

The Nano-Hertz Gravitational Wave Background: Connection to sub-GeV dark matter

Seminar at Stockholm university, November 13th 2025

Carlo Tasillo,
Uppsala University

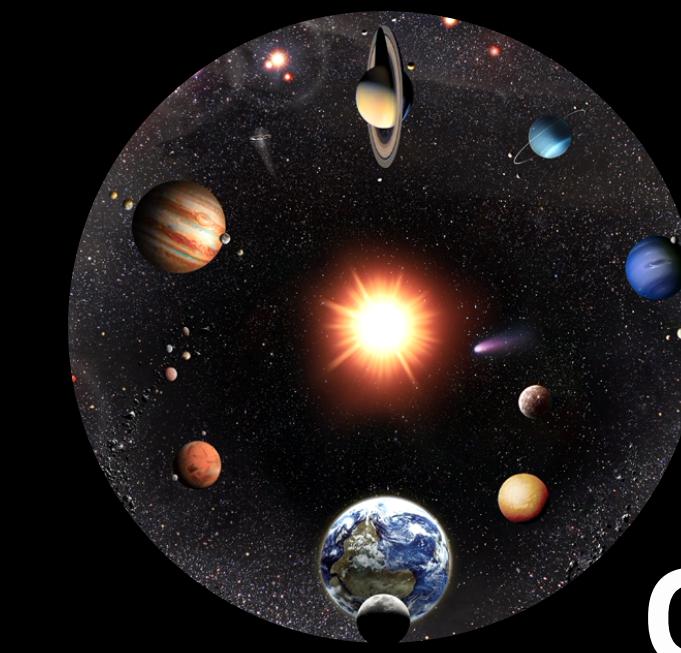
Based on work with Sowmiya Balan, Torsten Bringmann,
Frederik Depta, Felix Kahlhöfer, Thomas Konstandin, Jonas Matuszak,
Kai Schmidt-Hoberg, Pedro Schwaller

JCAP 11 (2023) 053,
JCAP 08 (2025) 062,
and **Phys.Rev.Res. 7 (2025)**



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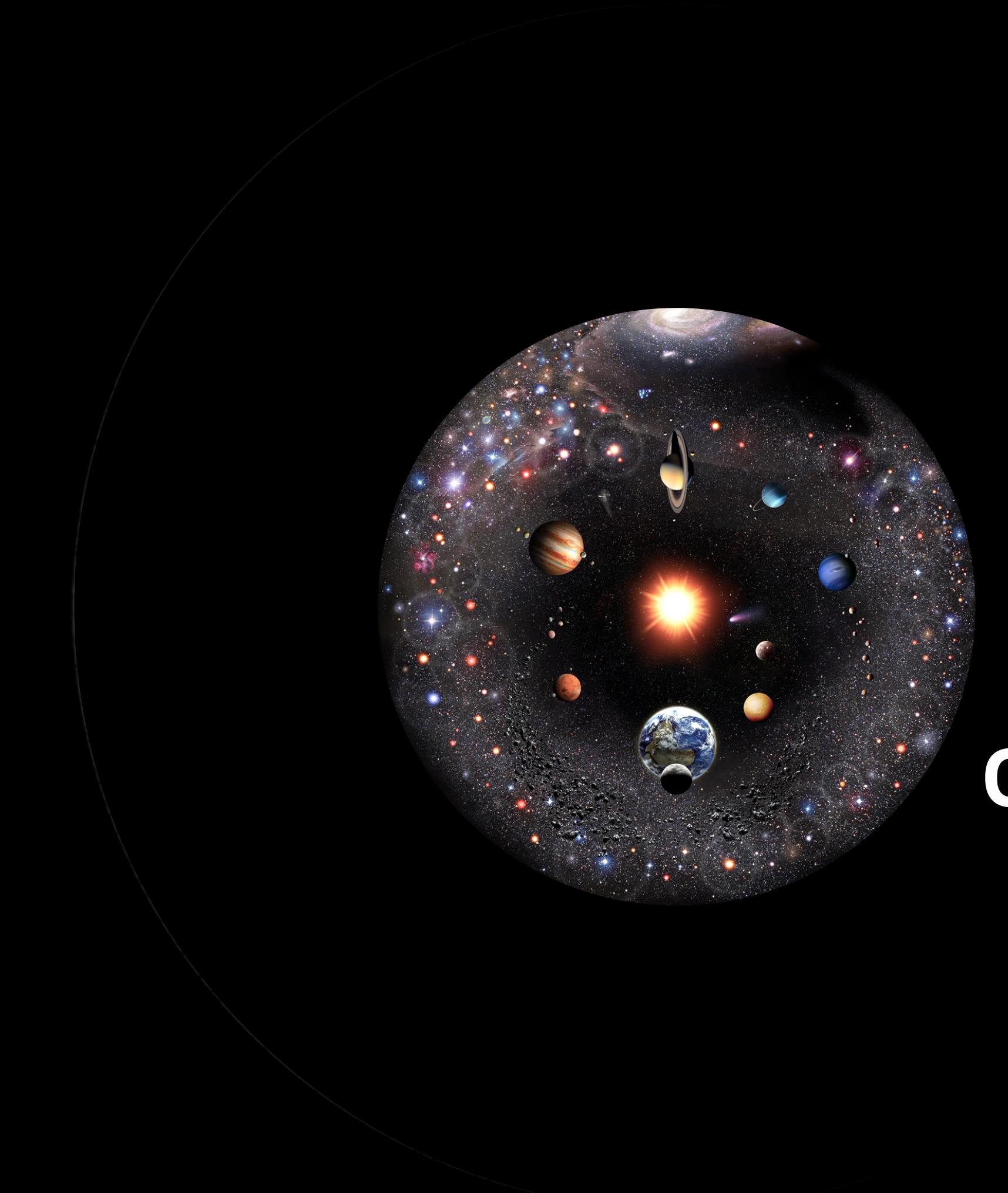
It's the end of the world as we know it (and I feel fine)



Our Solar System

PABLO
CARLOS
BUDASSI

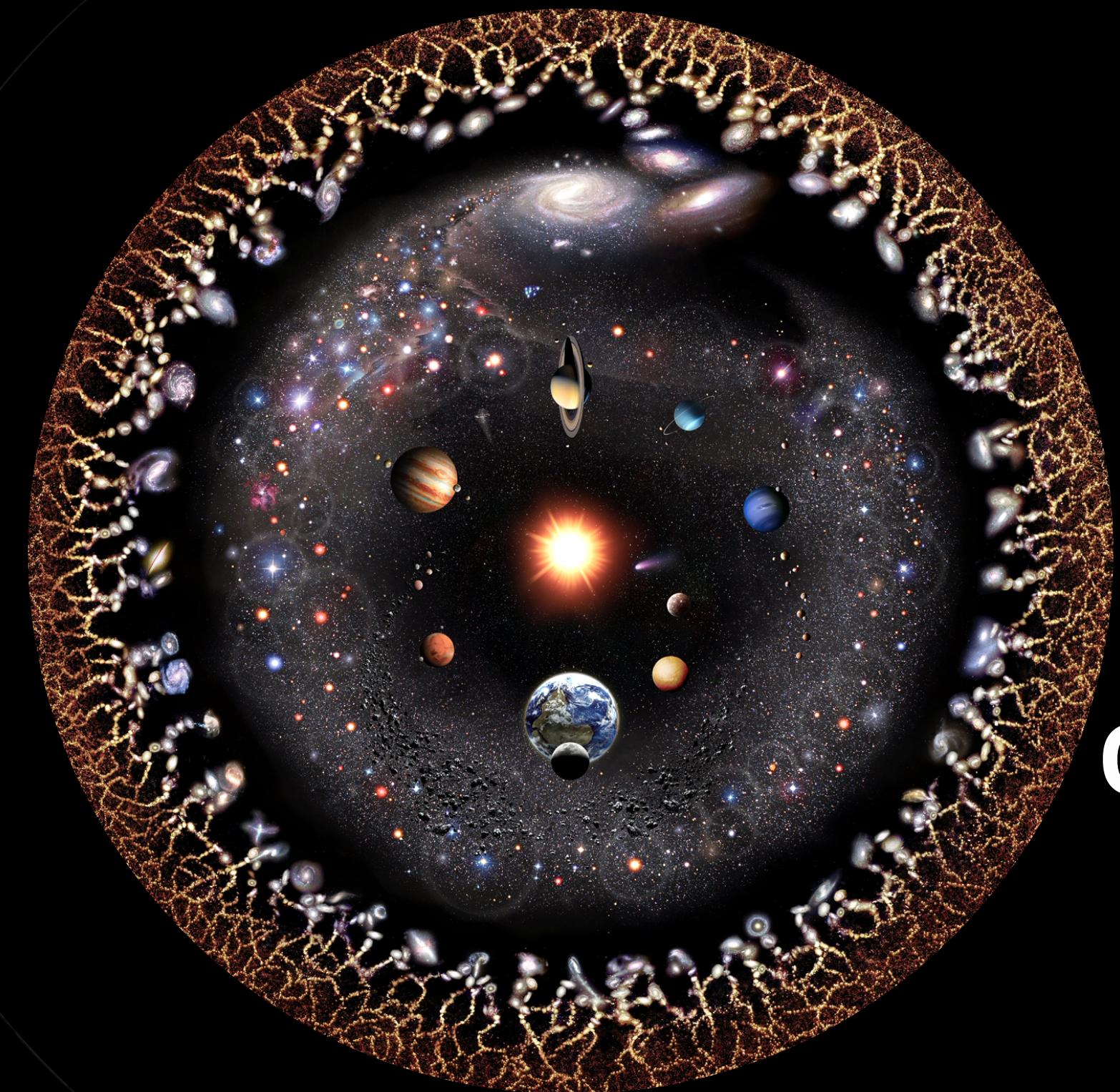
It's the end of the world as we know it (and I feel fine)



Our galaxy

PABLO
CARLOS
BUDASSI

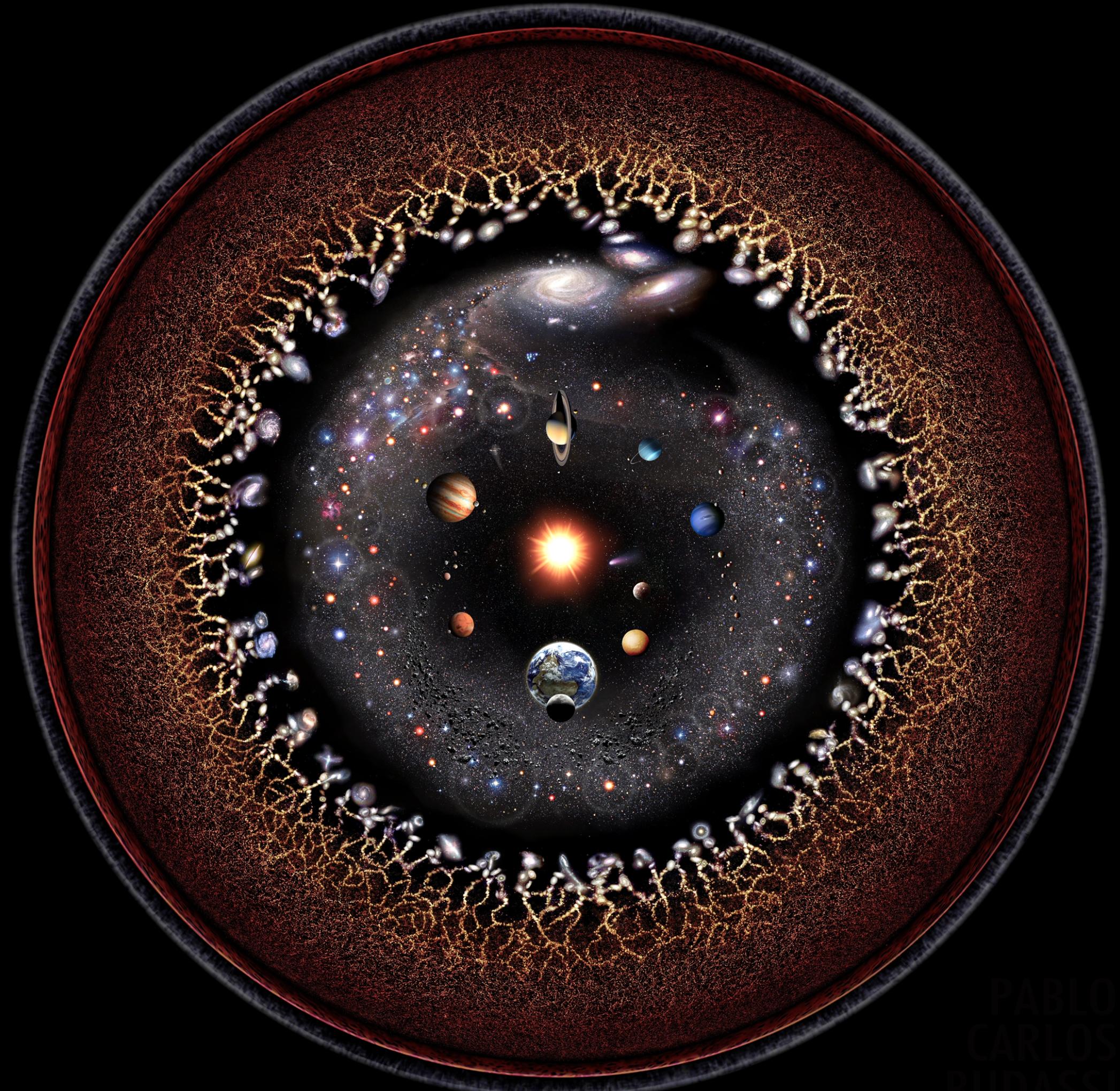
It's the end of the world as we know it (and I feel fine)



Other galaxies

PABLO
CARLOS
BUDASSI

It's the end of the world as we know it (and I feel fine)



The CMB...
and the CGWB?

PABLO
CARLOS
BUDASSI

At Last, There's -

A globe-span-

Astronomers detect 'cosmic bass note' of gravitational waves

Sound comes from the merging of supermassive black holes across the universe, according to scientists

Scientists 'hear' cosmic hum from gravitational waves

Gravitational waves that ripple through the universe

Scientists have observed for the first time the faint ripples caused by the motion of holes that are gently stretching and squeezing everything in the universe

Black Holes in Space

Gravitational waves at the center of the Milky Way

Scientists record 'cosmic hum' from black holes

It may be a massive black hole

of Low-Frequency Gravitational Waves

the waves, w-

Scientists 'hear' cosmic hum from gravitational waves

Sound comes from the merging of supermassive black holes across the universe, according to scientists

A Background 'Hum' Pervades the Universe. Scientists Are Racing to Find Its Source

Astronomers are now seeking to pinpoint the origins of an exciting new form of gravitational waves that was announced earlier this year

Astro-

SCIENCE

Colossal gravitational waves—trillions of miles long—found for the first time

Radio telescopes around the world picked up a telltale hum reverberating across the cosmos, most likely from supermassive black holes merging in the early universe.

In a major discovery, scientists say space-time churns like a choppy sea

The mind-bending finding suggests that everything around us is constantly being rolled by low-frequency gravitational waves

First Evidence of Giant Gravitational Waves Thrills Astronomers

For first time ever, scientists "hear" gravitational waves rippling through the universe

Monster gravitational waves spotted for first time

Physics

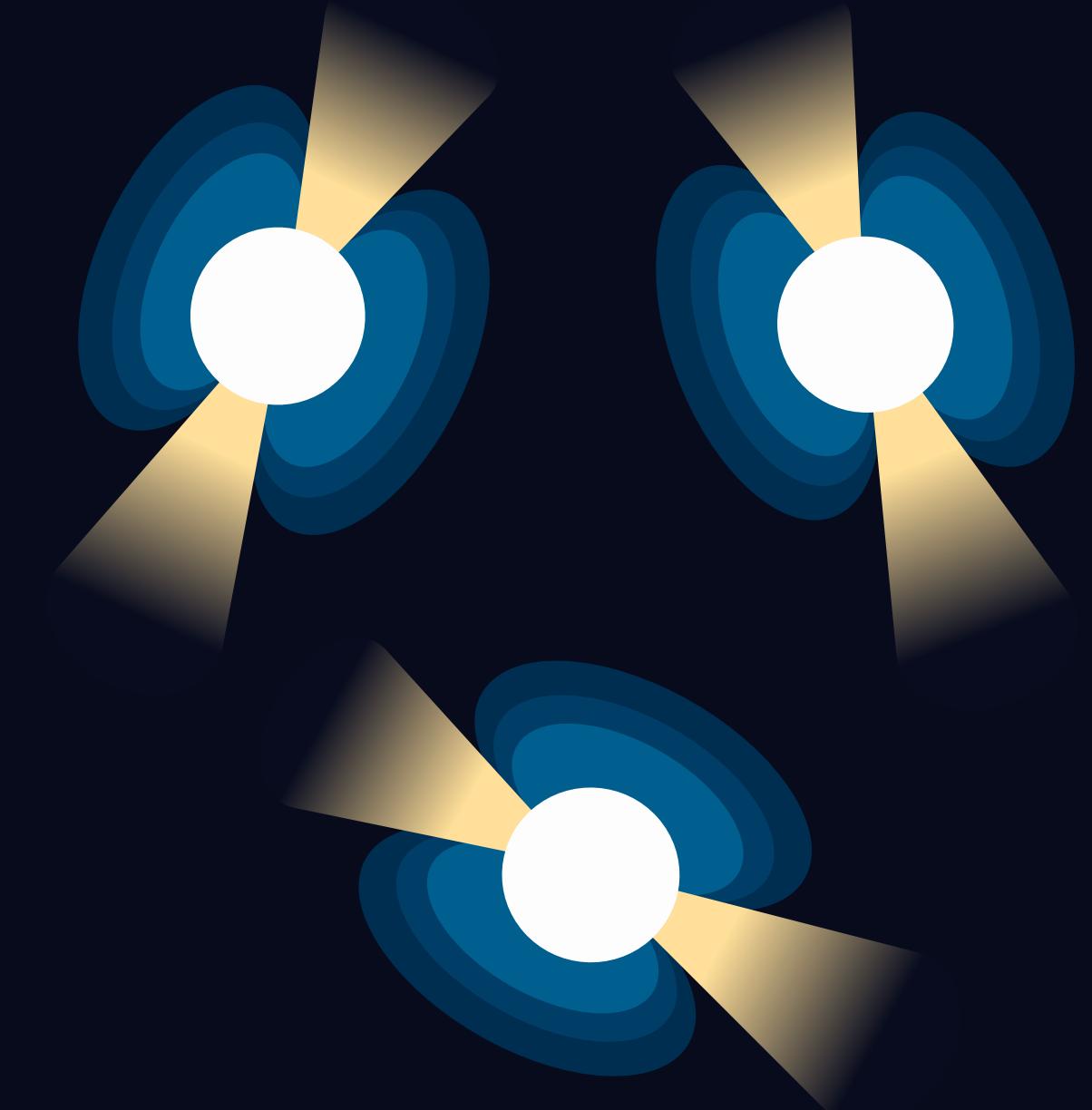
Gravitational waves produce a background hum across the whole universe

After decades of searching, astronomers have found a distinctive pattern of light, from spinning stars called pulsars, that suggests huge gravitational waves are creating gentle ripples in space-time across the universe

We live in the age of gravitational wave cosmology!

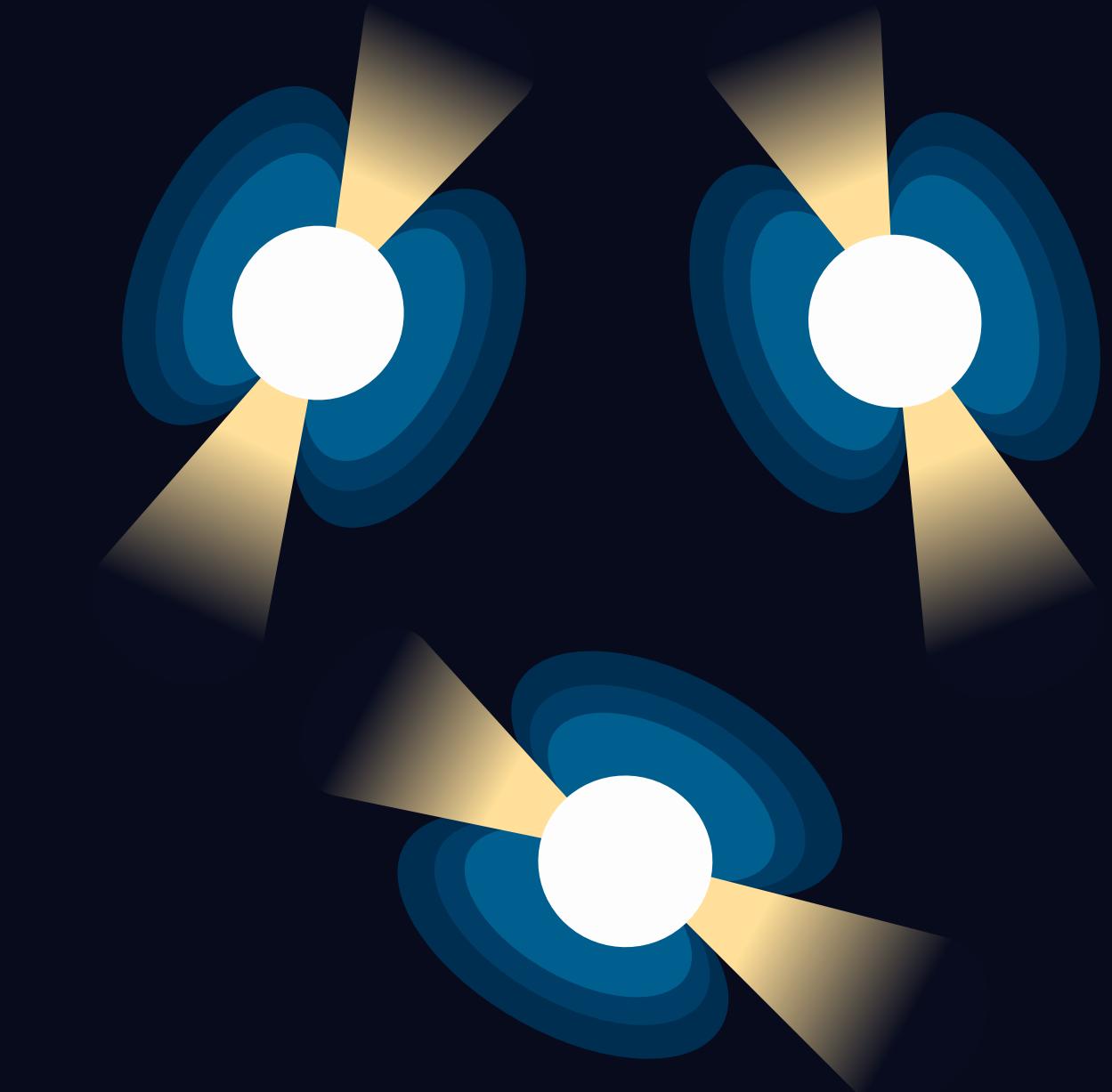
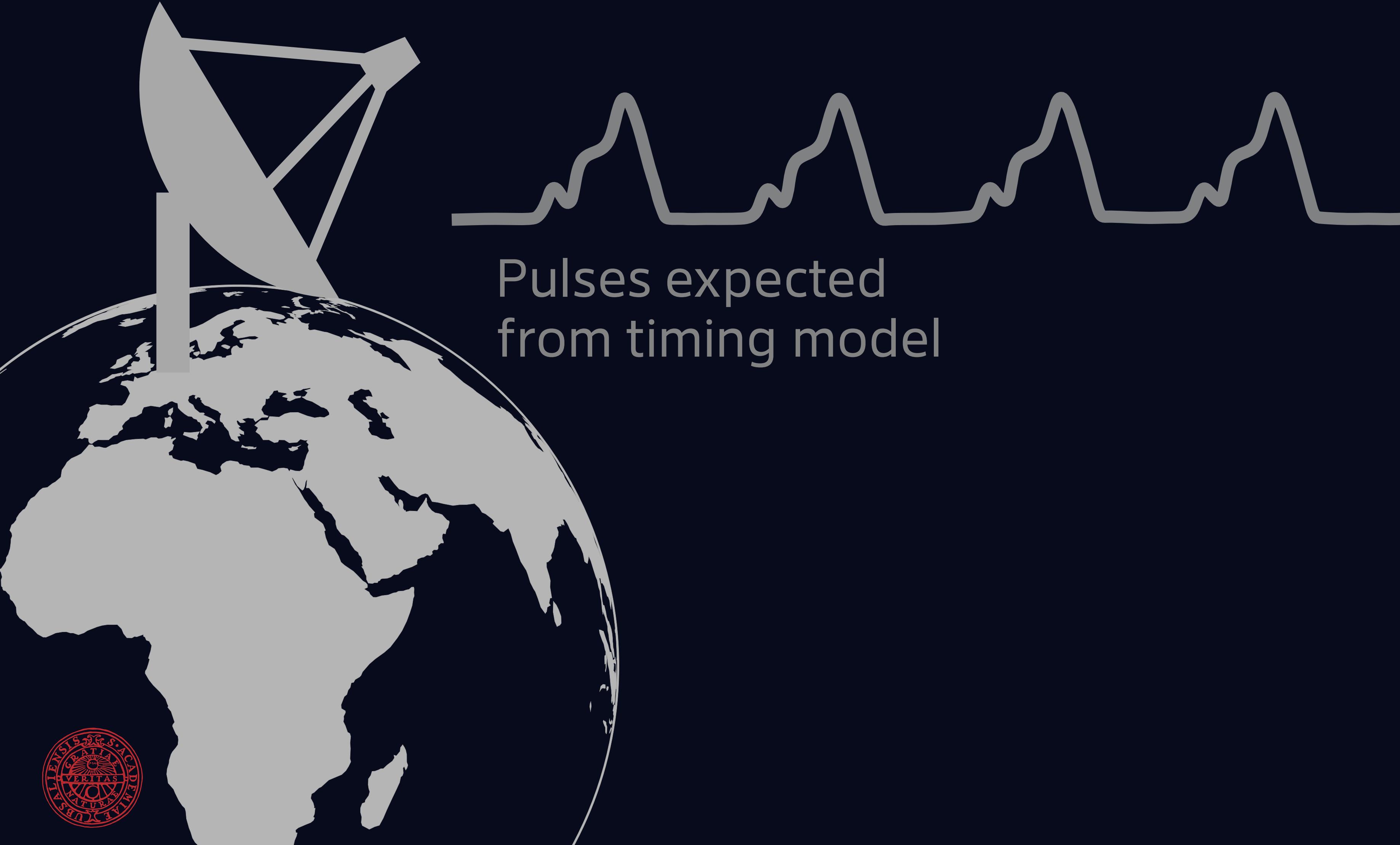
The working principle of a pulsar timing array

