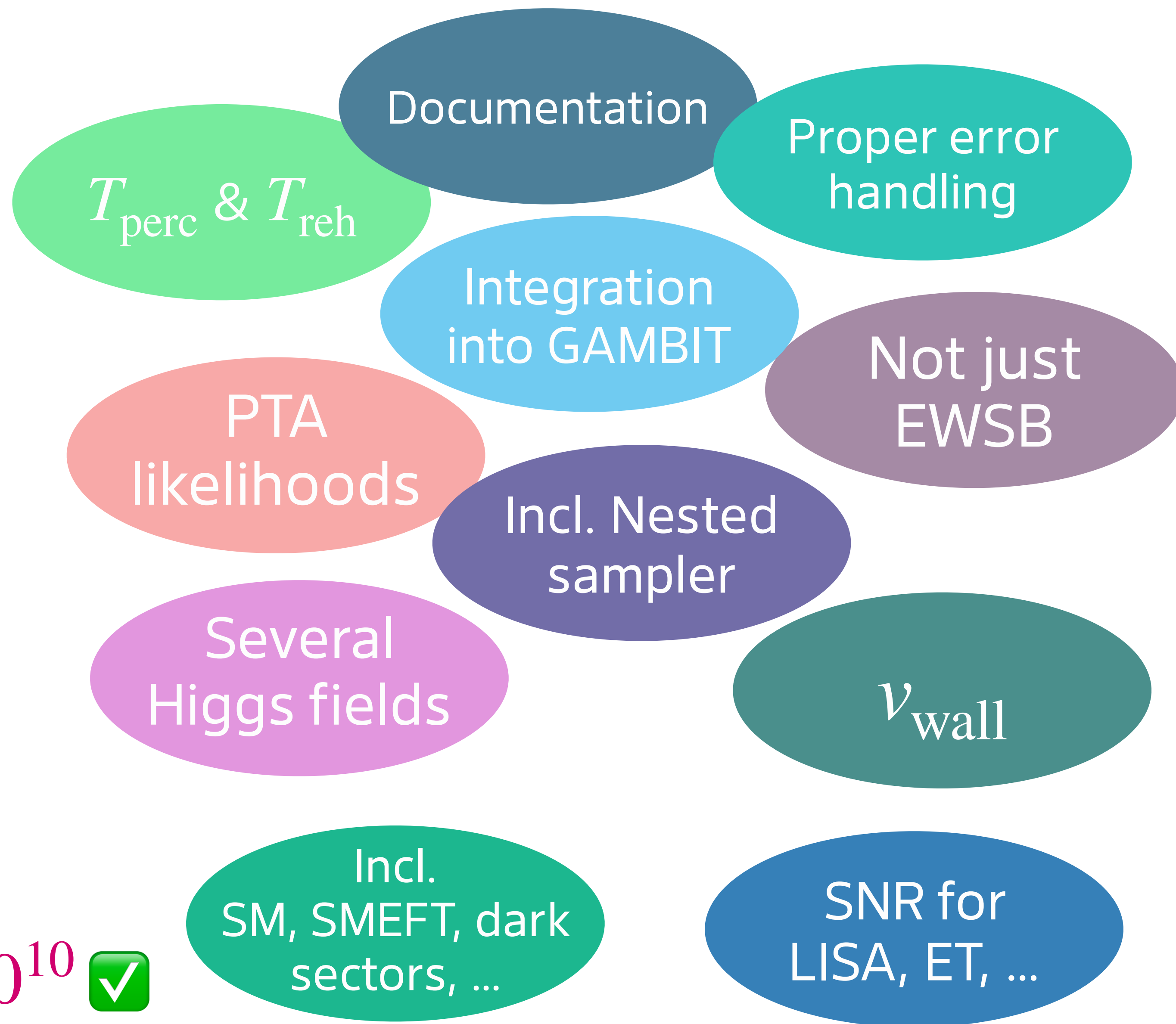
Extreme supercooling with $\alpha = 10^{10}$ ✓