Galactic millisecond pulsars



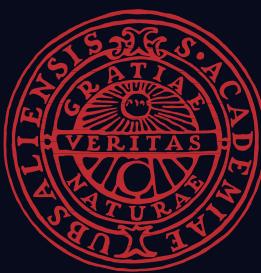
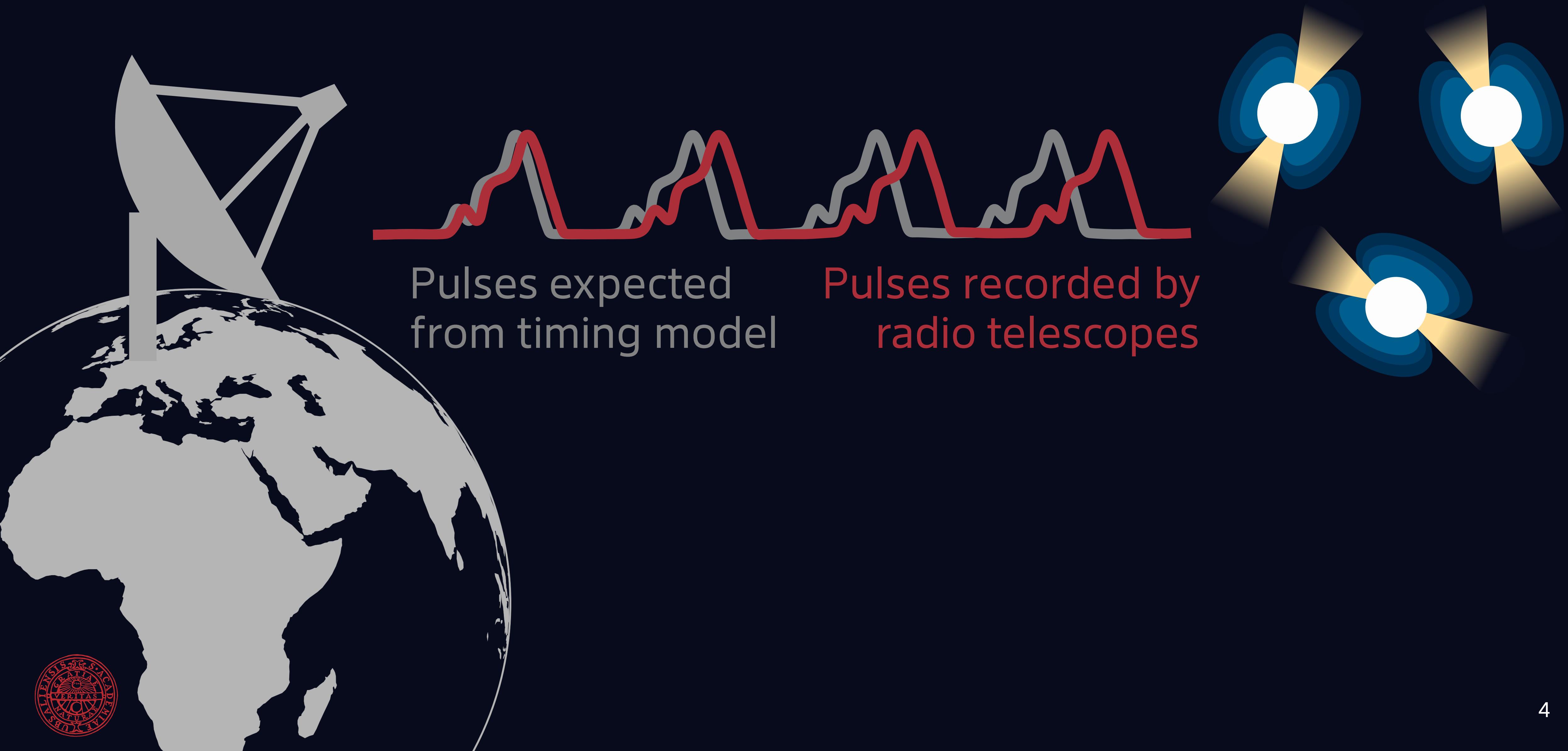
The working principle of a pulsar timing array

Galactic millisecond pulsars



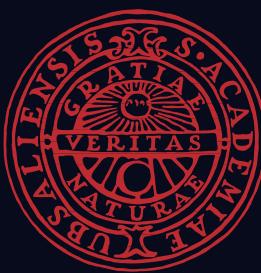
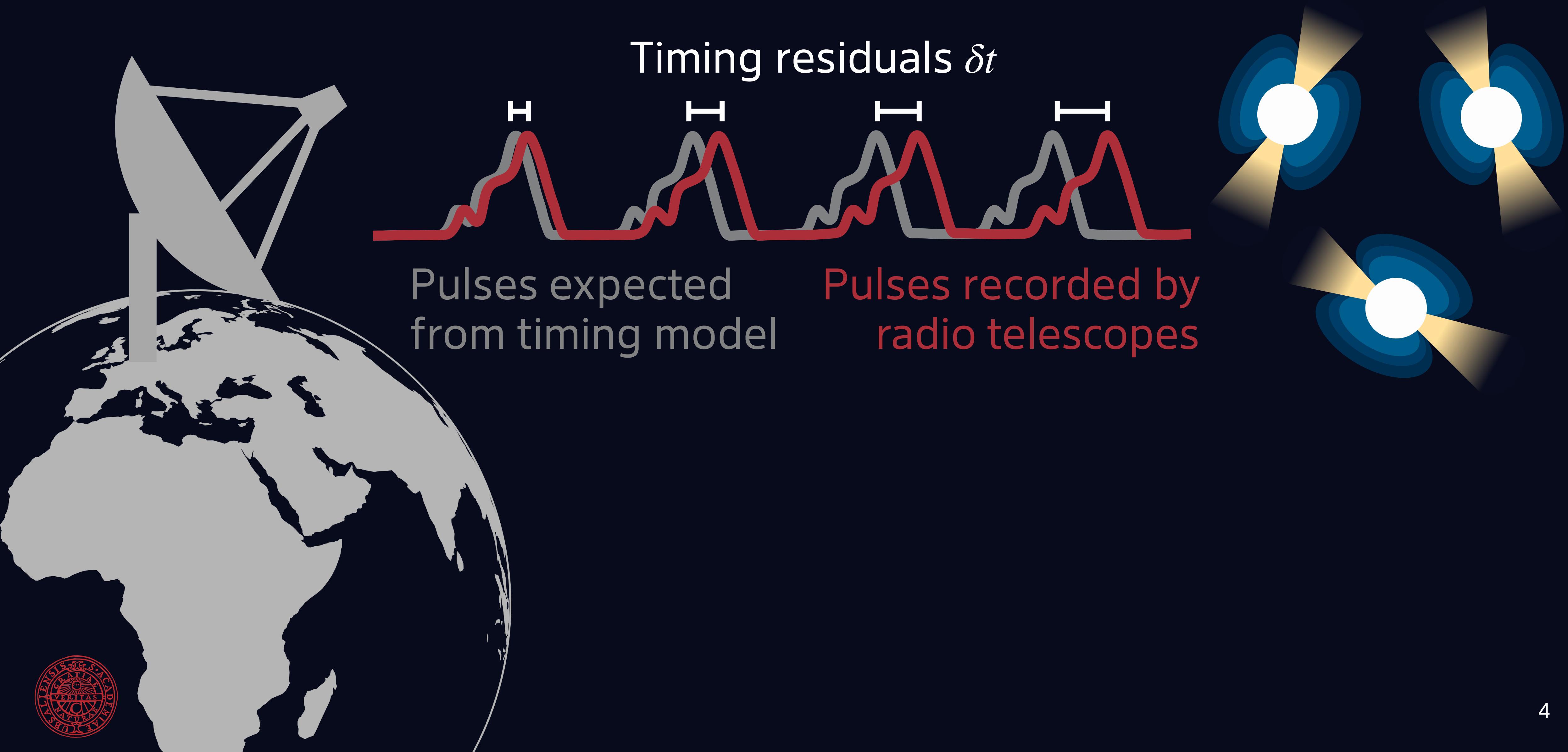
The working principle of a pulsar timing array

Galactic millisecond pulsars



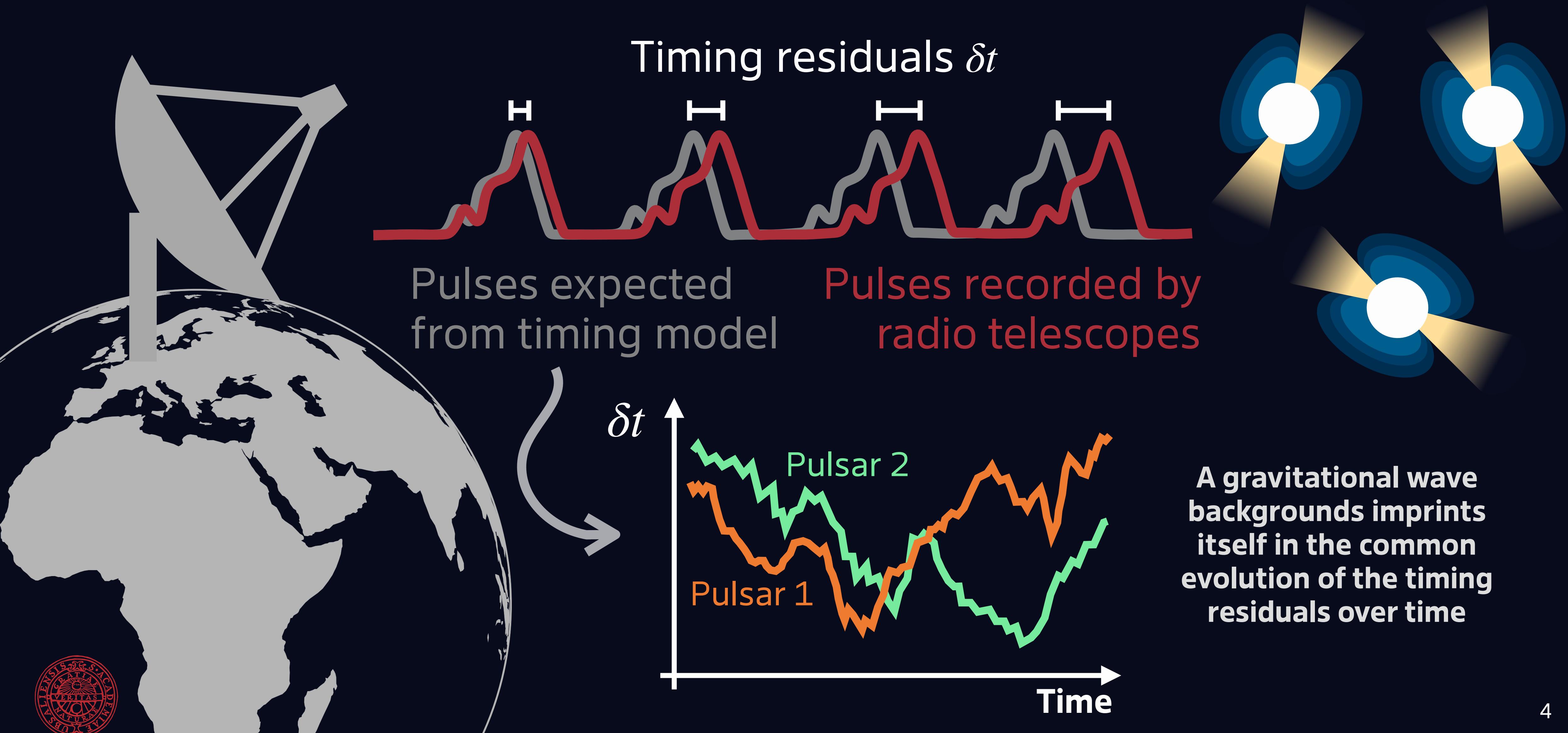
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Galactic millisecond pulsars

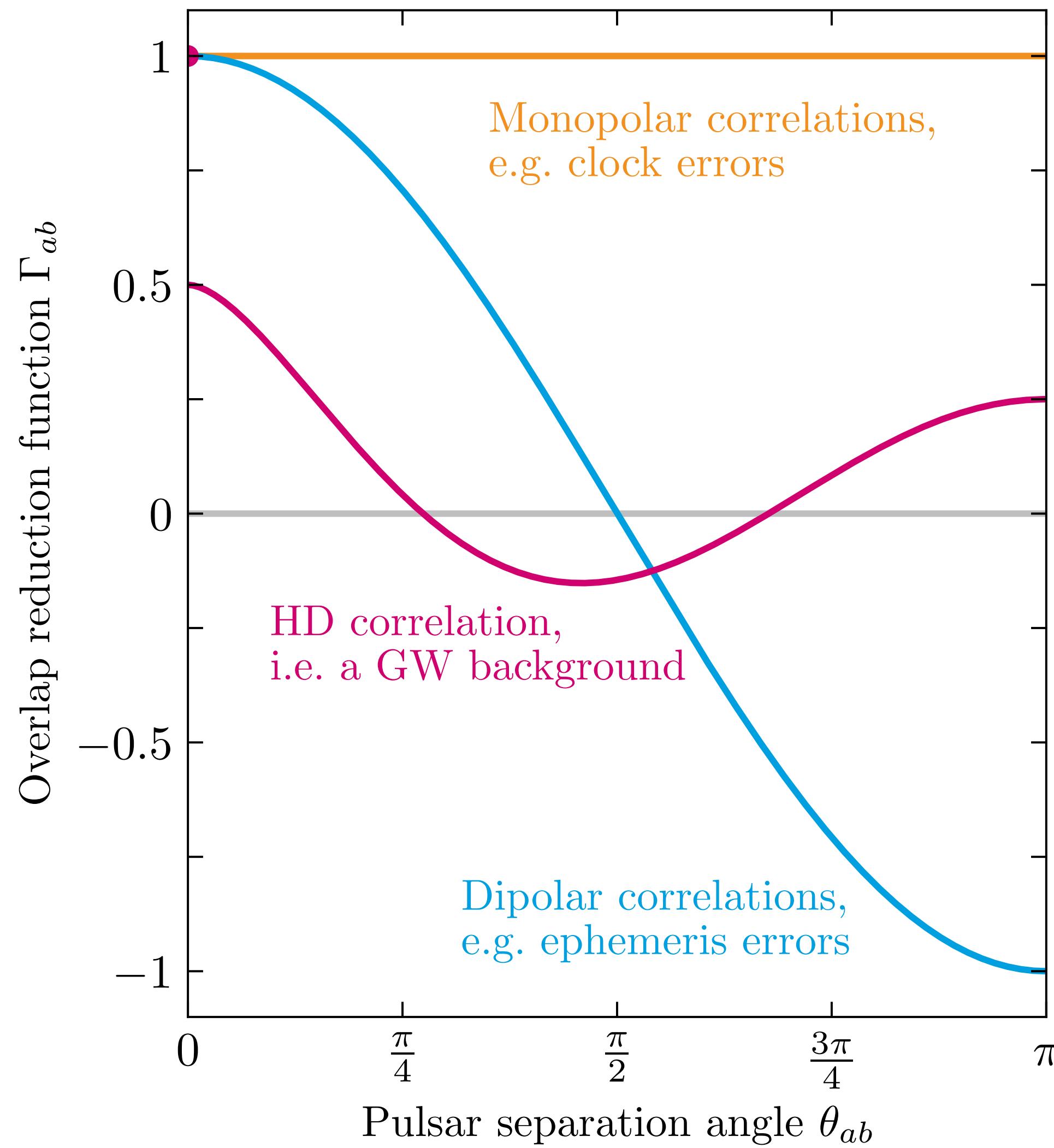


The working principle of a pulsar timing array

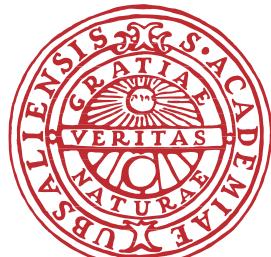
Galactic millisecond pulsars



Searching for the Hellings-Downs correlation

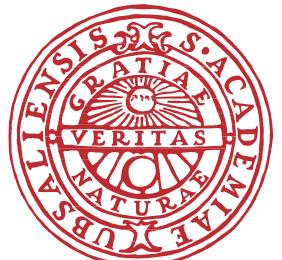
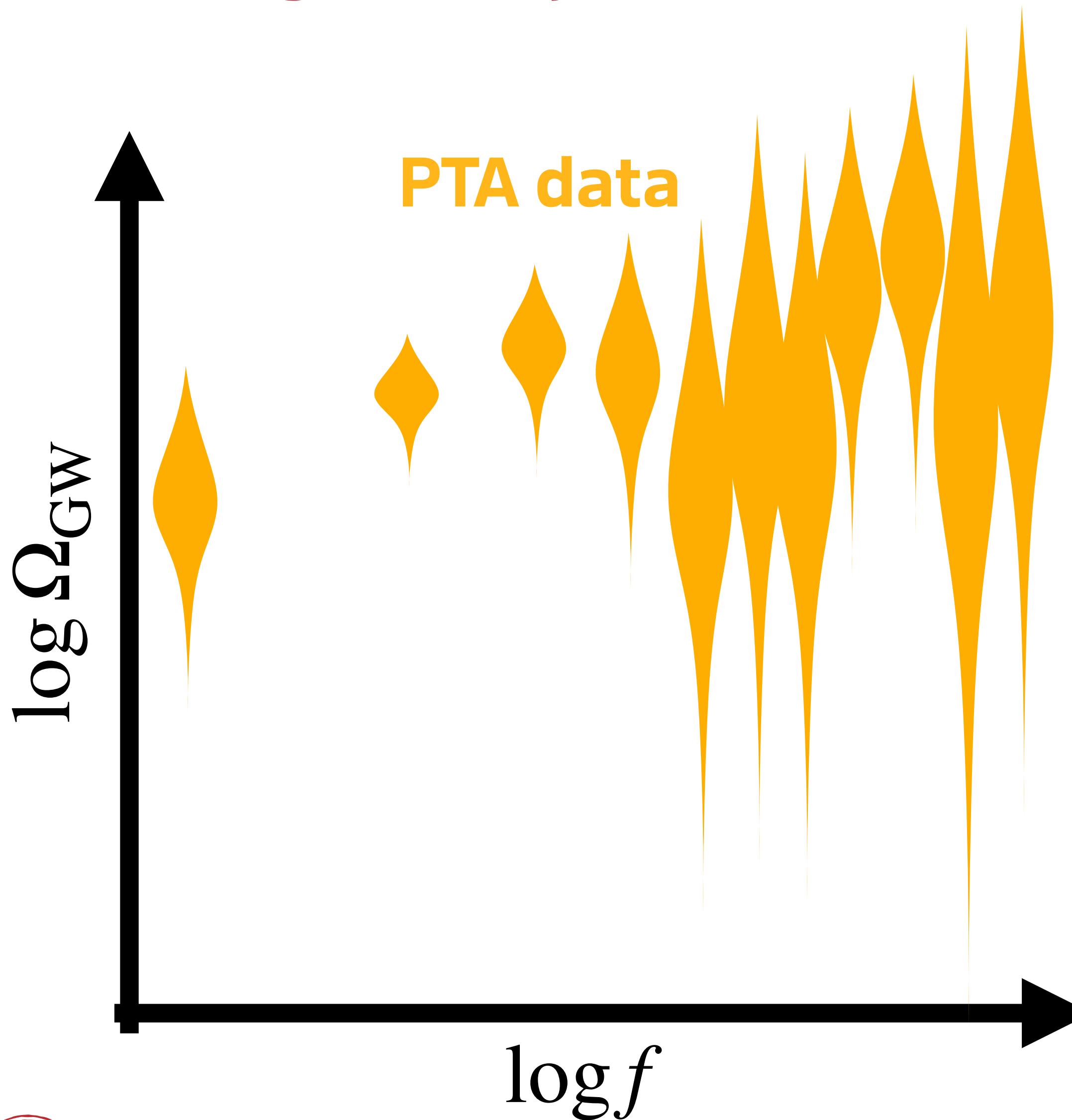


- PTAs found an underlying „common red process“ among $\mathcal{O}(70)$ pulsars
- Signal could have many sources:
 - ▶ Pulsars themselves, **Clock errors, Ephemeris errors:**
All ruled out with $>5\sigma$ significance
 - ▶ **Gravitational wave background:**
 $3 - 4\sigma$ evidence [NANOGrav, 2023]

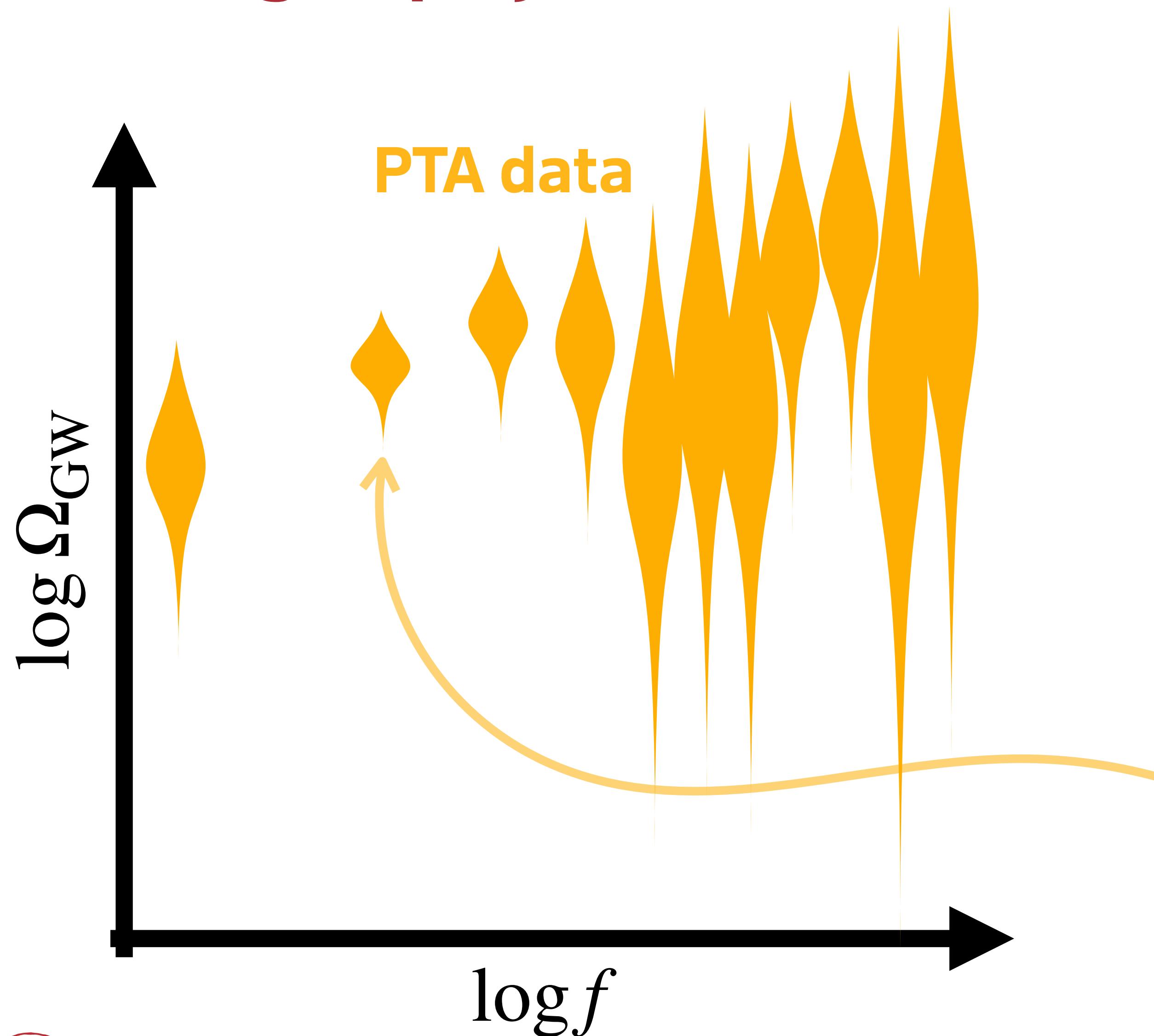


What is the source?

Learning to play the violin



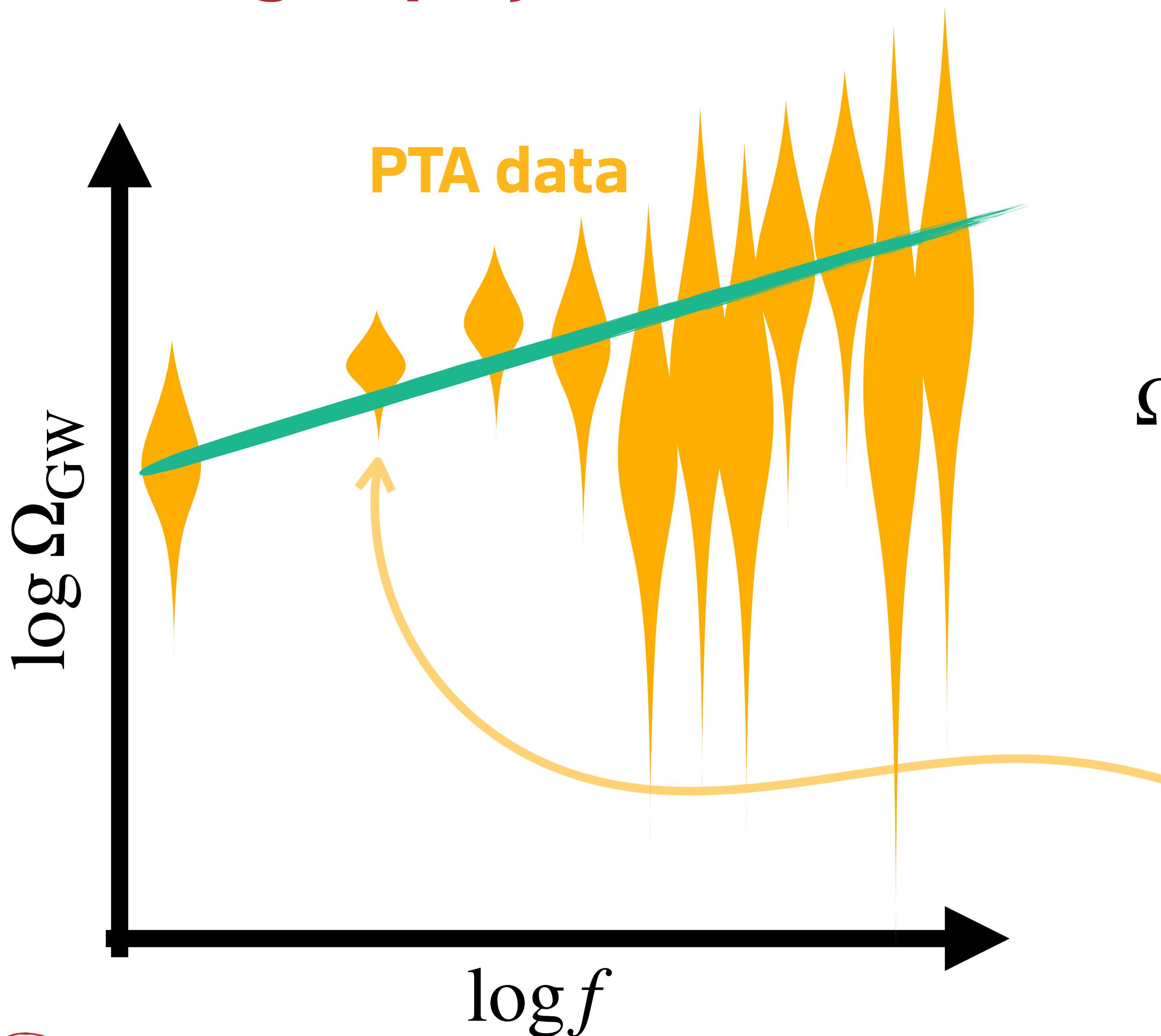
Learning to play the violin



Each „violin” in the Bayesian spectrogram can be understood as a data point with non-Gaussian error bar, describing the Fourier amplitude of a given frequency.



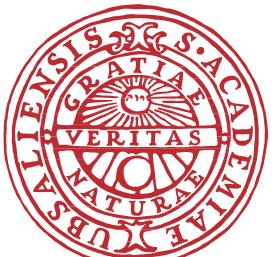
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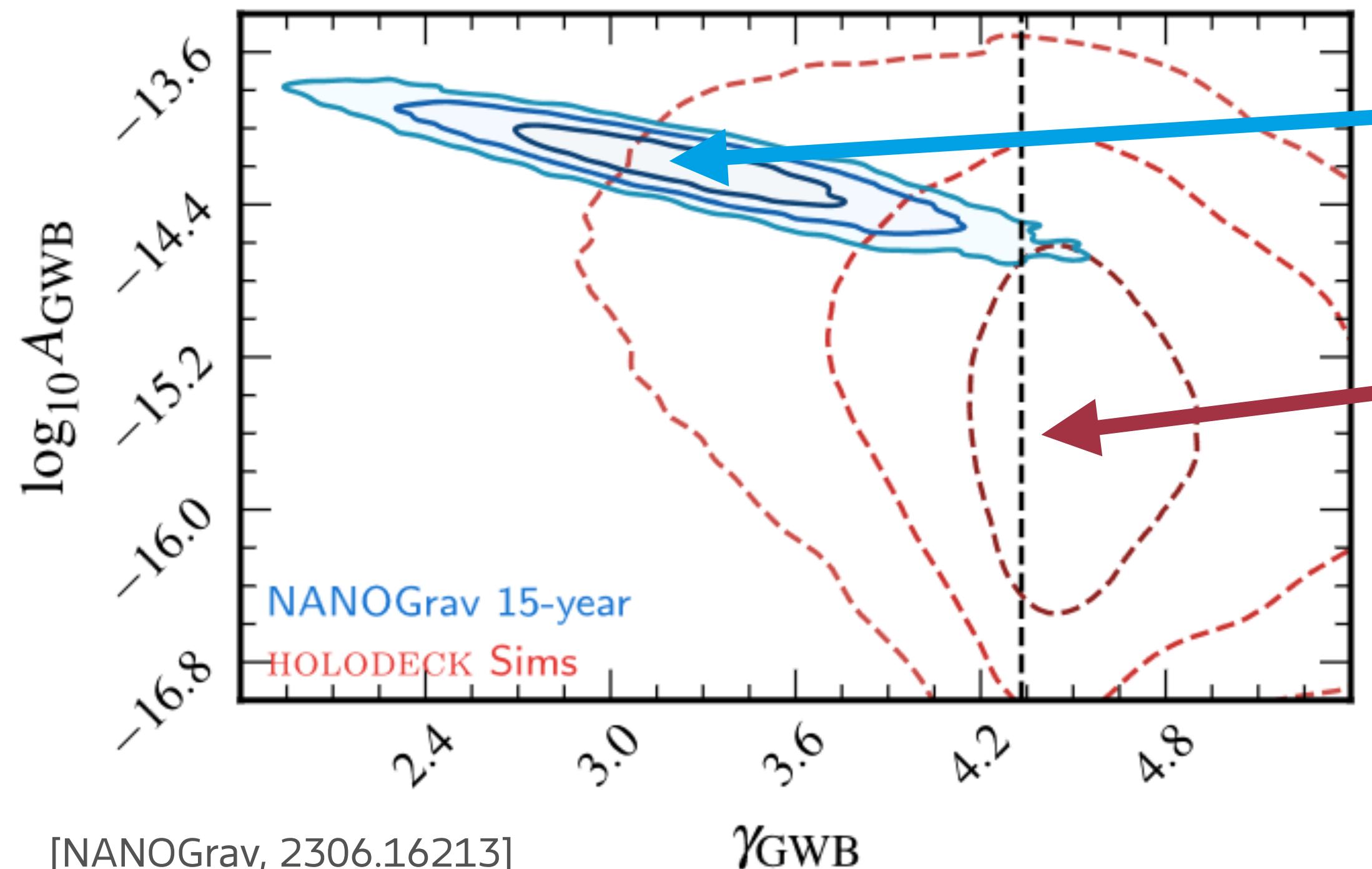
The inferred spectral shape of the GWB is well described by a power law

$$\Omega_{\text{GW}}(f) = \frac{2\pi^2}{3H_0^2} A^2 \left(\frac{f}{1 \text{ yr}^{-1}} \right)^{5-\gamma} \text{ yr}^{-2}$$

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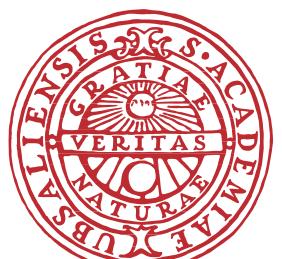


Merging supermassive black holes

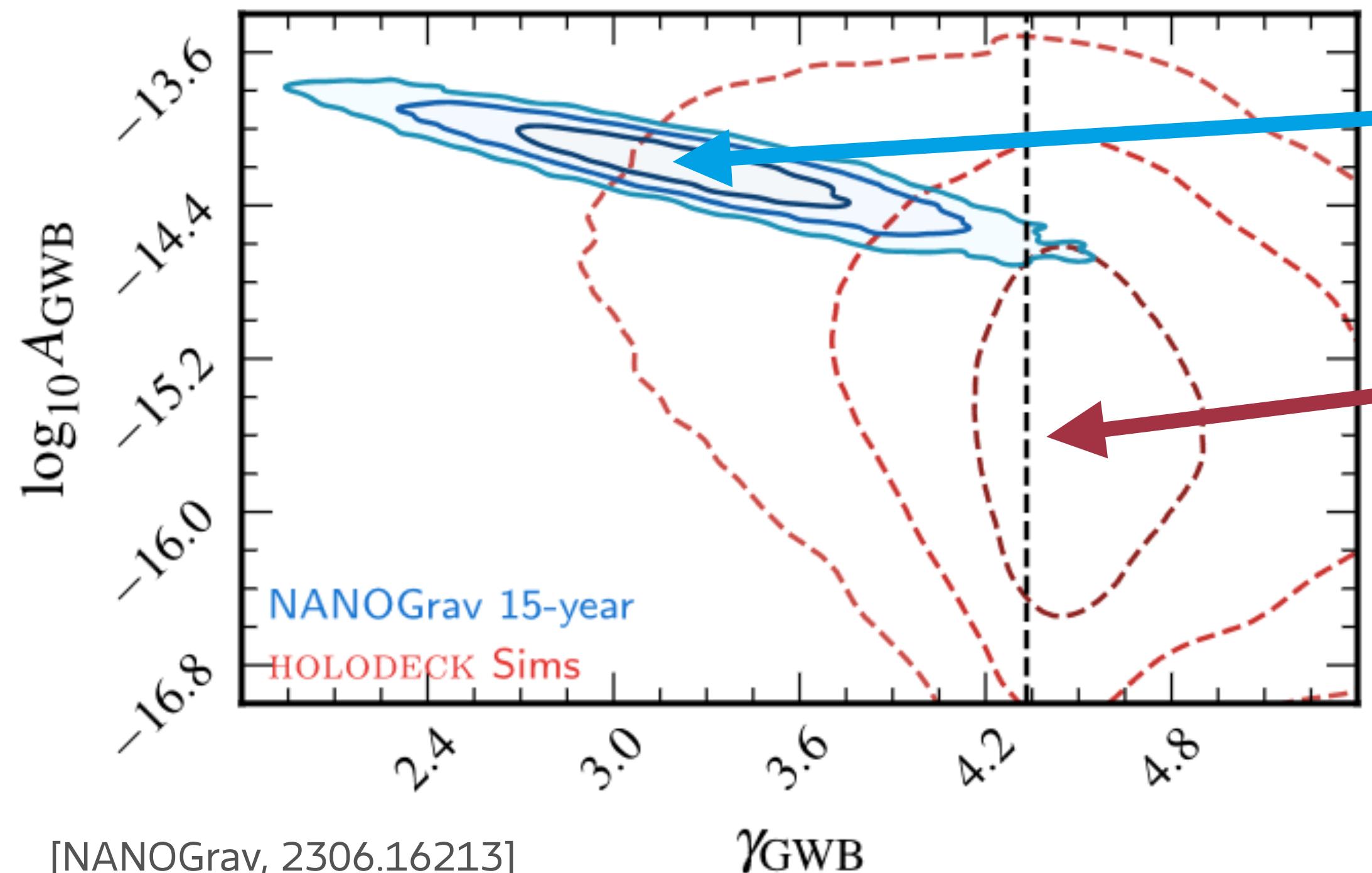


Observed signal follows a power-law spectrum with amplitude A and slope γ

Astrophysical simulations based on realistic BH populations predict much weaker signals with higher γ (more power in low frequencies)



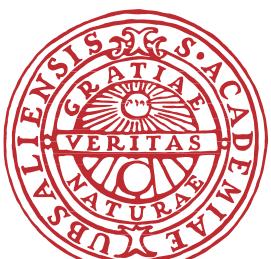
Merging supermassive black holes



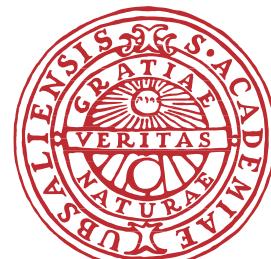
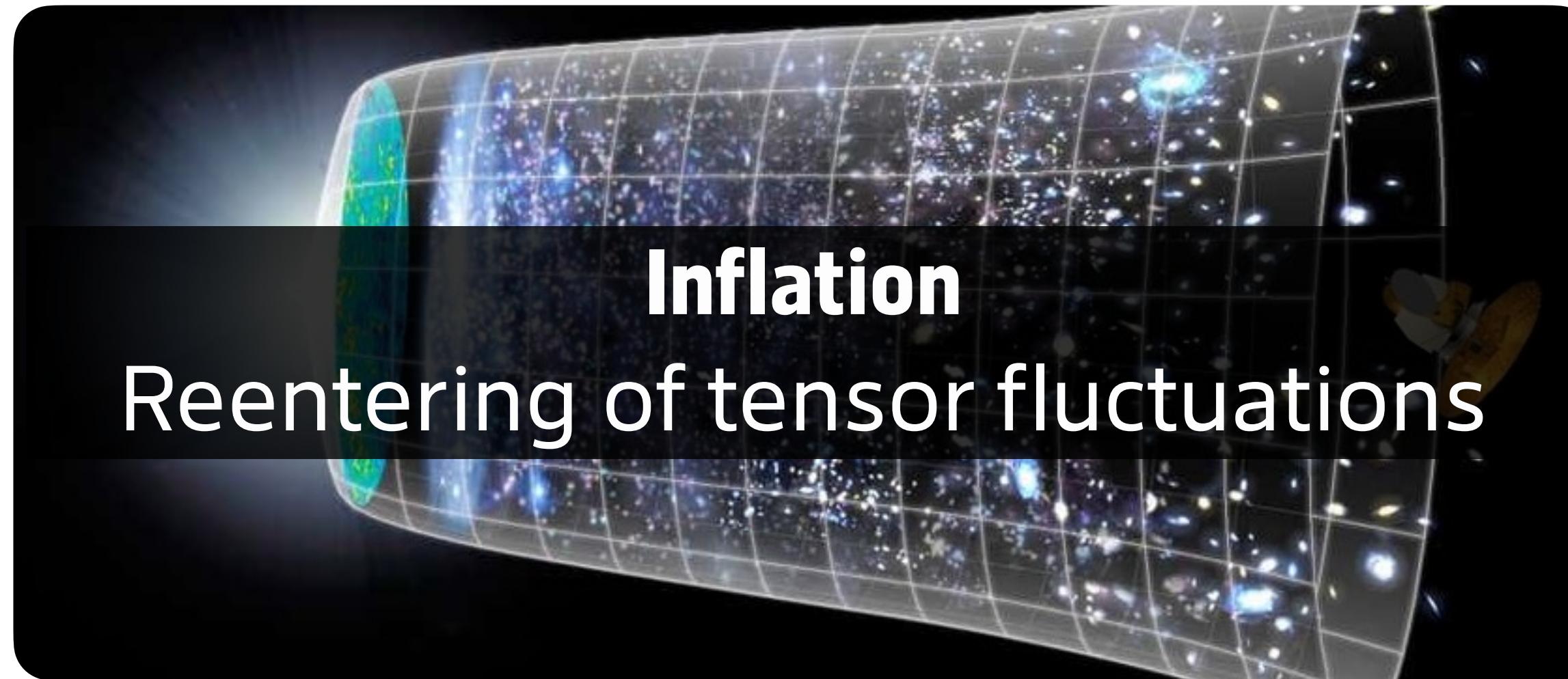
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Are there other signal sources?

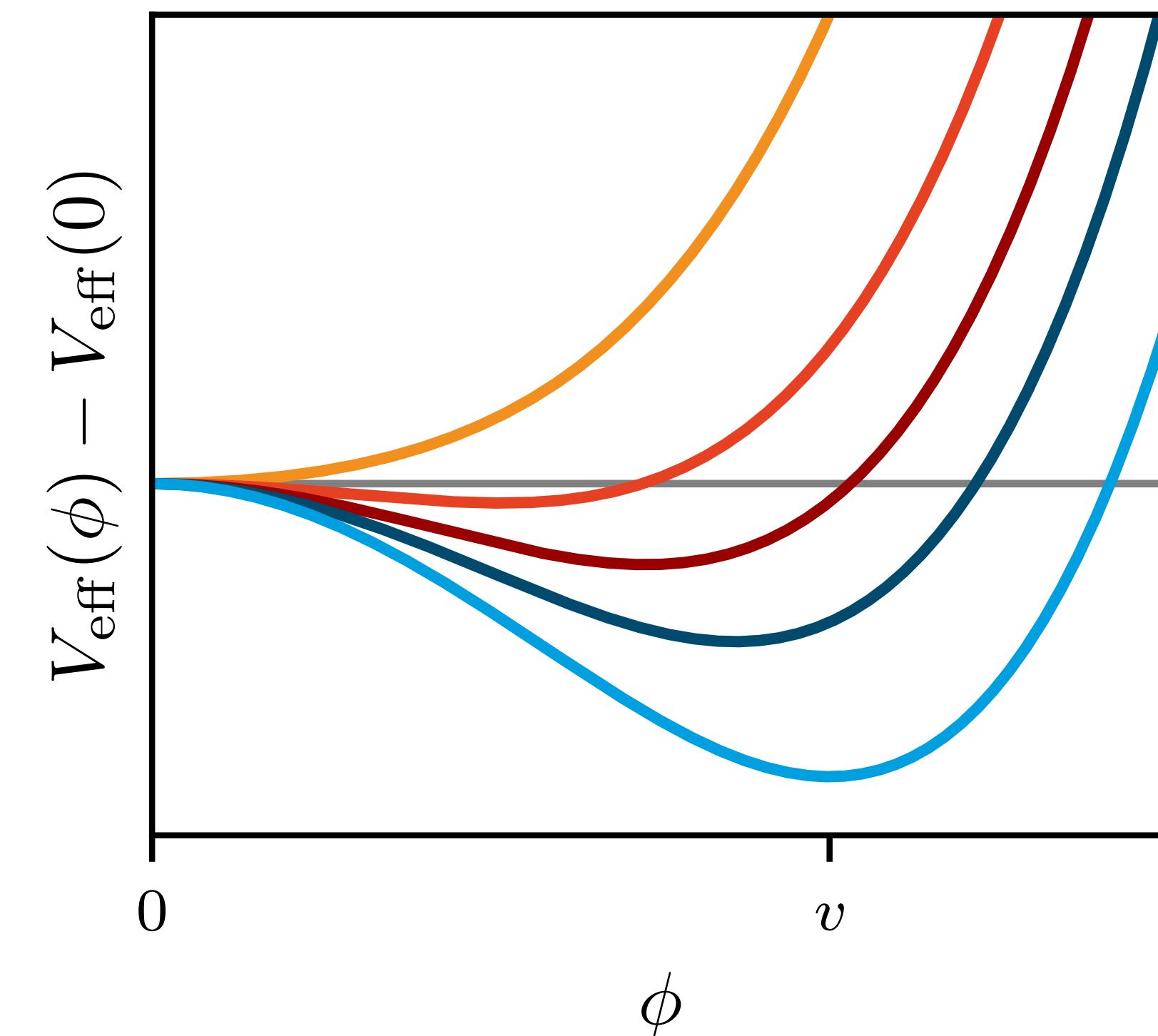


Possible cosmological sources of the PTA signal



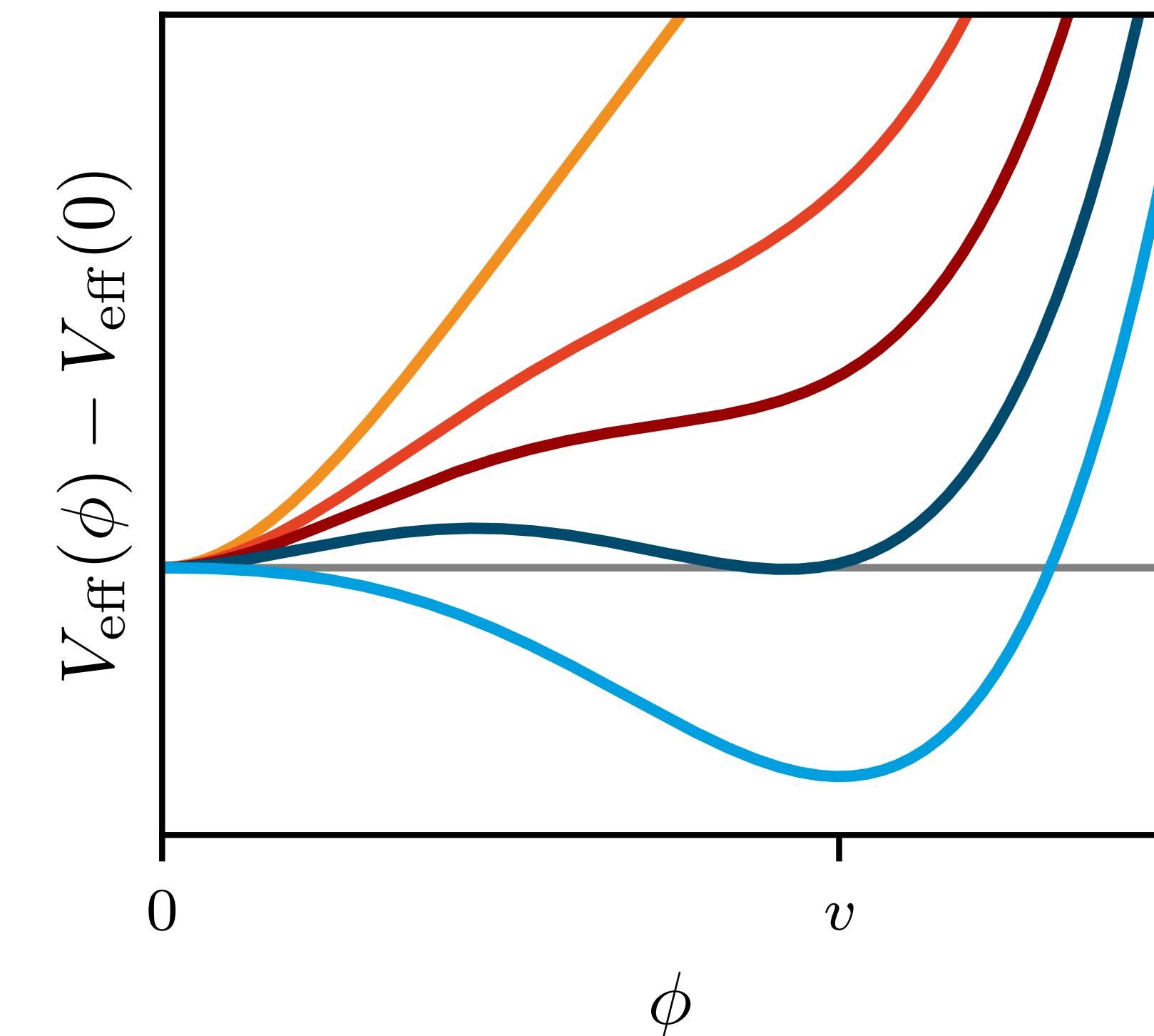
First-order phase transitions vs. cross-overs

Cross-over phase transition

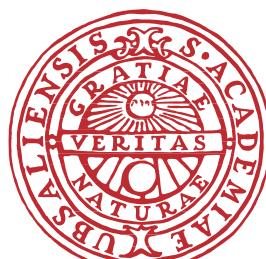


A scalar field “rolls down” from $\phi = 0$ to $\phi = v$, when the plasma cools from **high temperatures** to **low temperatures**.