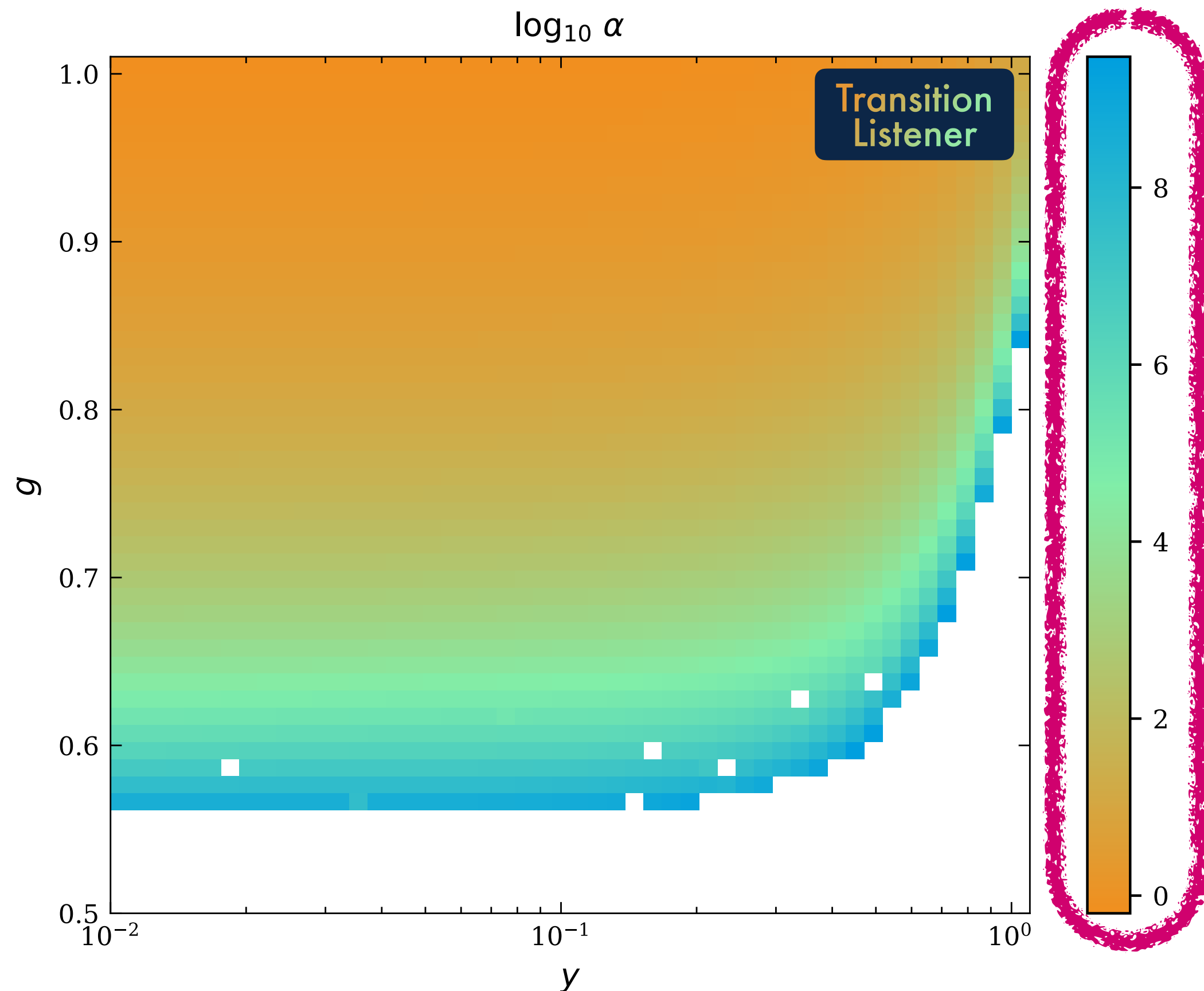
If you're not convinced yet...