First-order phase transition

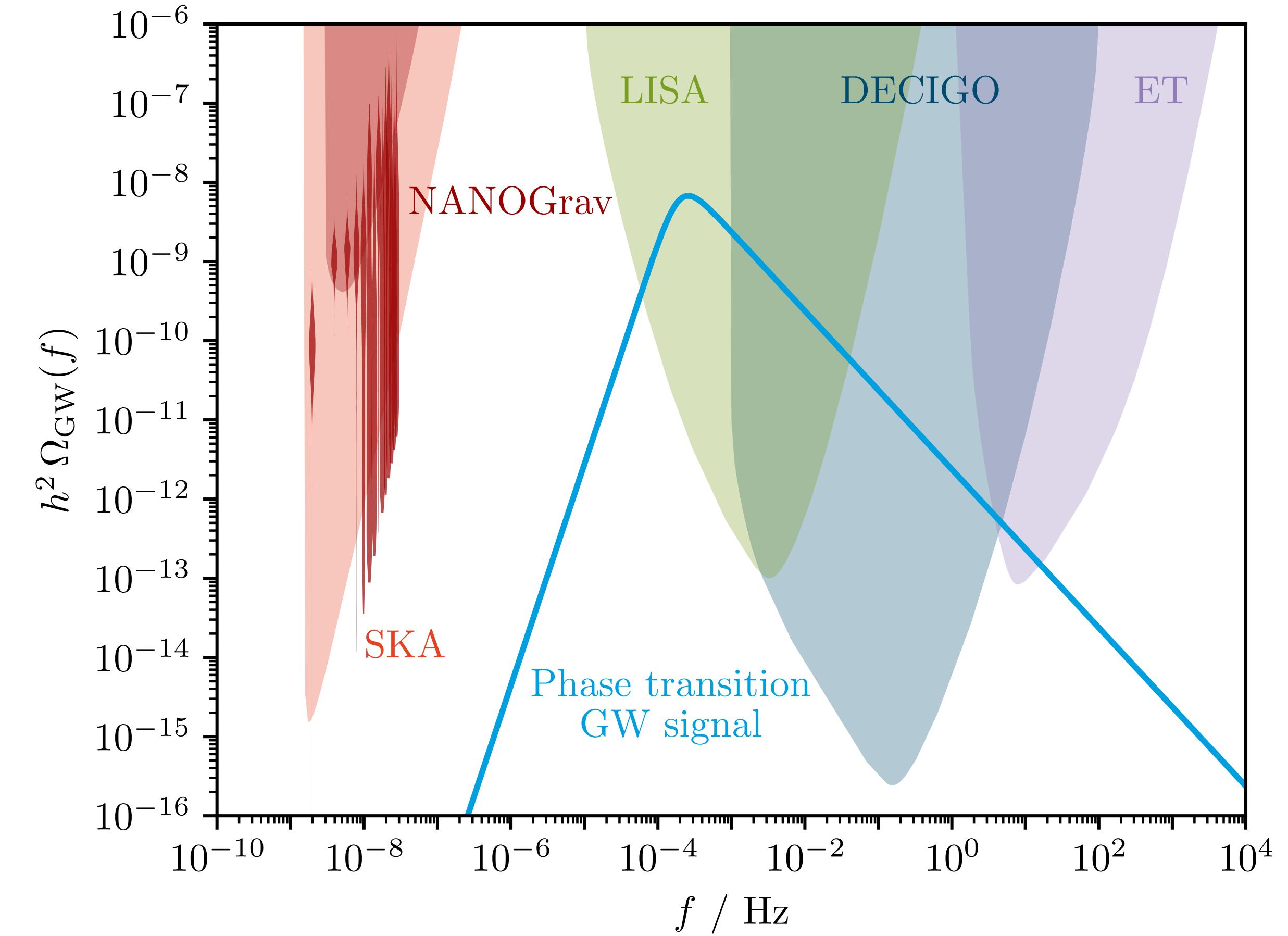
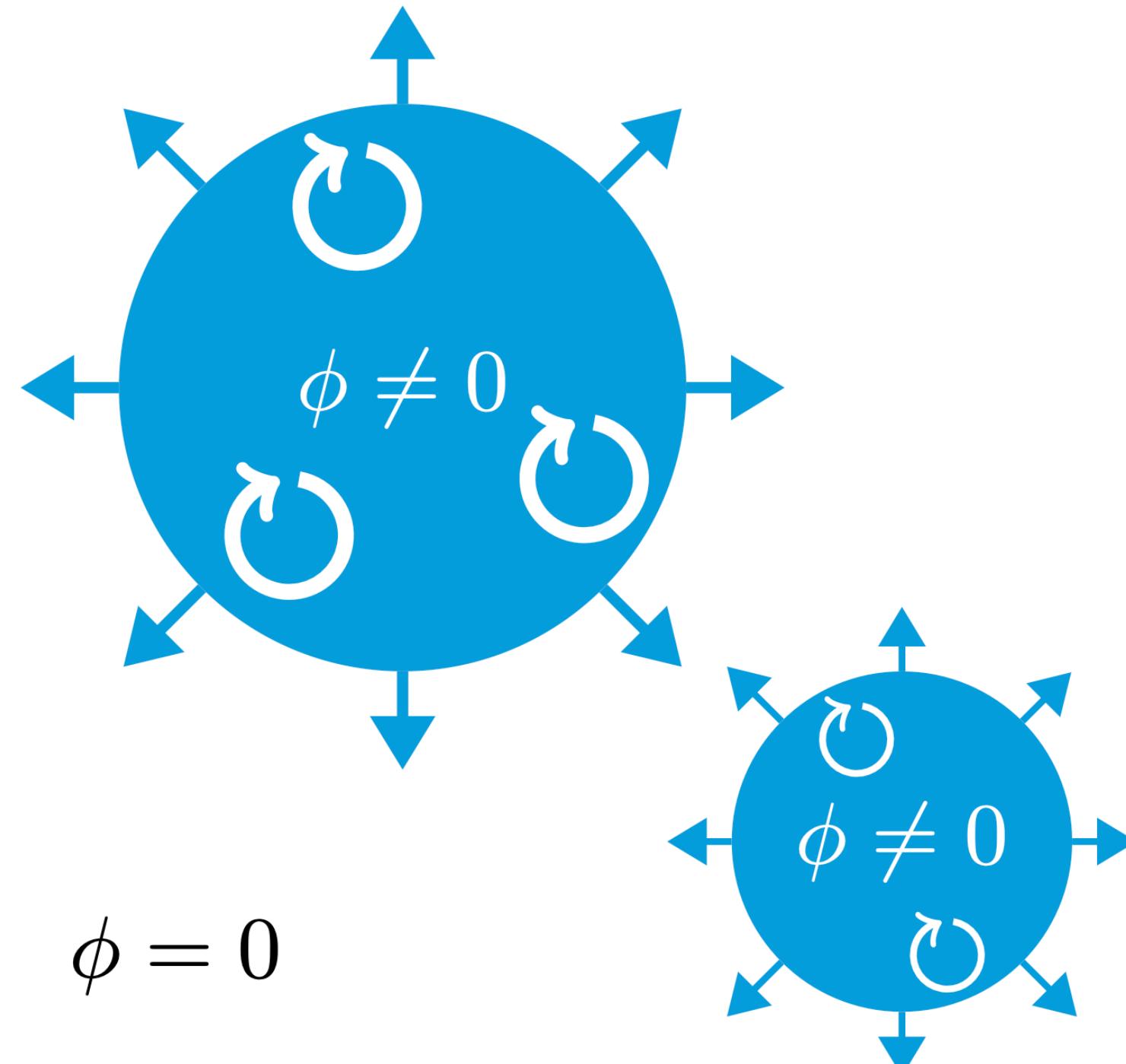


A scalar field tunnels to the true potential minimum $\phi \neq 0$ to minimize its free energy.

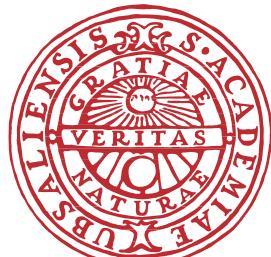


First-order phase transitions produce GWs

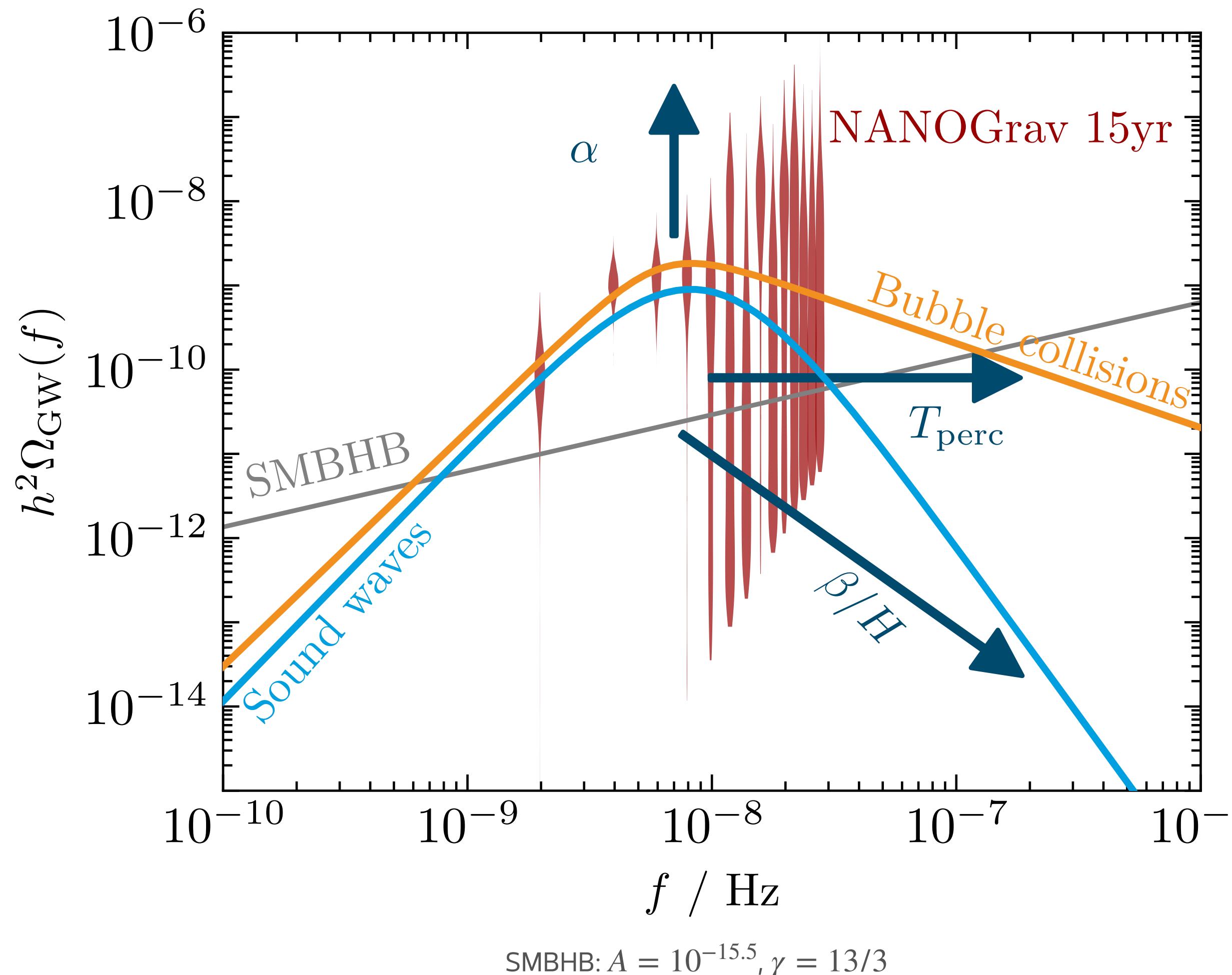
Bubbles of the new phase nucleate, collide and perturb the plasma...



... giving rise to an observable stochastic gravitational wave background.



Parametrization of the GW signal

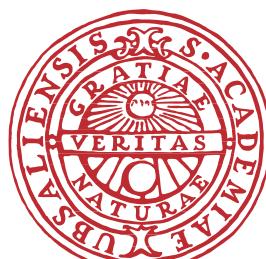


$$h^2 \Omega_{\text{GW}}^{\text{sw,bw}}(f) \simeq 10^{-6} \left(\frac{\alpha}{\alpha + 1} \right)^2 \left(\frac{H}{\beta} \right)^{1,2} \mathcal{S} \left(\frac{f}{f_{\text{peak}}} \right)$$

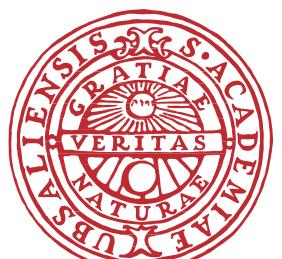
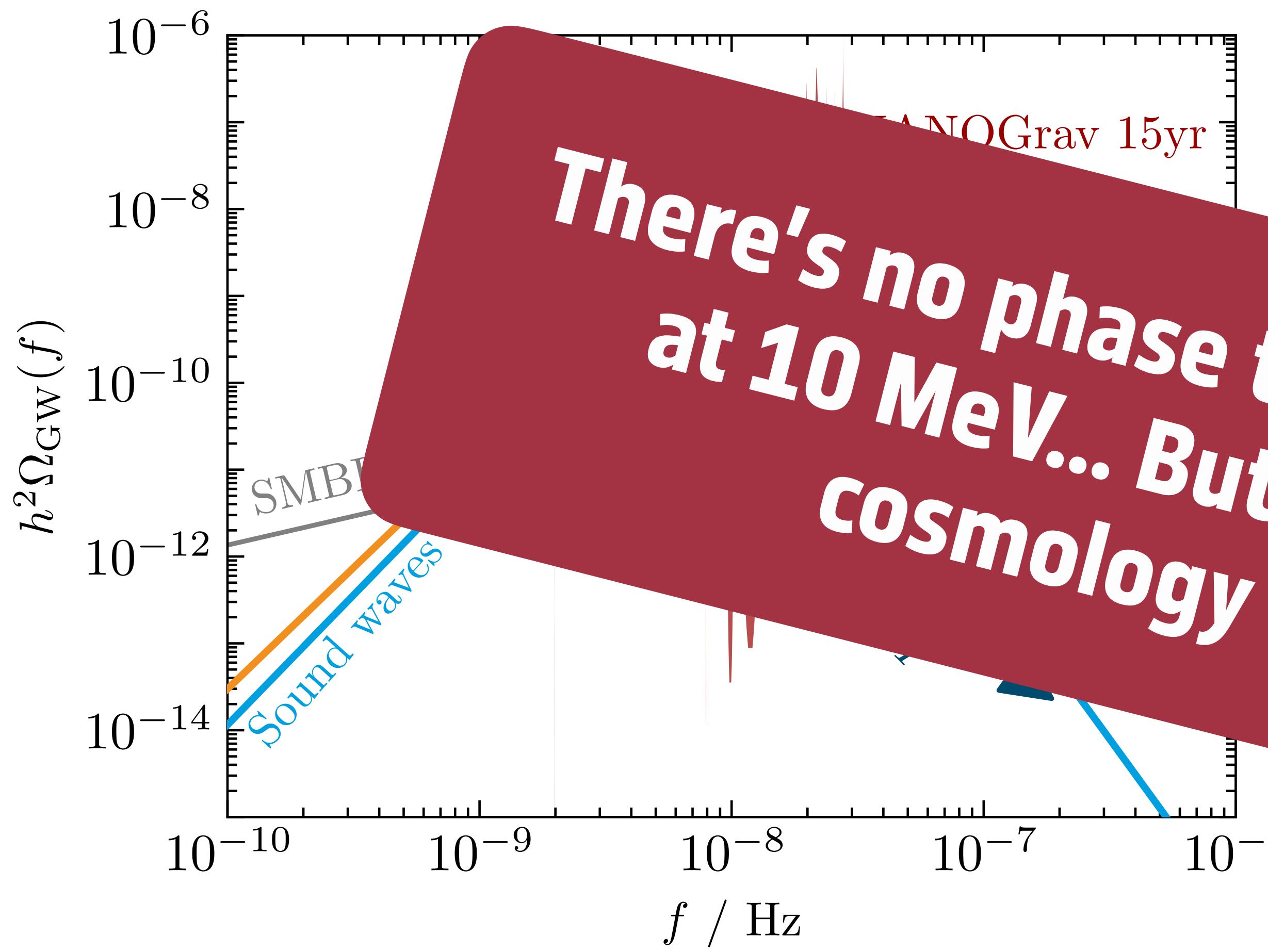
with $f_{\text{peak}} \simeq 0.1 \text{ nHz} \times \frac{\beta}{H} \times \frac{T}{\text{MeV}}$

To fit the new pulsar timing data:

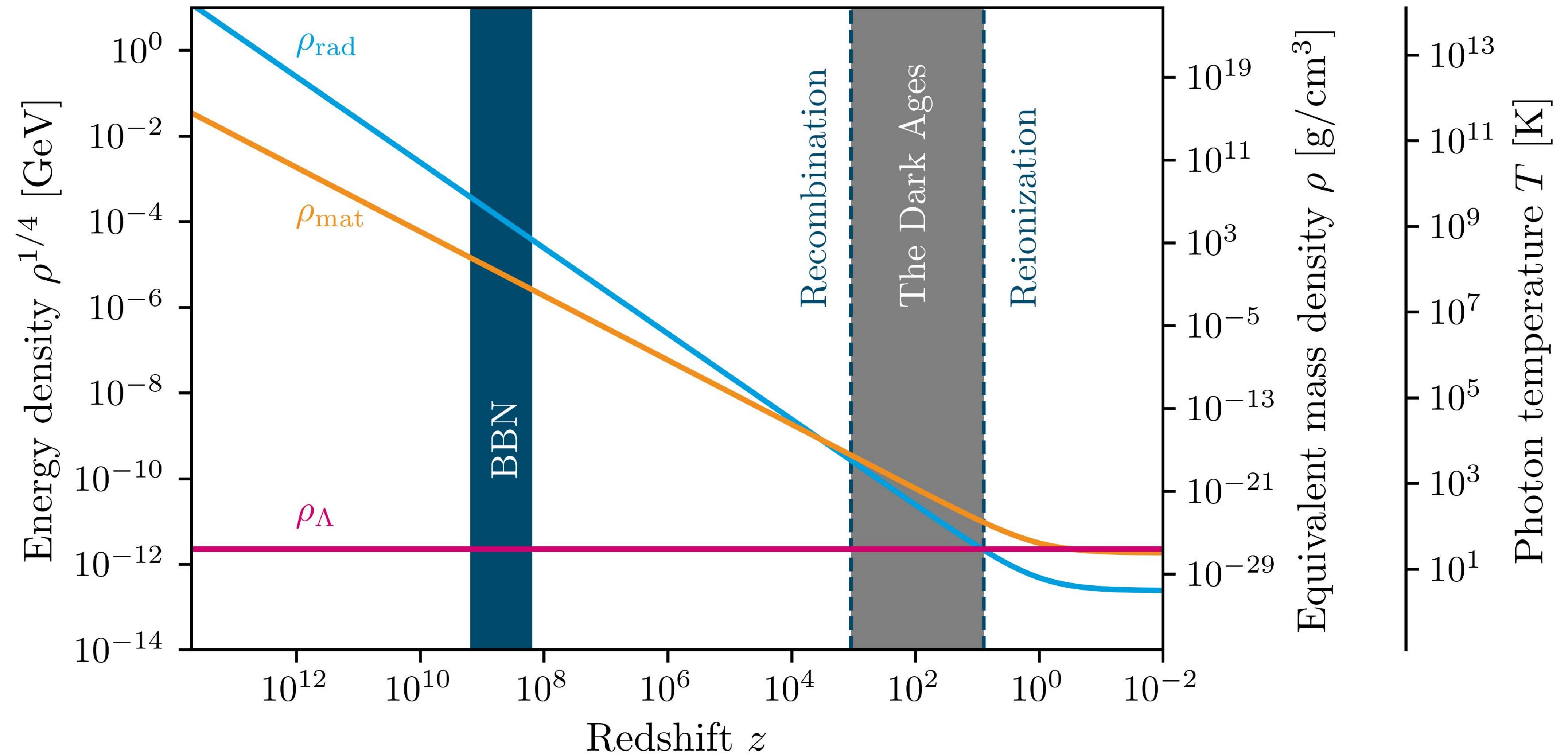
- Strong transitions, $\alpha \gtrsim 1$
- Slow transitions, $\beta/H \approx 10$
- Percolation around $T \approx 10 \text{ MeV}$



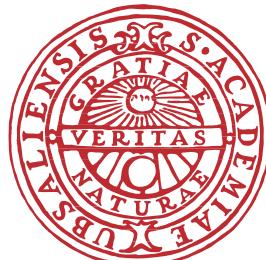
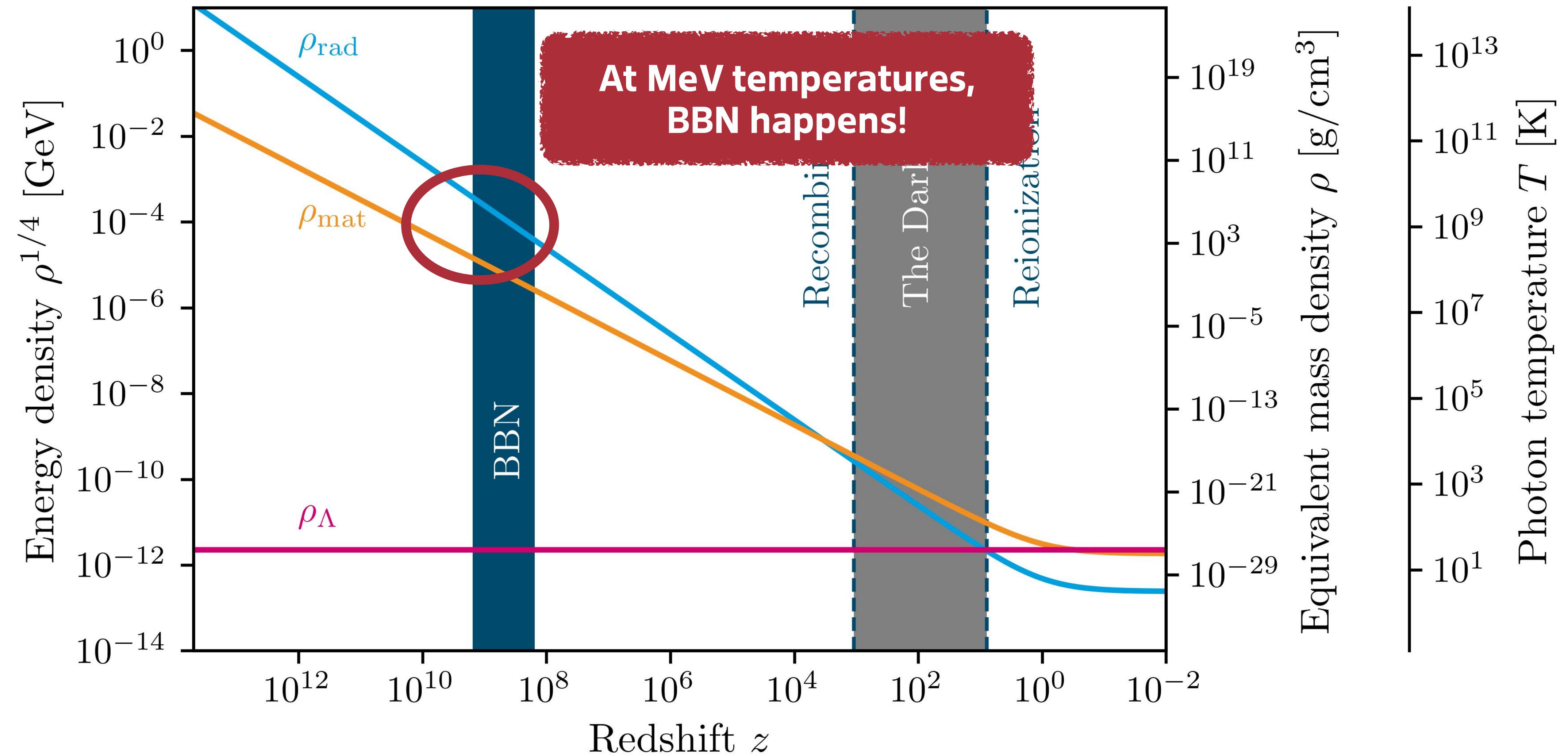
Parametrization of the GW signal



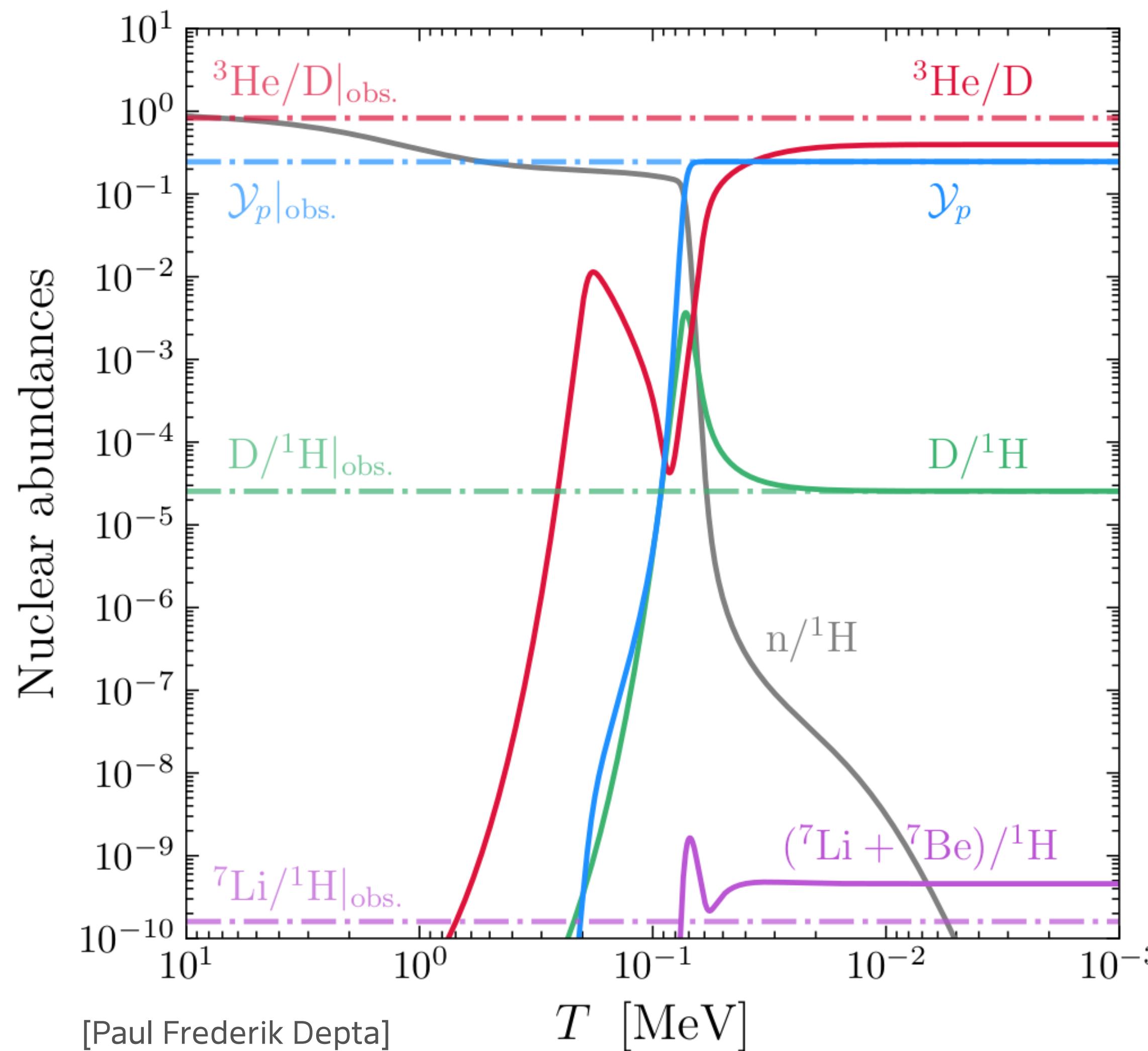
A brief history of time



A brief history of time



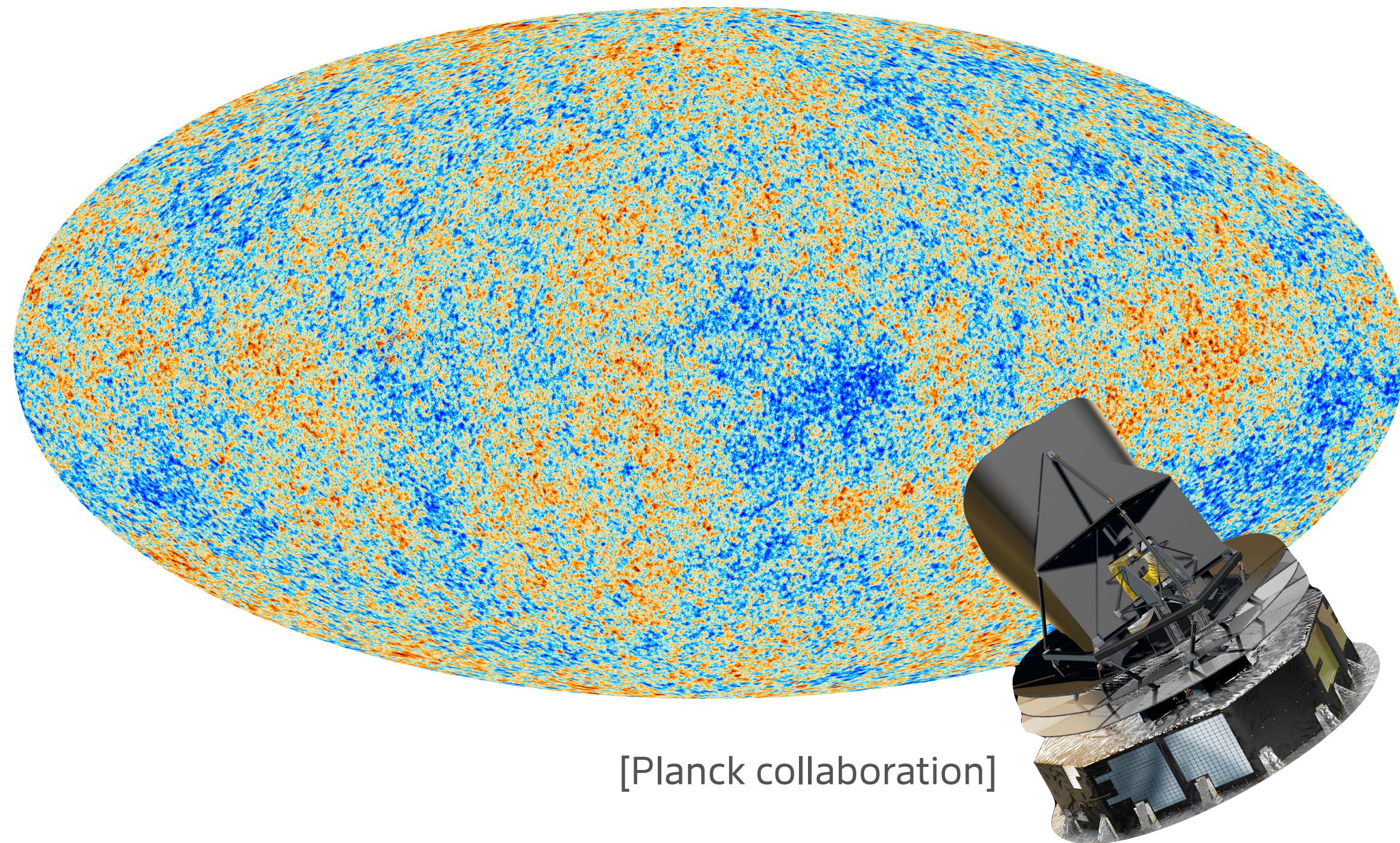
Big Bang Nucleosynthesis and the CMB



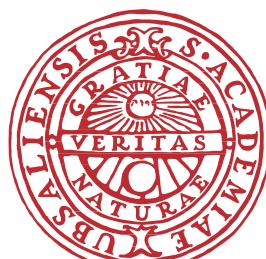
- Observation of primordial light element abundances in good agreement with standard BBN
- $N_{\text{eff}}^{\text{BBN}} = 2.898 \pm 0.141$



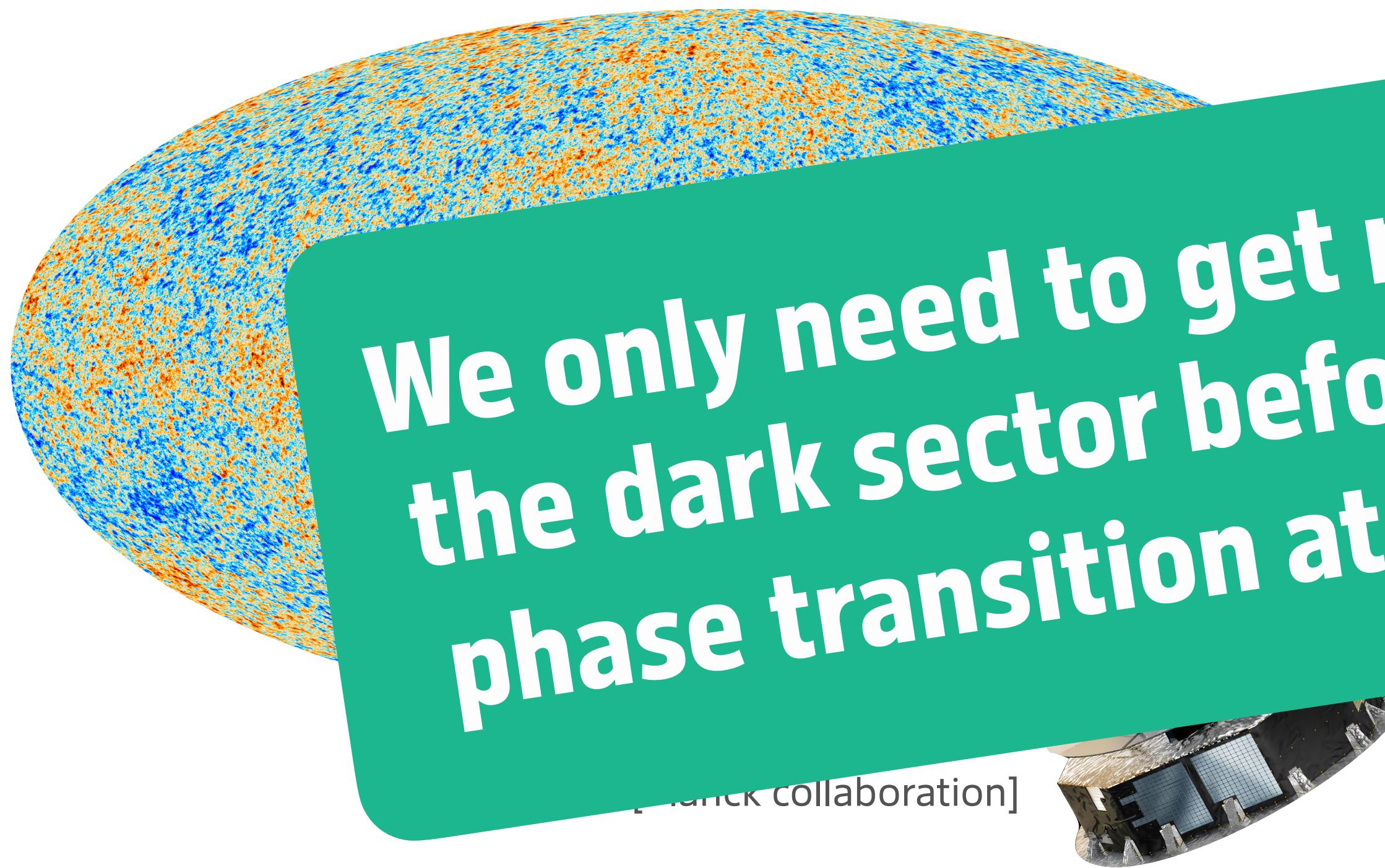
Big Bang Nucleosynthesis and the CMB



- Observation of primordial light element abundances in good agreement with standard BBN
- $N_{\text{eff}}^{\text{BBN}} = 2.898 \pm 0.141$
- $N_{\text{eff}}^{\text{CMB}} = 2.99 \pm 0.17$
- Consistent with 3 SM neutrinos



Big Bang Nucleosynthesis and the CMB

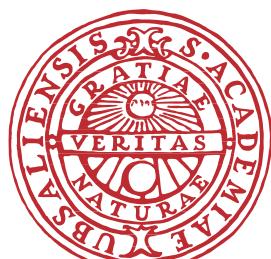


- Observation of primordial abundances in the CMB

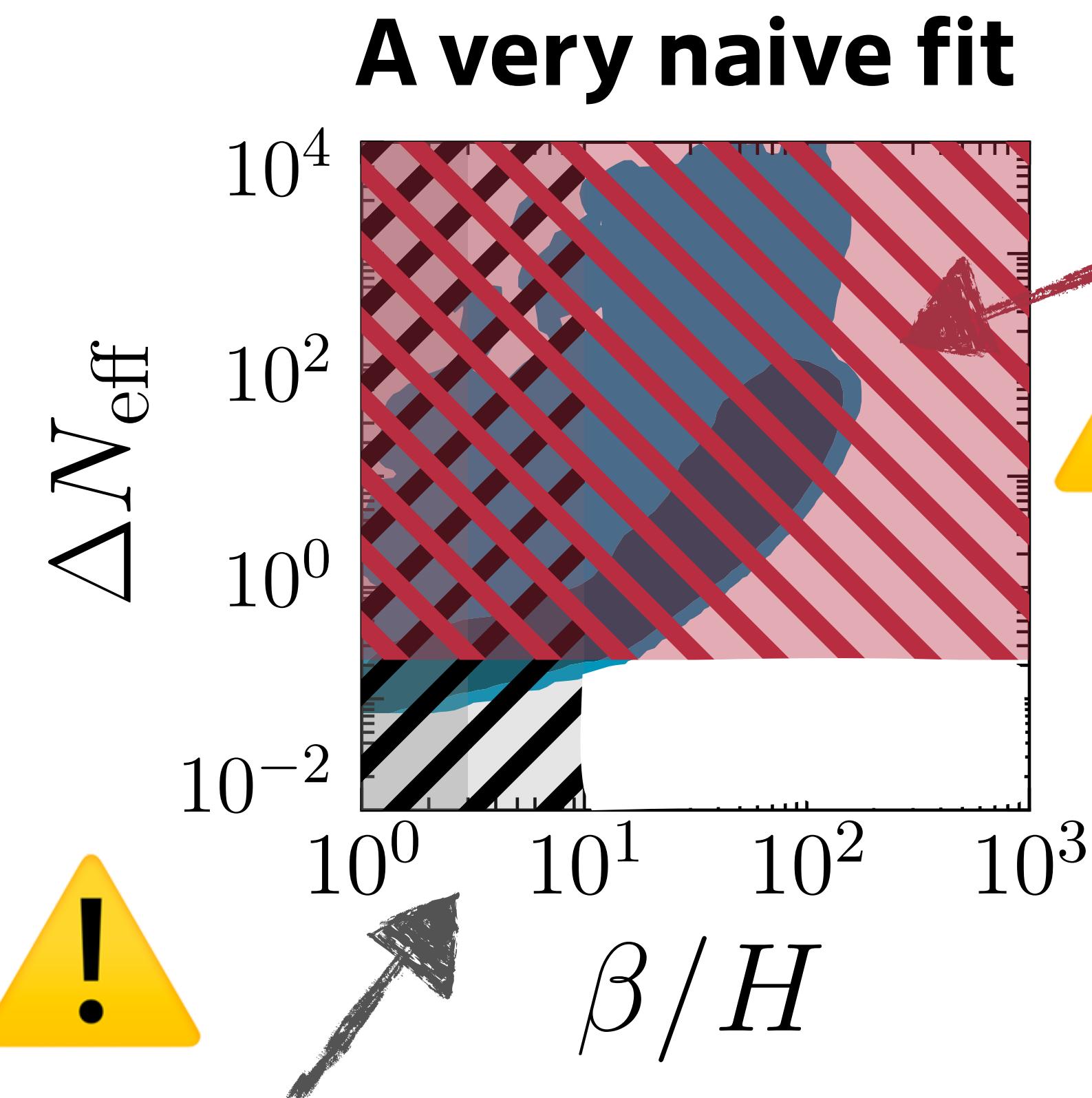
41

$$\text{enr} = 2.99 \pm 0.17$$

- Consistent with 3 SM neutrinos



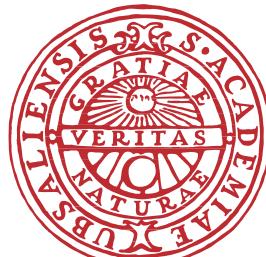
A dark sector without portal couplings



The liberated vacuum energy remains in the dark sector. A good fit would require enormous $\Delta N_{\text{eff}} \gg 0.22$

Giant „Hubble” bubble sizes would be needed, violating causality & questioning validity of GW predictions

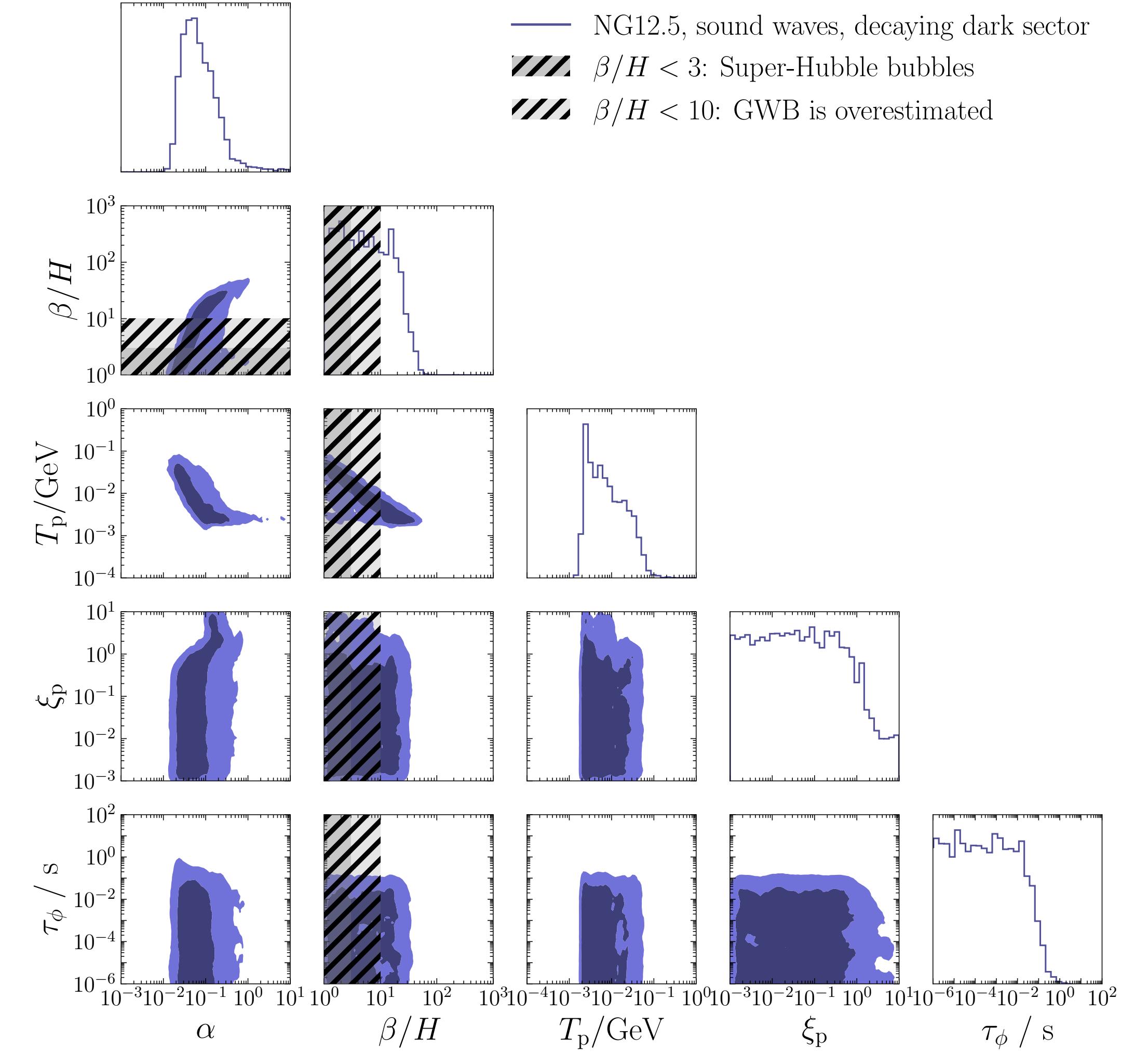
[CT et al, JCAP 11 (2023) 053]



The dark sector must die for the GWs to live...



If the dark sector decays before BBN, a great fit to PTA data can be achieved!

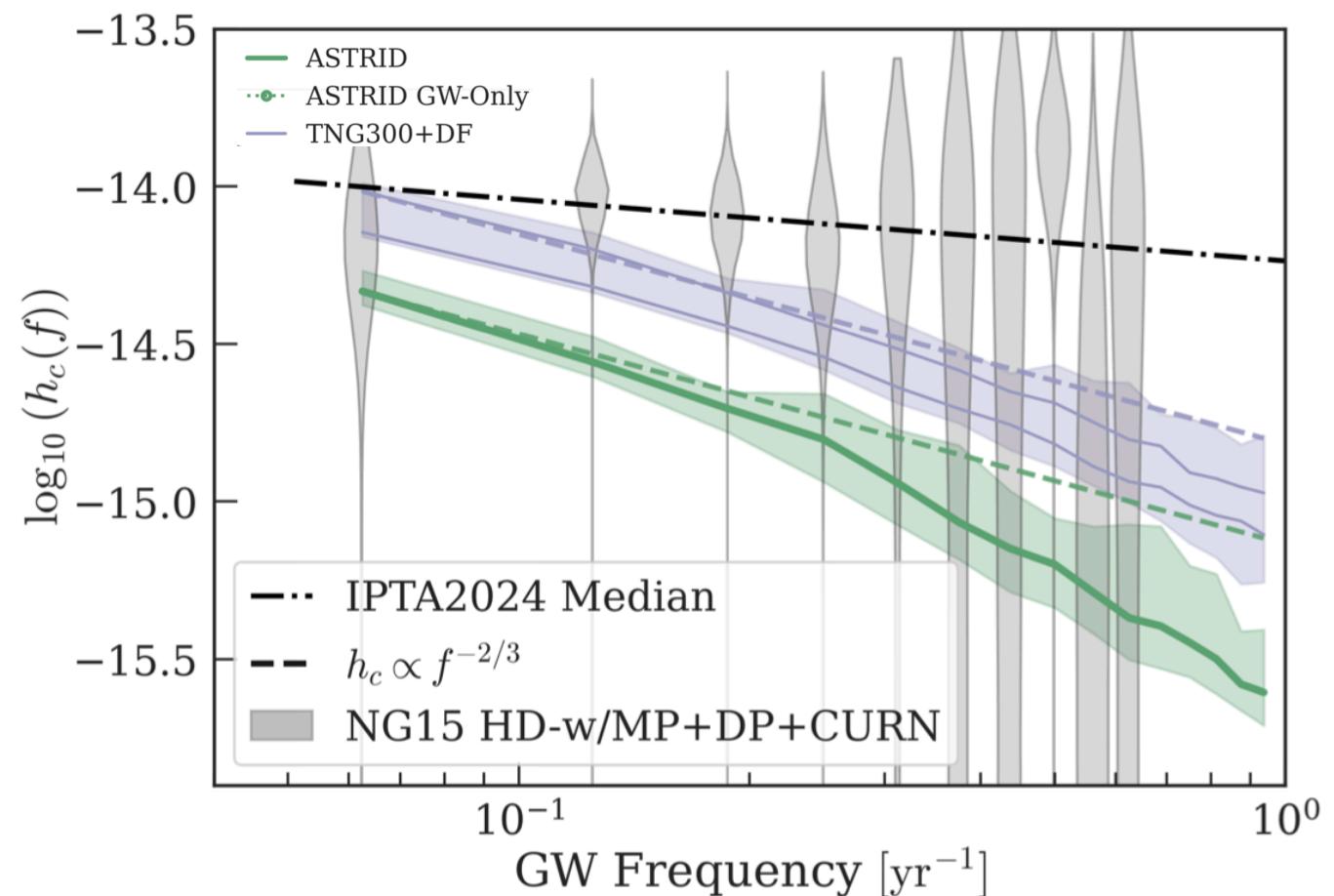


[CT et al, JCAP 11 (2023) 053]



New PTA data: higher peak frequency and slope

[NANOGrav, PPTA, EPTA,
CPTA, InPTA, Meerkat]



N-Body simulations:
SMBHB unable to account for full GW signal

[Chen+, 2502.01024]

What happened since July 2023?

Solution to the final parsec problem?

[Chiaberge+, 2501.18730]

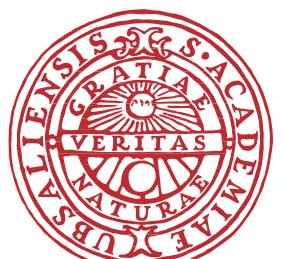
Investigation of specific dark sector models

[2412.16282, 2501.11619, 2501.14986,
2501.15649, 2502.04108, ...]

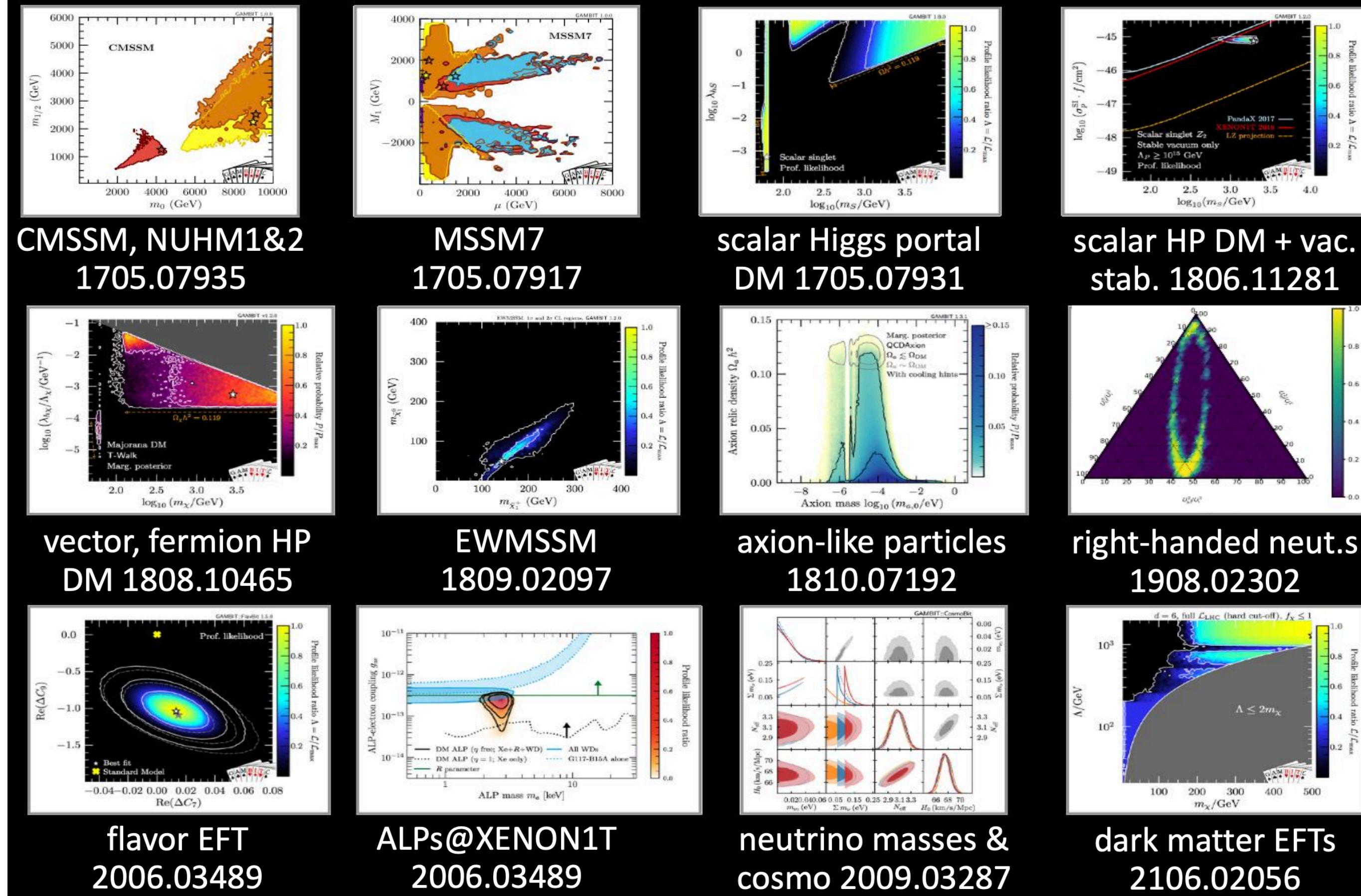
More constraints than just ΔN_{eff} ?