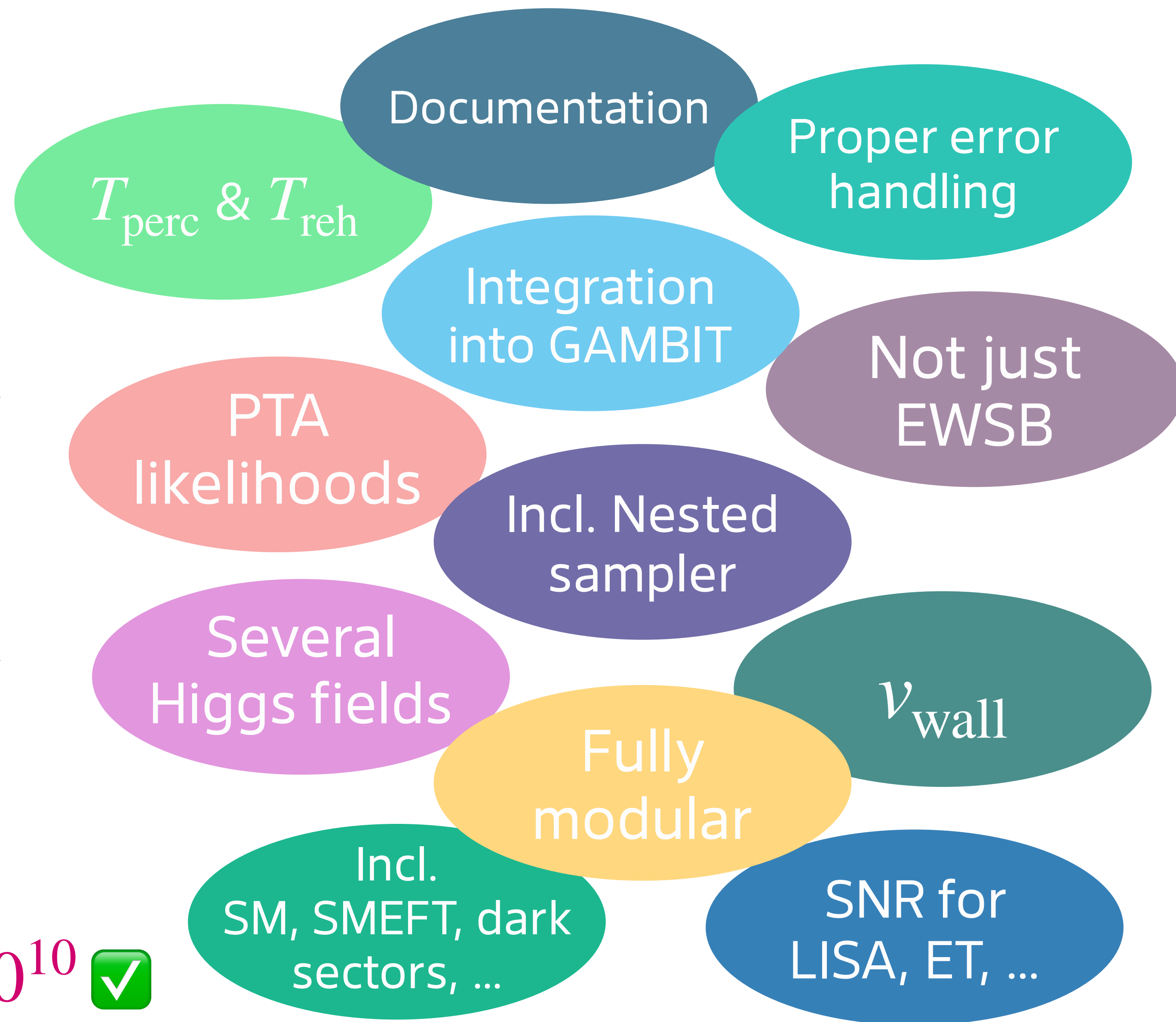
Extreme supercooling with $\alpha = 10^{10}$



If you're not convinced yet...



Extreme supercooling with $\alpha = 10^{10}$



Summary



- PTAs could have observed a dark sector phase transition on top of the black hole background
 - ➔ Dark sector phase transition can explain the PTA signal **better than only SMBHBs**
 - ➔ Performed global fit with PTA, BBN, CMB, bullet cluster, and beam dump likelihoods
 - ➔ Best-fit scenarios **can be tested by upcoming beam-dump & collider experiments**
 - ➔ **Soon: TransitionListener v2**

**Transition
Listener**



**Thank you very much
for your attention!**
Do you have any questions?