CT+ [JCAP 08 (2025) 062]

Rest of this talk and my own focus



GAMBIT: from Lagrangians to Likelihoods

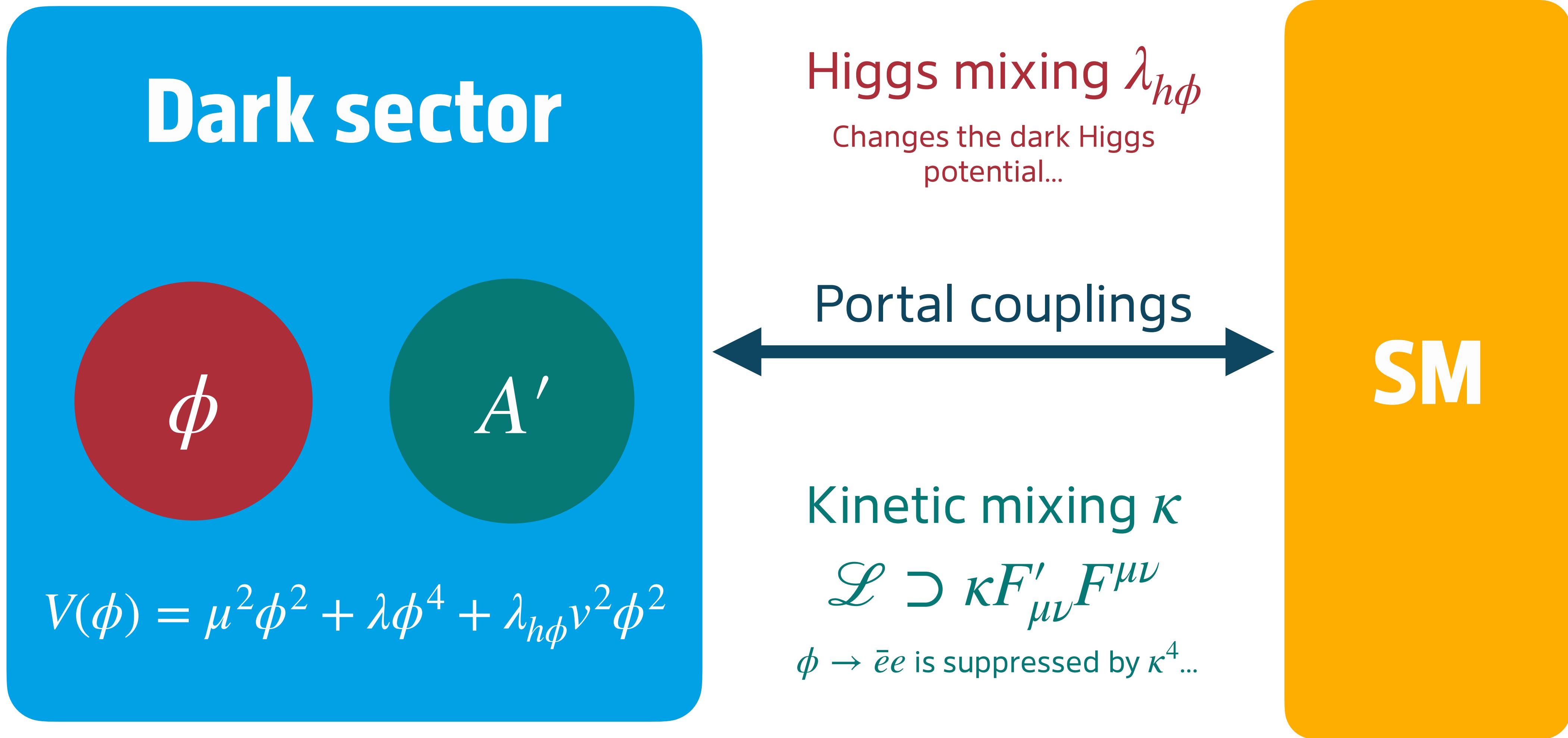


Slide by C. Balázs @ SUSY 2021

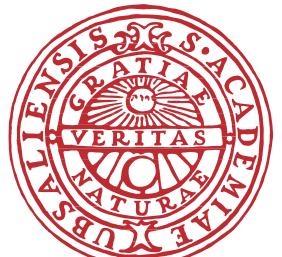


To combine BBN + CMB,
direct and indirect DM
detection, bullet cluster
and beam dump
constraints: GAMBIT

A minimal dark sector setup



See 2412.16282, 2501.11619, 2501.15649, 2501.14986
by Banik, Gonçalves, Costa, Li et al.



A minimal dark sector setup

Dark sector

$$V(\phi)$$

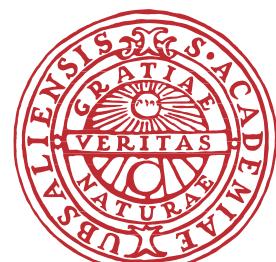
This model is flawed. Hard (impossible?) to avoid cosmological constraints and fine-tuning...

$$\mathcal{L} \supset \kappa F'_{\mu\nu} F^{\mu\nu}$$

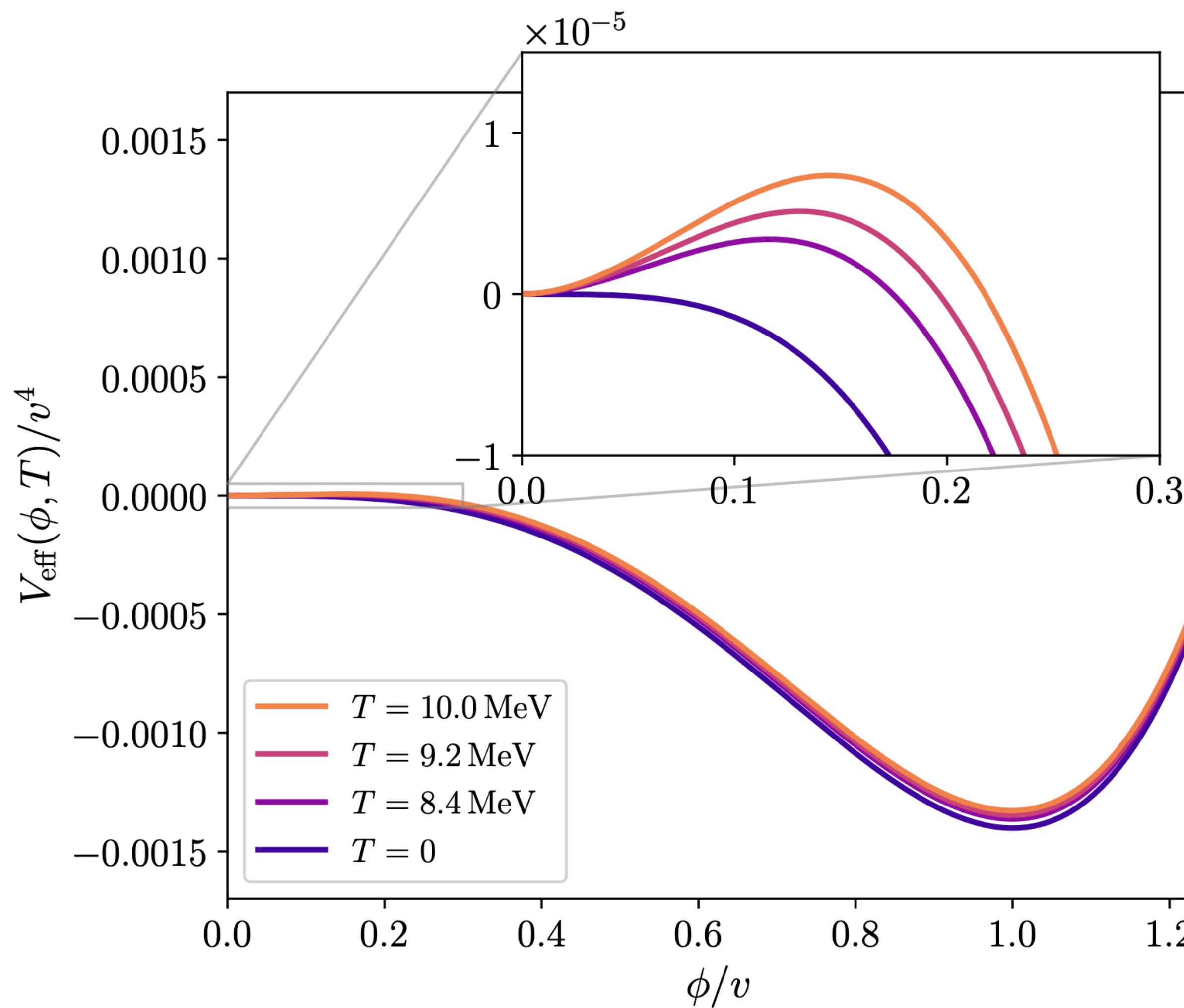
$\phi \rightarrow \bar{e}e$ is suppressed by κ^4 ...

Higgs mixing

?



Interlude: How to be supercool 😎



Note: This is not the *only* way to achieve strong supercooling. Watch out for my upcoming paper together with Jonas, Kai, Thomas and Torsten! :)

$$V_{\text{tree}}(\phi) = \lambda \phi^4$$

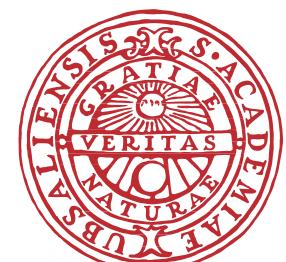
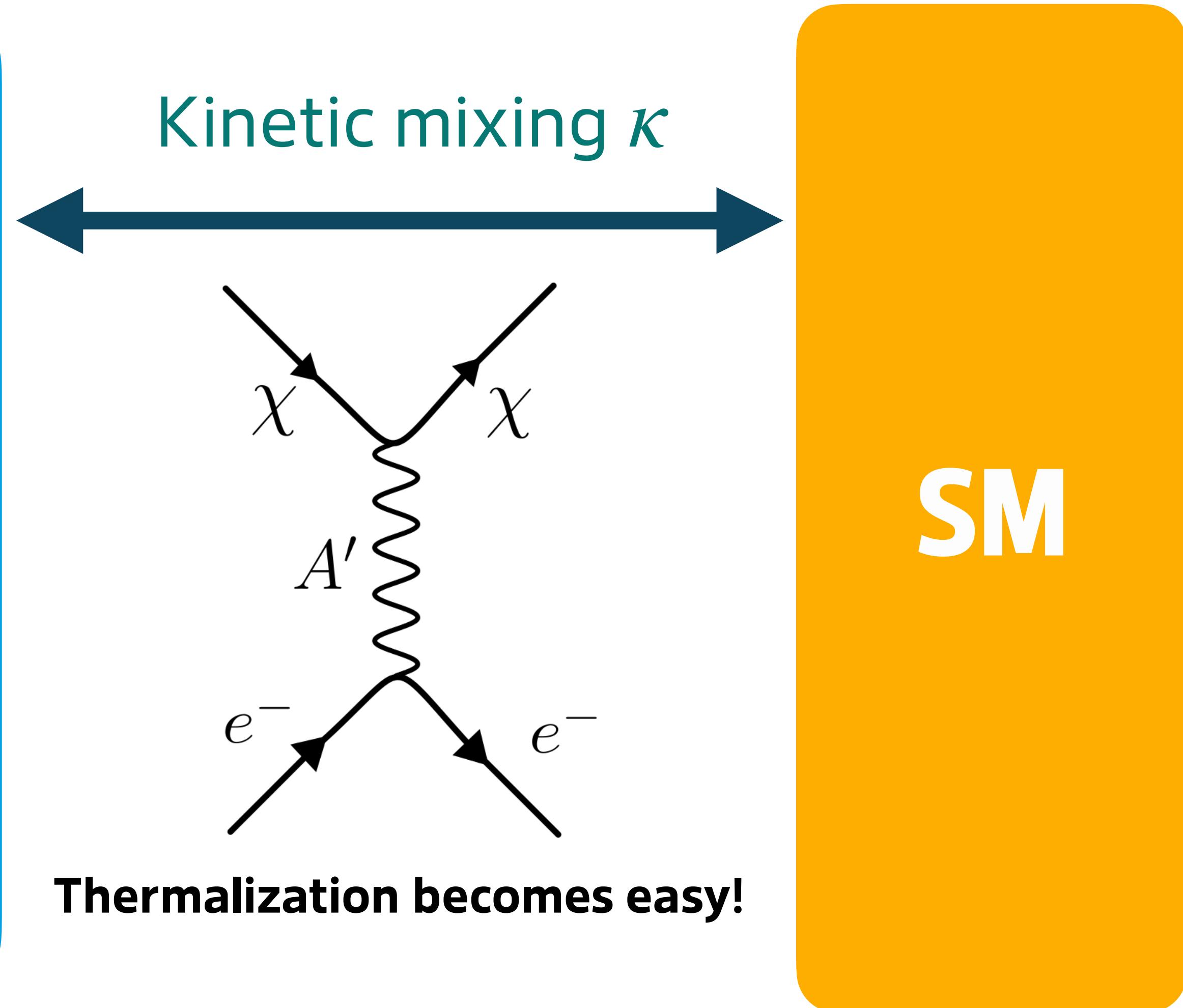
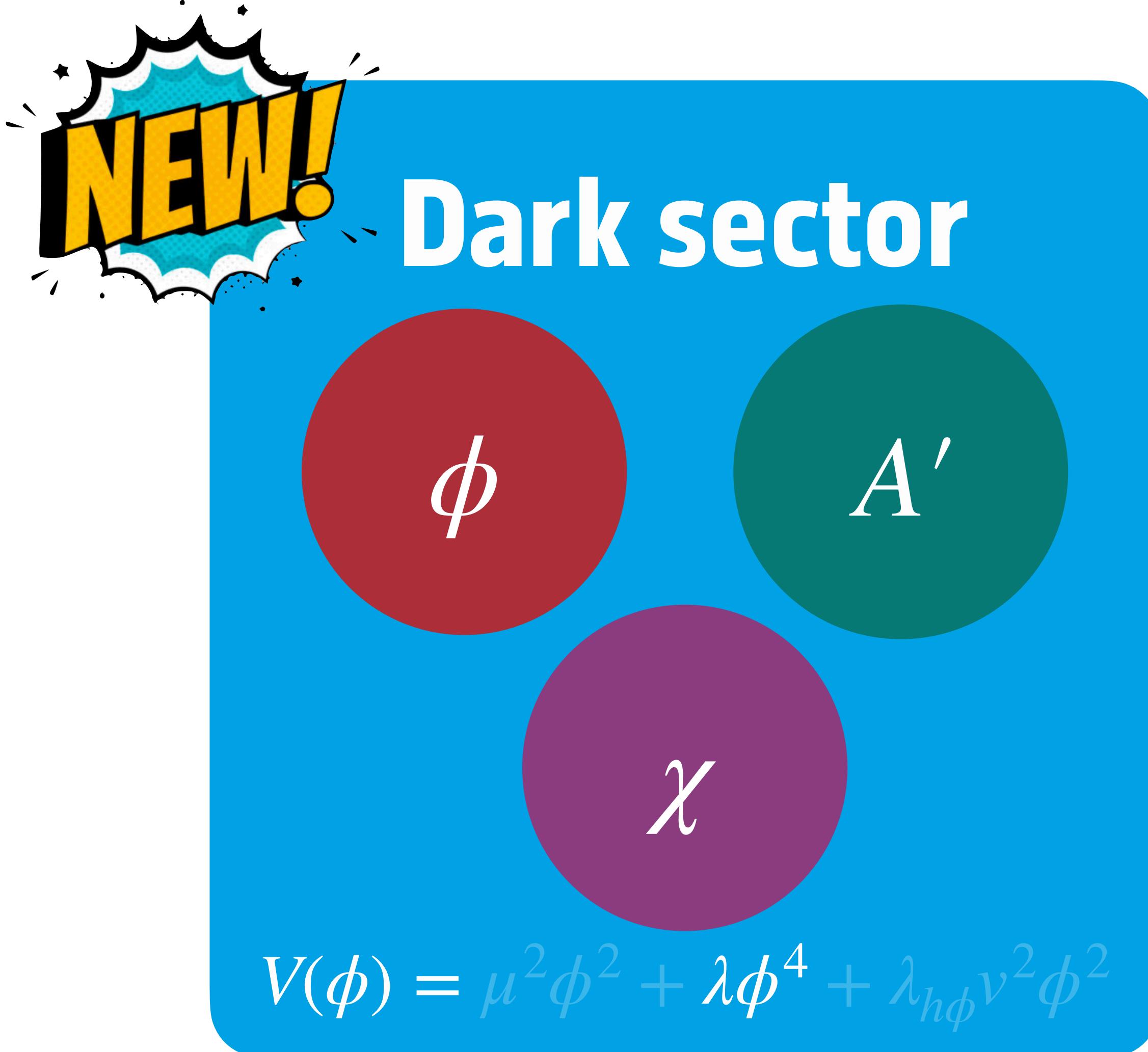
Quantum and thermal corrections

$$V_{\text{eff}}(\phi, T) \supset \lambda \phi^4 \log\left(\frac{T}{v}\right)$$

Loop-induced barrier down until very low temperatures, i.e. strong supercooling



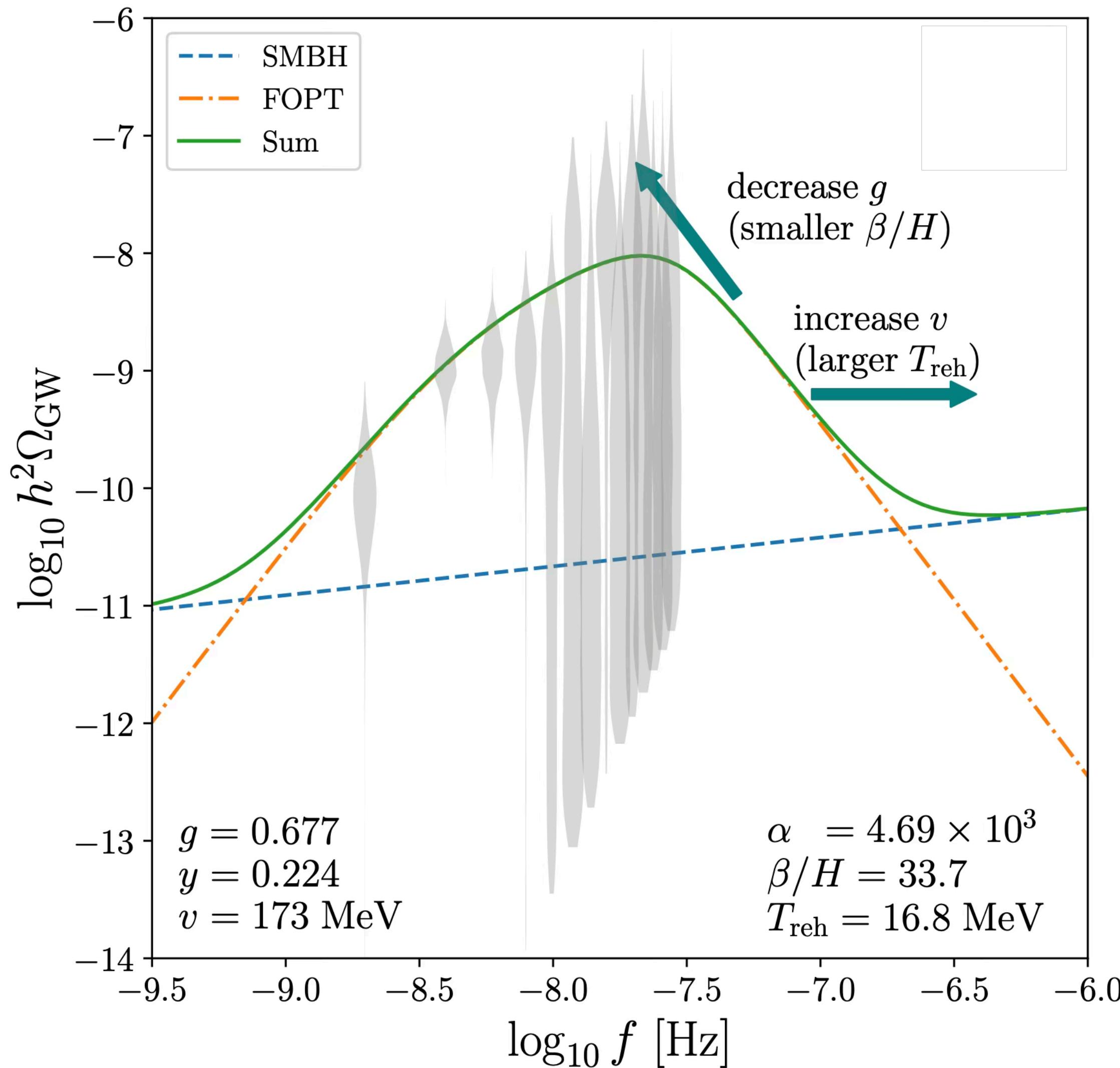
A conformal dark sector incl. dark matter candidate



CT+ [JCAP 08 (2025) 062]

Carlo Tasillo — The Nano-Hertz Gravitational Wave Background: Connection to sub-GeV dark matter

All constraints can be circumvented



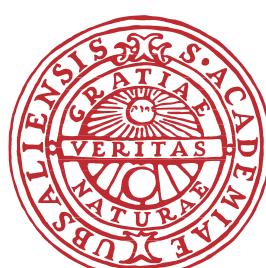
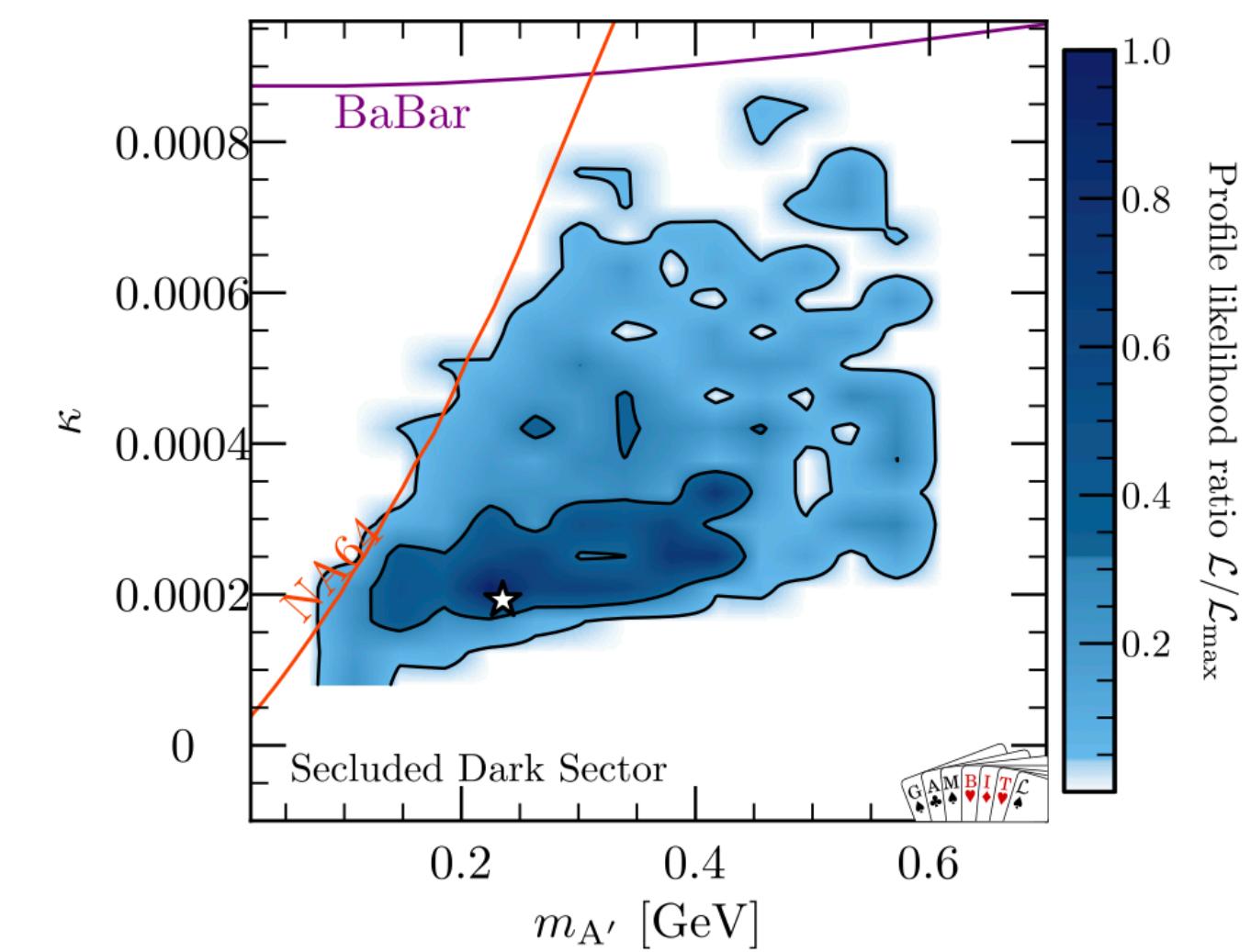
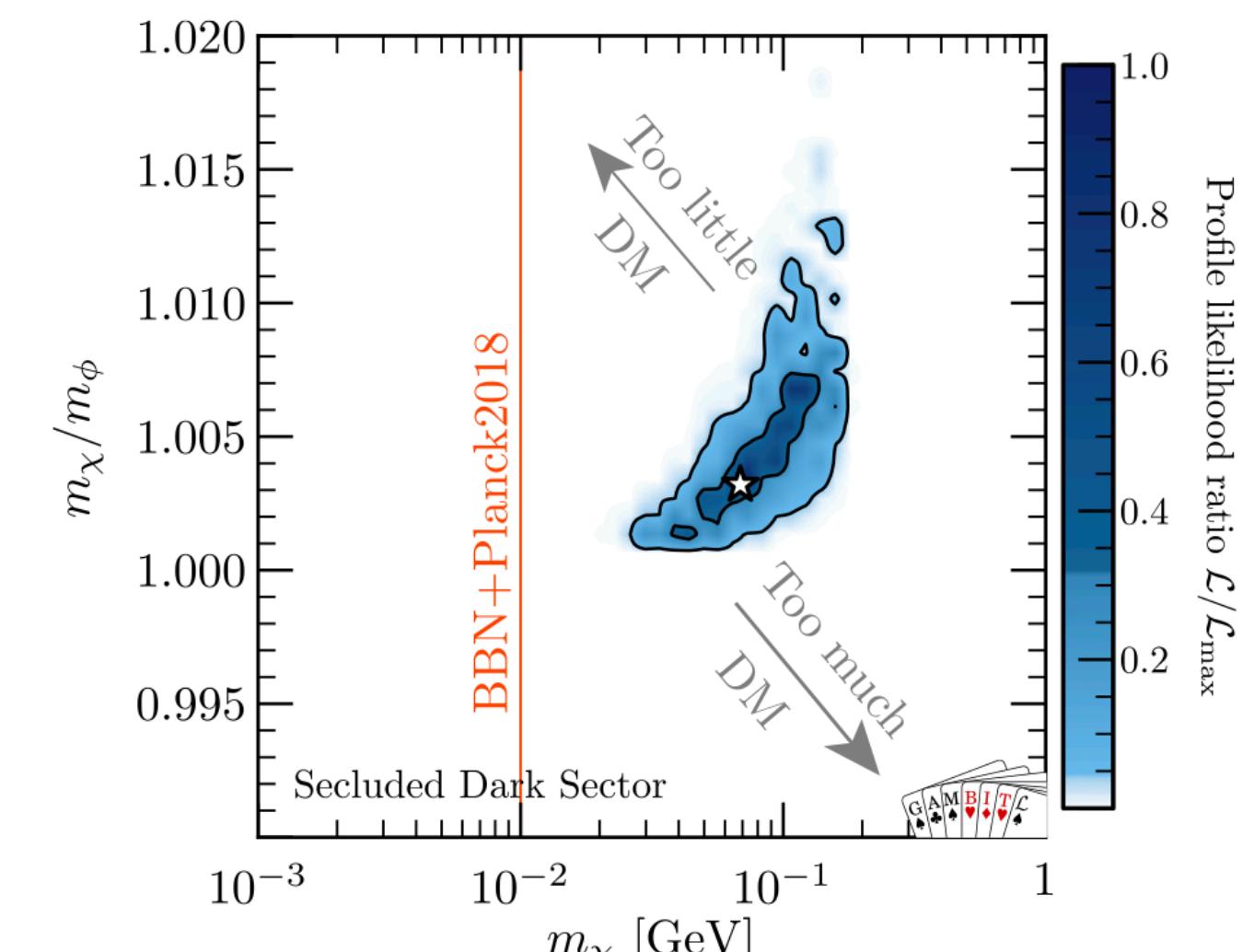
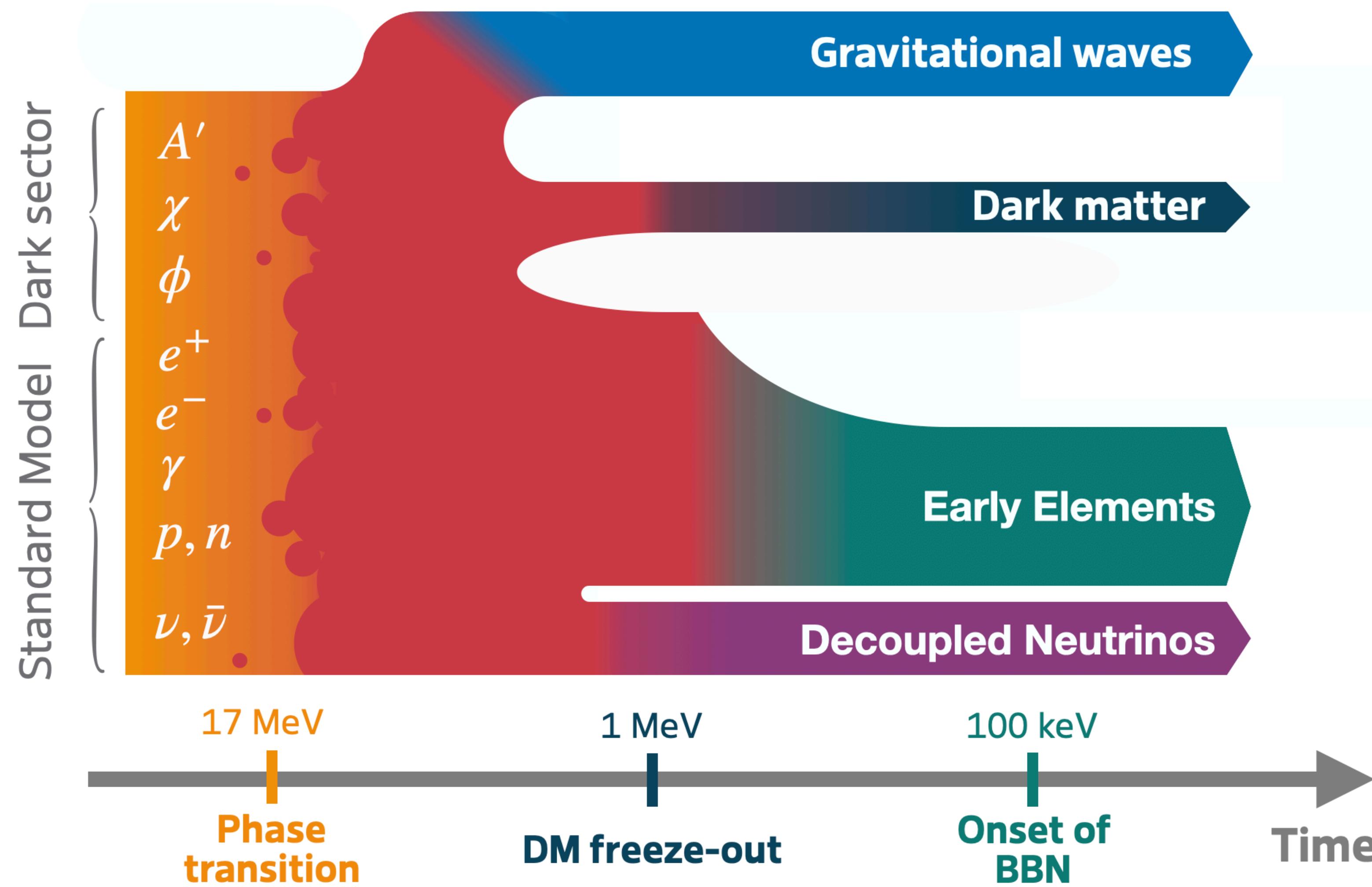
Global fit found parameter space with

- 100% of observed DM relic density
- Loud phase transition on top of „standard“ SMBH background
- Negligible impact on BBN and CMB
- No relevant direct + indirect detection + bullet cluster constraints
- Testable LDMX/Belle-II/NA64 prediction:

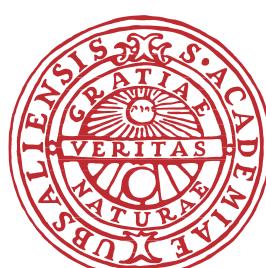
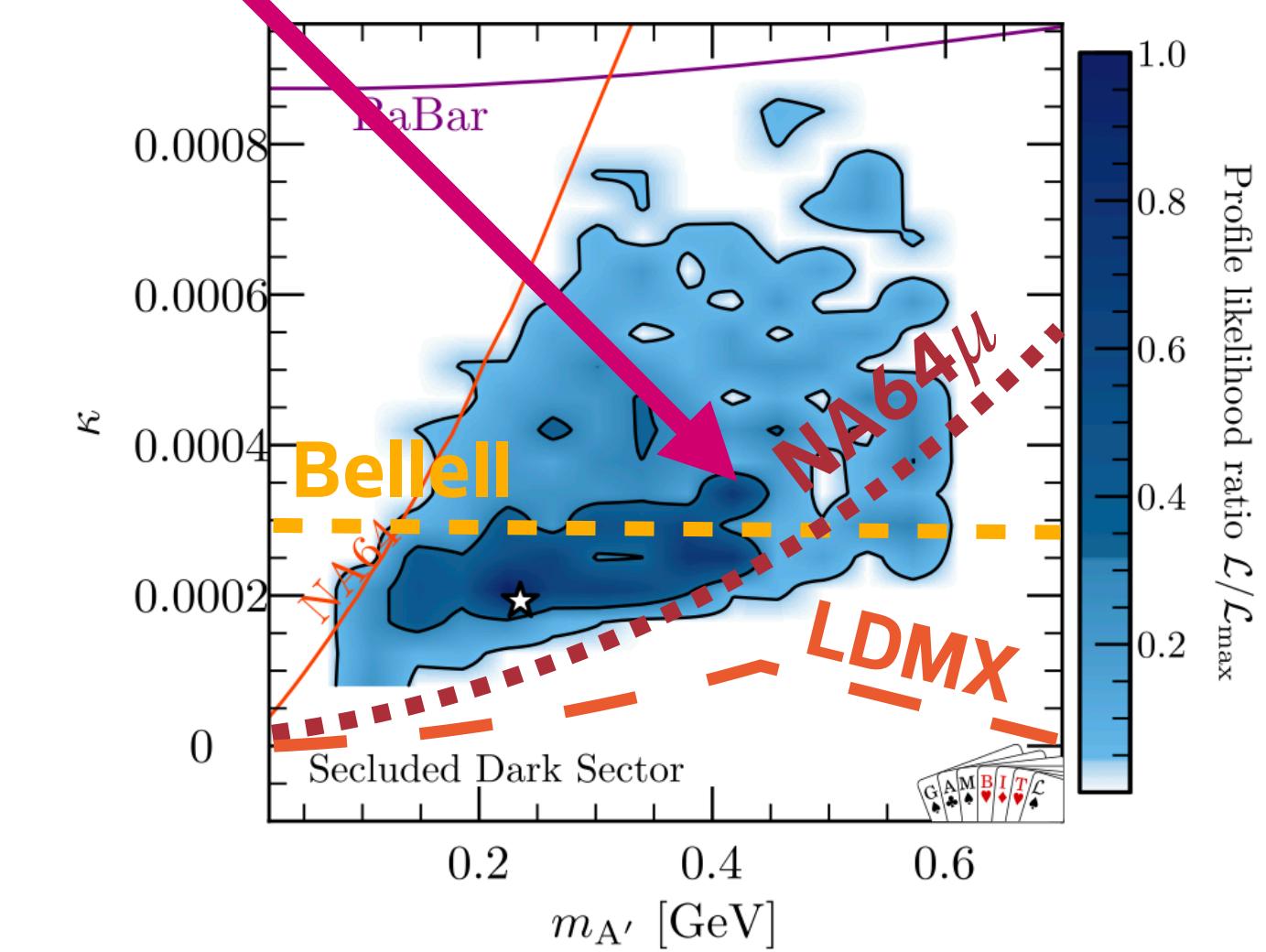
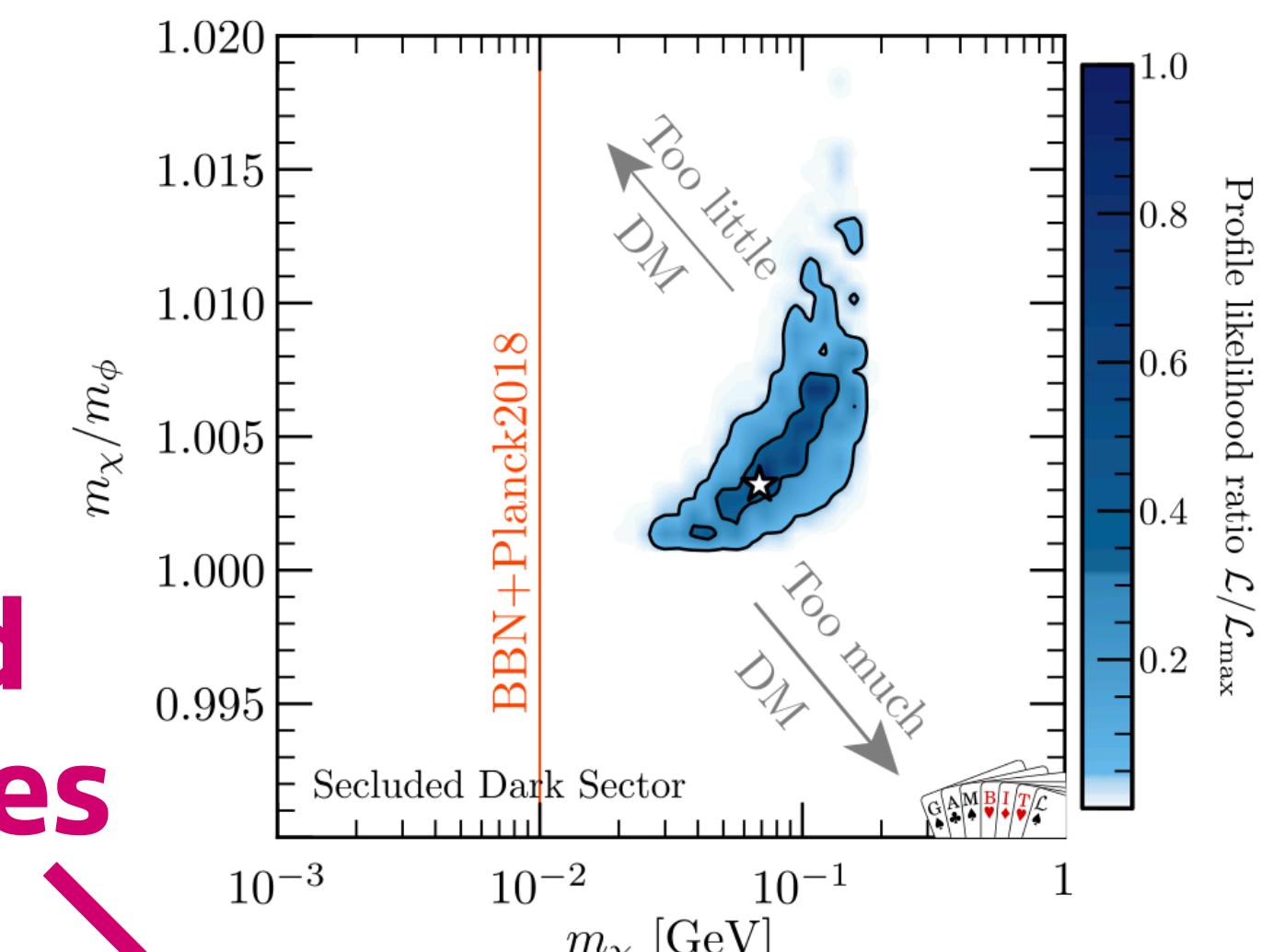
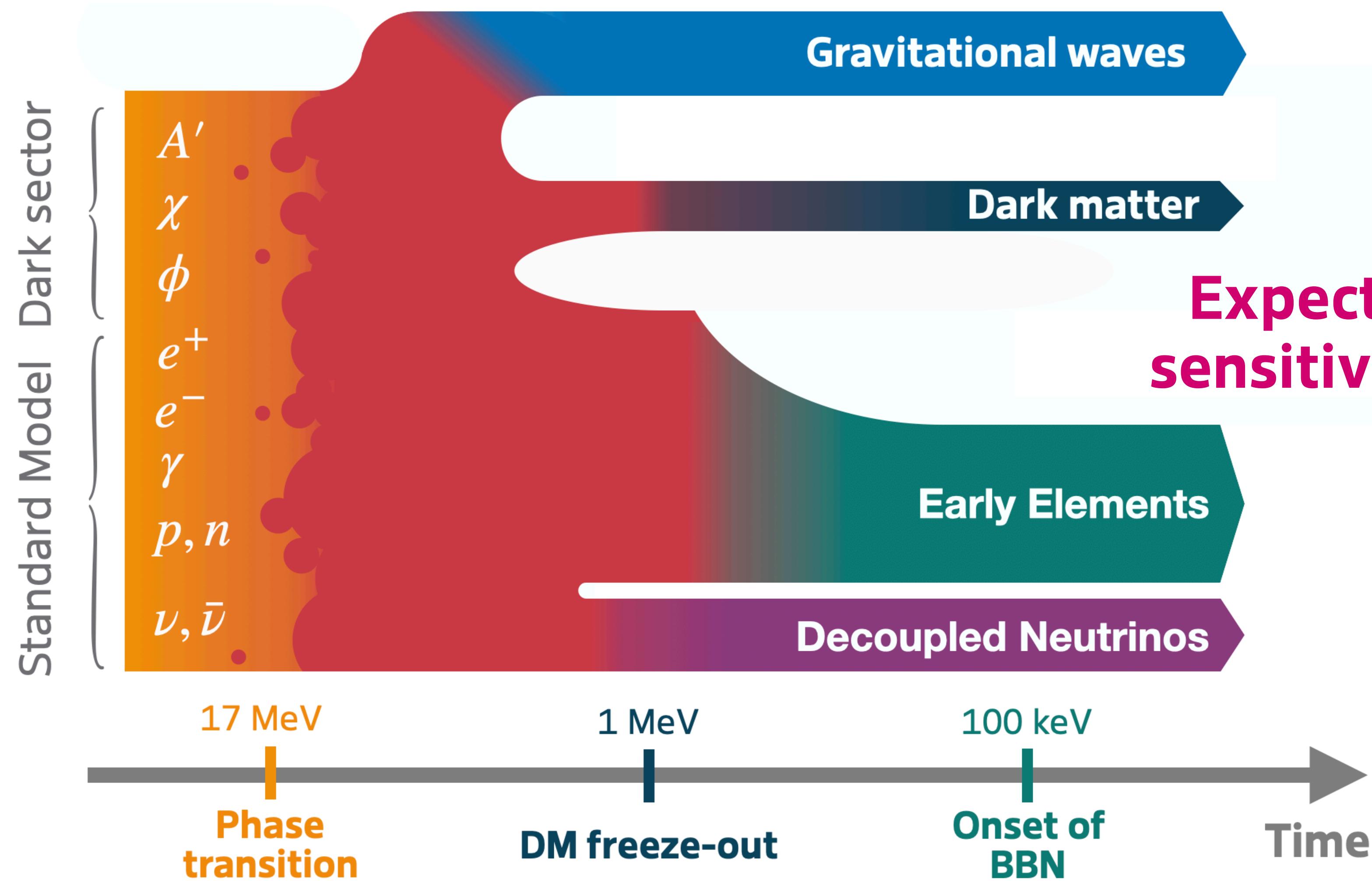
$$m_{A'} = 100 - 200 \text{ MeV}, \kappa \simeq 10^{-4}$$



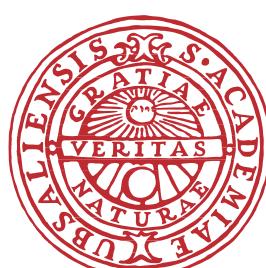
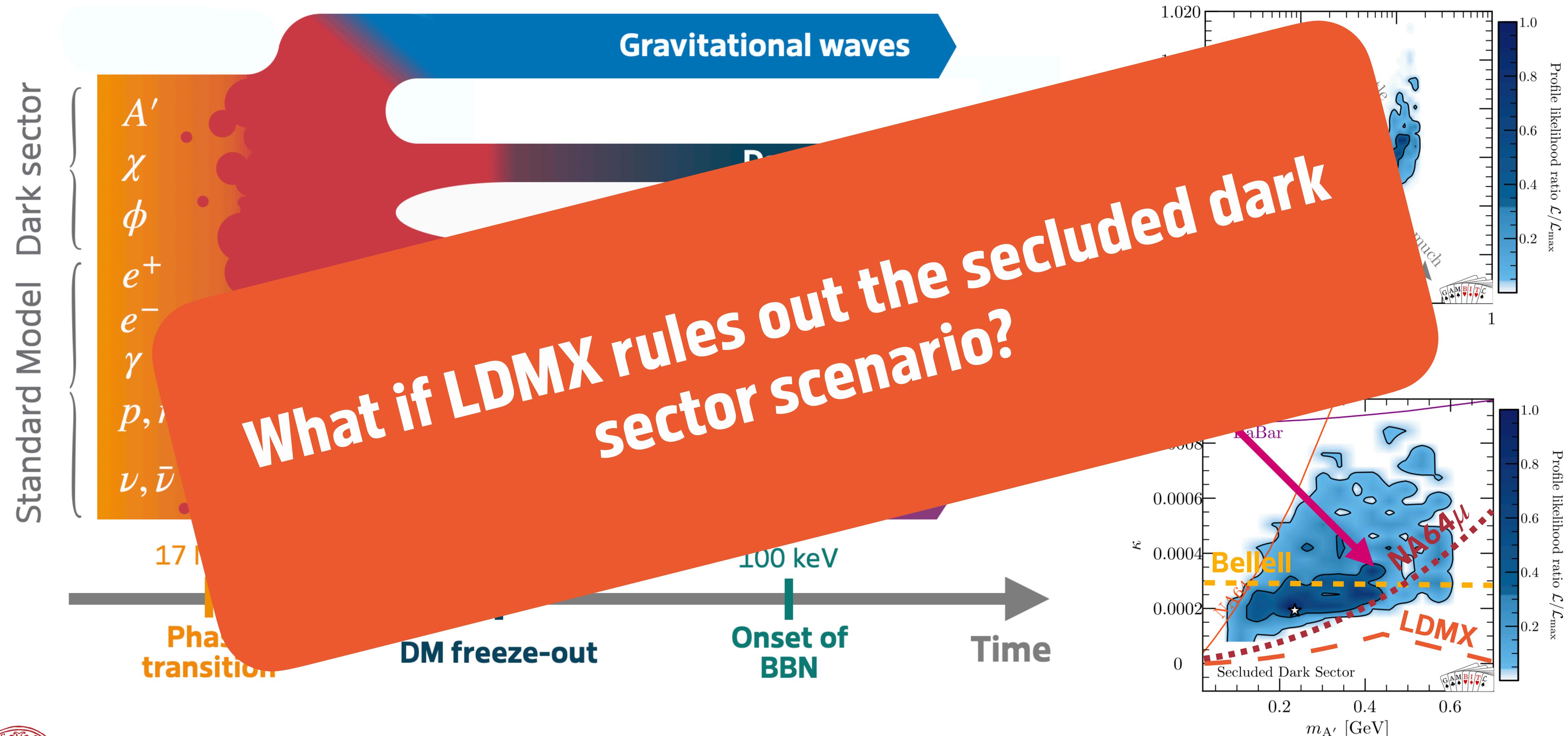
How does our scenario evade all available constraints?



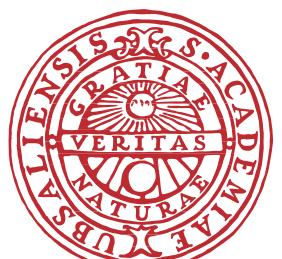
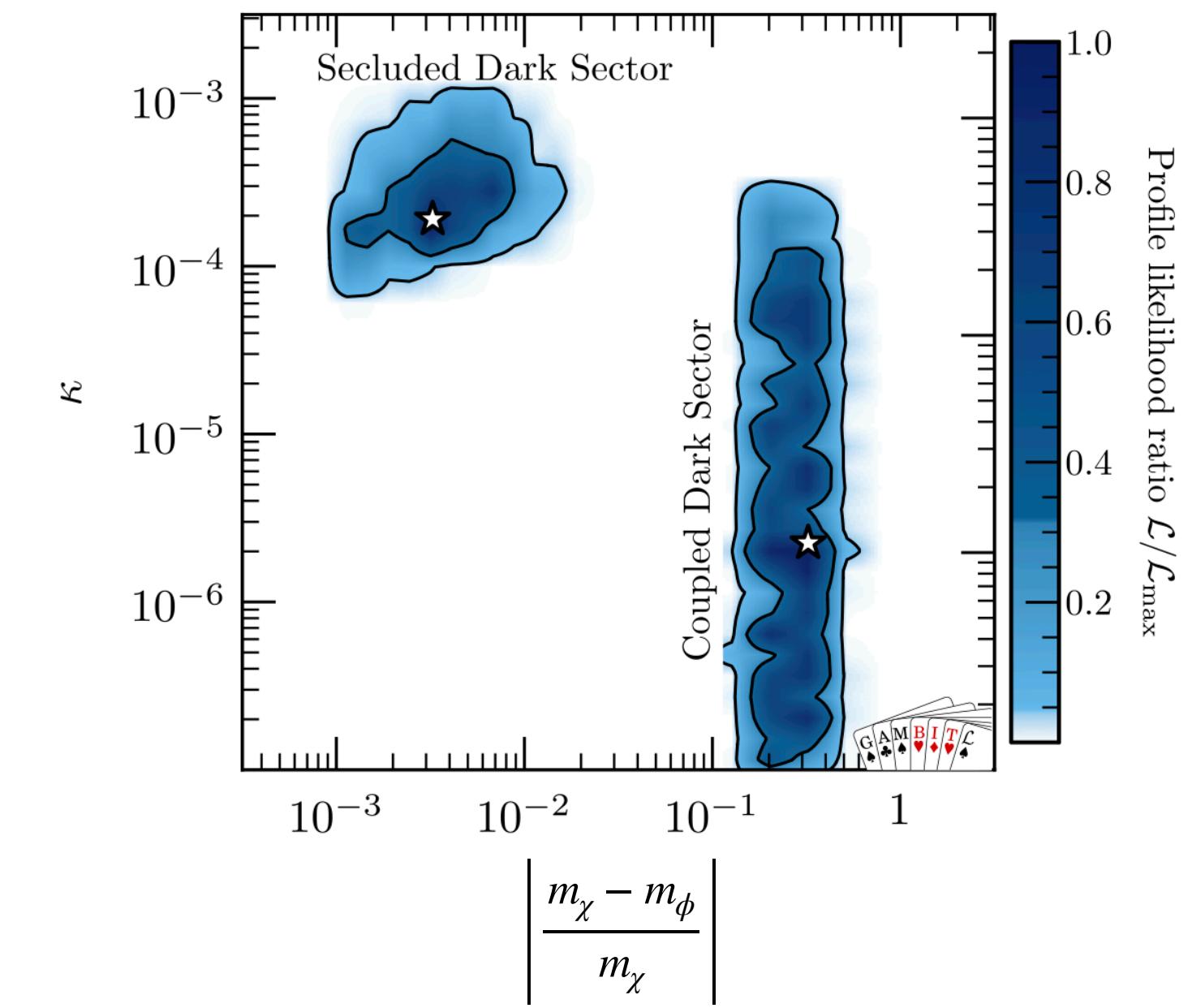
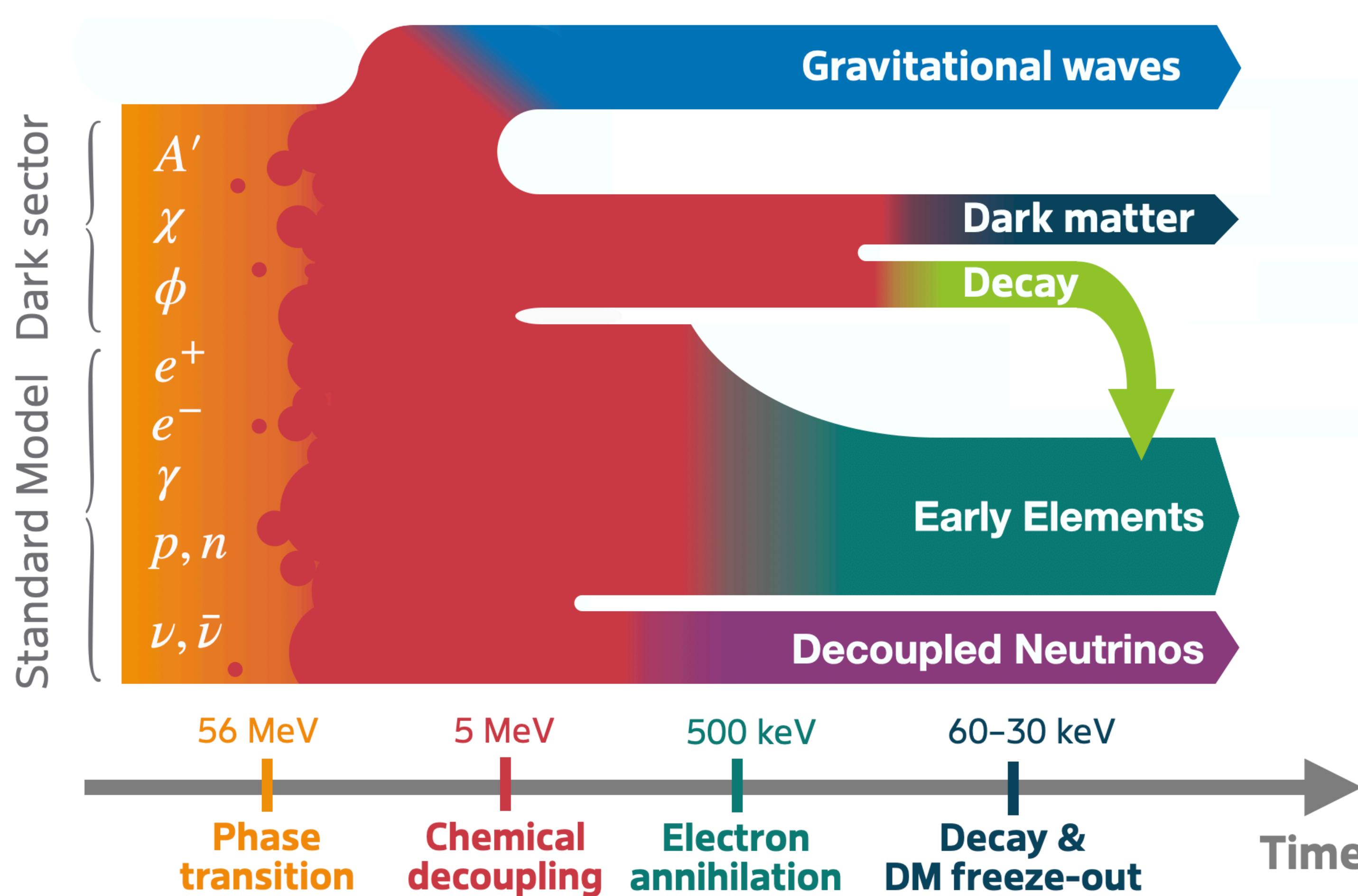
How does our scenario evade all available constraints?



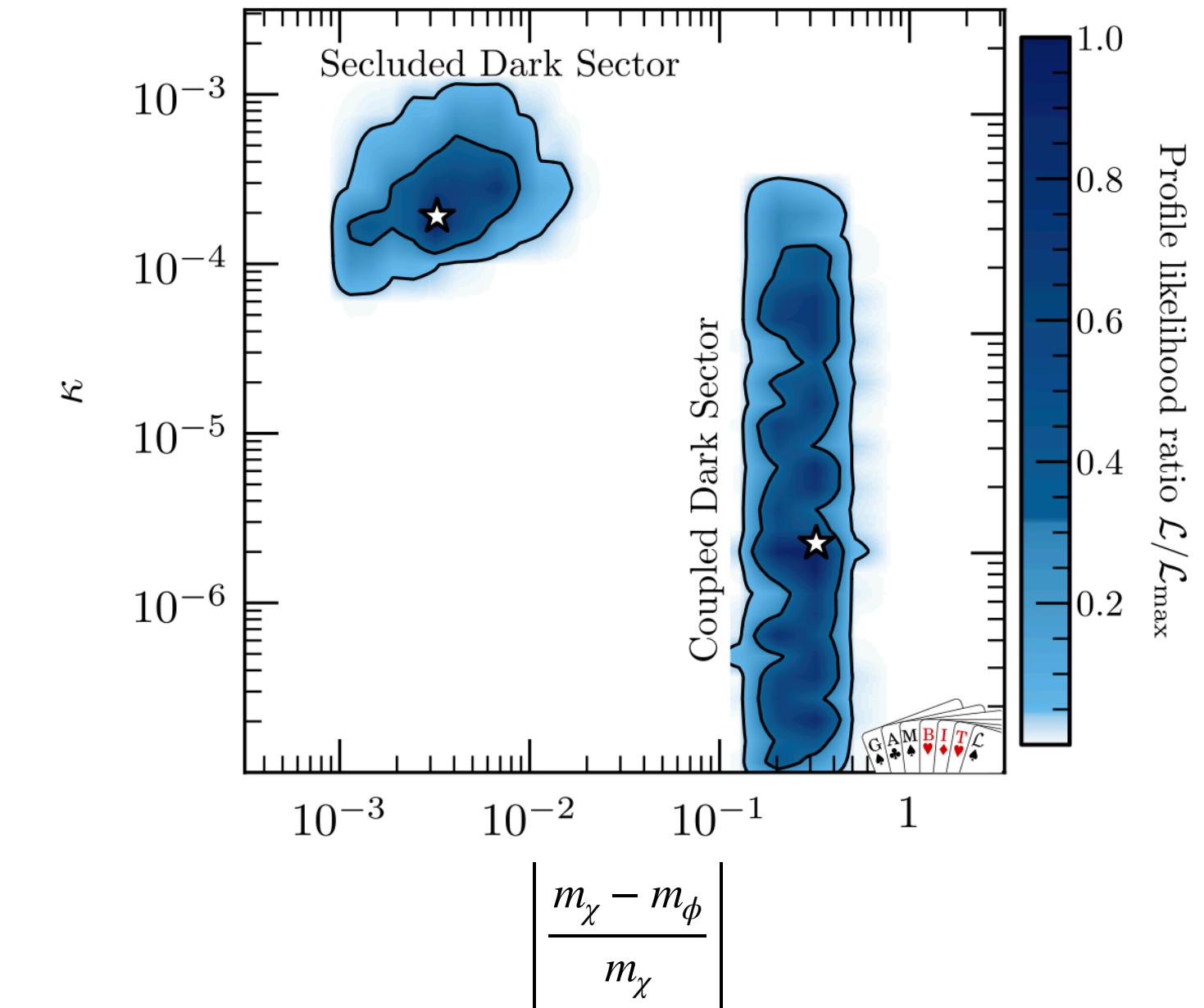
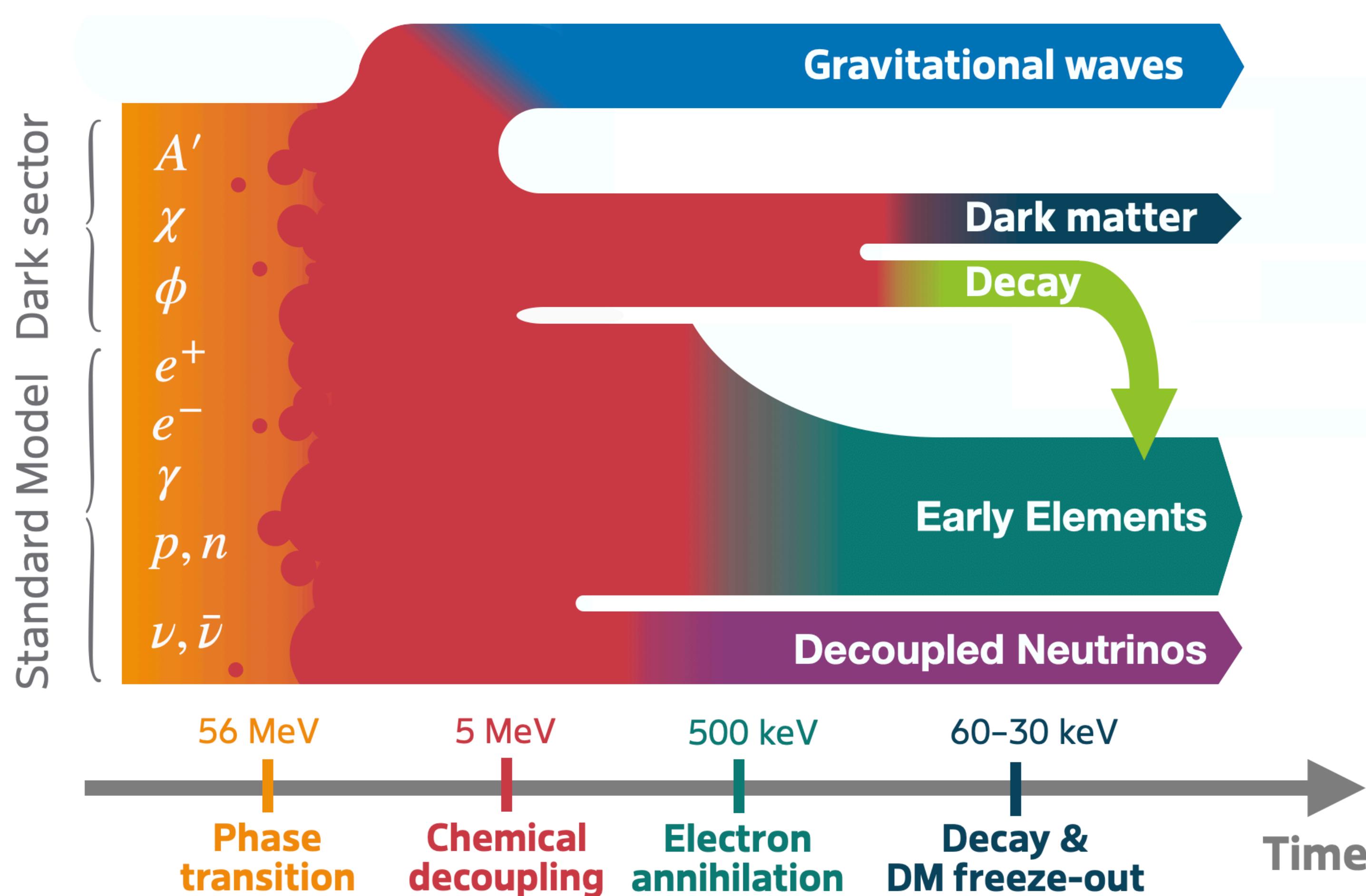
How does our scenario evade all available constraints?



Coupled DS scenario: incl dim-6 operator for $\phi \rightarrow ee$



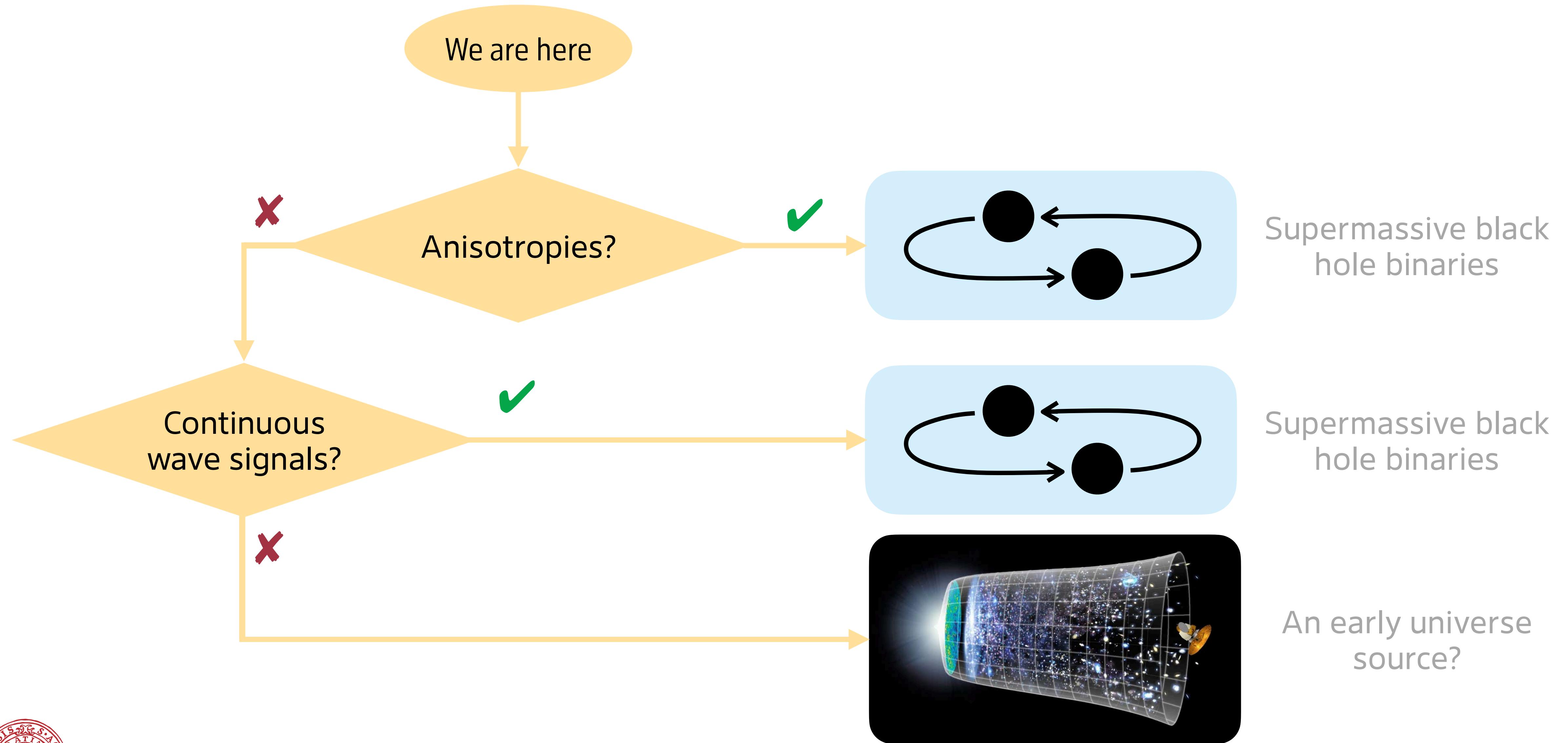
Coupled DS scenario: incl dim-6 operator for $\phi \rightarrow ee$



$\phi \rightarrow ee$ decays through a dim-6 operator open up the parameter space and save the model from potential future constraints



Grande finale: Quo vadis pulsar timing?



Time for a commercial break

In case you want to test your own phase transition models...

```
Welcome to TransitionListener v2.0!

Config
Type SinglePoint
Model models/TL_conformal_dark_u1.py
Output scans/example_point/
Format txt
Description example point, conformal U(1) model

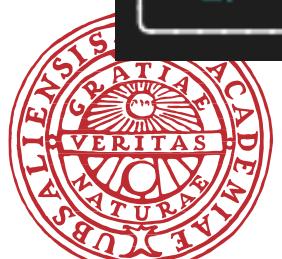
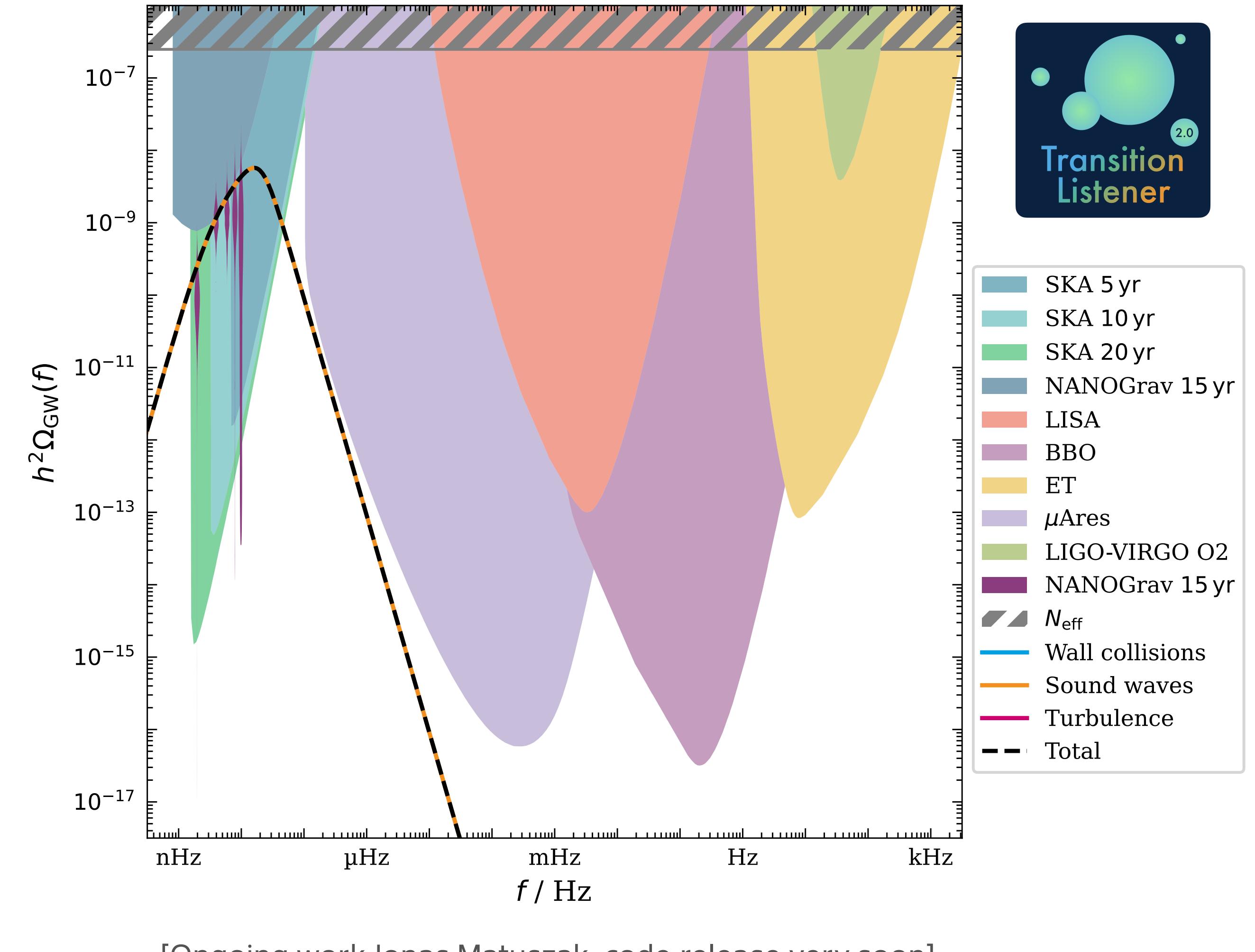
Scan parameters
Parameter Value
g 0.7
v_GeV 0.1
y 0.01

Starting analysis of example point, conformal U(1) model

Input parameters
Parameter Value
g 7.0000000000e-01
y 1.0000000000e-02
v_GeV 1.0000000000e-01

Derived parameters
Parameter Value
lambda 1.6790420728e-02

Zero-temperature mass spectrum
Particle Type Mass [GeV]
m_phi boson 2.2443542988e-02
m_varphi boson 1.2957785586e-02
m_A_T boson 7.0000000000e-02
m_A_L boson 7.0000000000e-02
m_psi1 fermion 7.0710678119e-04
m_psi2 fermion 7.0710678119e-04
```



An example for the output of TransitionListener

```
After removing redundant phases, 2 phases remain.

Found 2 phases:

Phase 0


| Parameter       | Value                |
|-----------------|----------------------|
| Tmin / GeV      | 2.35253655e-13       |
| Tmax / GeV      | 0.025860343165319342 |
| phi(Tmin) / GeV | [0.1]                |
| phi(Tmax) / GeV | [0.07745474]         |



Phase 1


| Parameter       | Value             |
|-----------------|-------------------|
| Tmin / GeV      | 2.35253655e-13    |
| Tmax / GeV      | 0.25              |
| phi(Tmin) / GeV | [-4.13835065e-10] |
| phi(Tmax) / GeV | [-2.06018231e-07] |


```

FULL GW PARAMETERS	
Parameter	Value
alpha	5.1244e+02
alpha_e	5.1263e+02
alpha_eq	9.9747e+00
alpha_hyd	5.1244e+02
alpha_inf	1.1566e+00
alpha_p	5.1237e+02
alpha_theta	5.1244e+02
betaH_from_RH	6.2224e+01
betaH_perc	6.3285e+01
c_s	5.8587e-01
c_s_bro	5.8587e-01
c_s_sym	5.7748e-01
coupled_hydrodynamics	True
D	1
g0	2
g_eff_tot_reh	1.4174e+01
h0	3.9100e+00
h_eff_tot_reh	1.4161e+01
kappa_phi	0
kappa_sw	9.9164e-01
kappa_turb	0.0000e+00
RH	7.1120e-02
step	1
Tcrit_SM_GeV	2.1734e-02
Tf_SM_GeV	2.1215e-03
Tnuc_SM_GeV	2.6768e-03
total_steps	1
Tperc	2.2124e+01
Tperc_SM_GeV	2.2124e-03
Treh	101.39173177184342
Treh_SM_GeV	1.0139e-02
v_wall	1
xi_crit	4.3499e+00
Warnings	
betaH_small	False
no_perc_splines	False
not_T0_global_min	False
too_weak_to_compute_perc	False

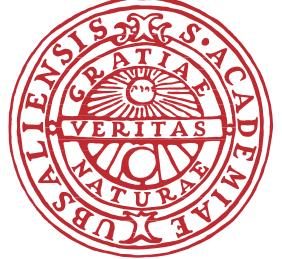
```
Found 1 possible phase transition(s) ...
First-order phase transition


| Parameter      | Value                 |
|----------------|-----------------------|
| Tnuc / GeV     | 0.0026767519252717566 |
| high phase     | 1                     |
| low phase      | 0                     |
| high vev / GeV | [-8.4332555e-11]      |
| low vev / GeV  | [0.10000133]          |
| action / GeV   | 0.4986143140000584    |

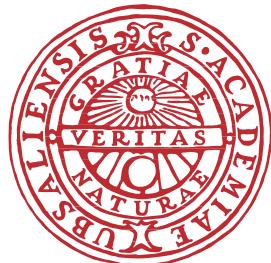
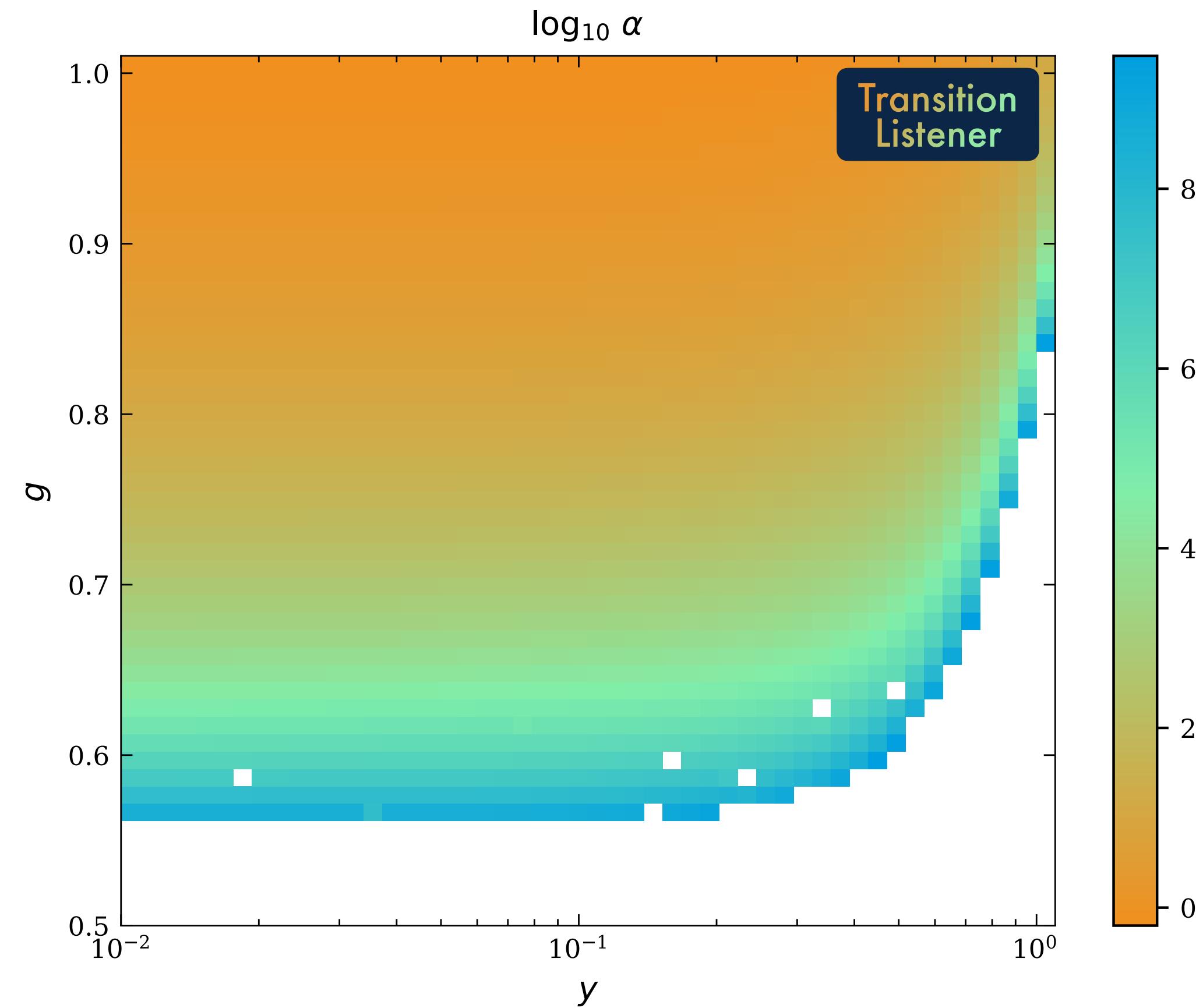

```

SNR VALUES AND OBSERVABILITY			
Detector	SNR	Should have been observed already?	Observable?
SKA_5_yrs	7.0490e+03		✓
SKA_10_yrs	8.6512e+04		✓
SKA_20_yrs	6.5400e+05		✓
EPTA_18_yrs	1.2500e+00		
NANOGrav_11_yrs	3.7351e+00	✓	
NANOGrav_15_yrs	4.7029e+00	✓	
LISA	1.4366e-08		
B-DECIGO	8.4122e-09		
DECIGO	1.1909e-08		
BBO	1.1978e-08		
ET	9.4051e-09		
muAres	5.8147e+00		
HLV_O2	4.8743e-28		
HLVK_design	3.3682e-26		

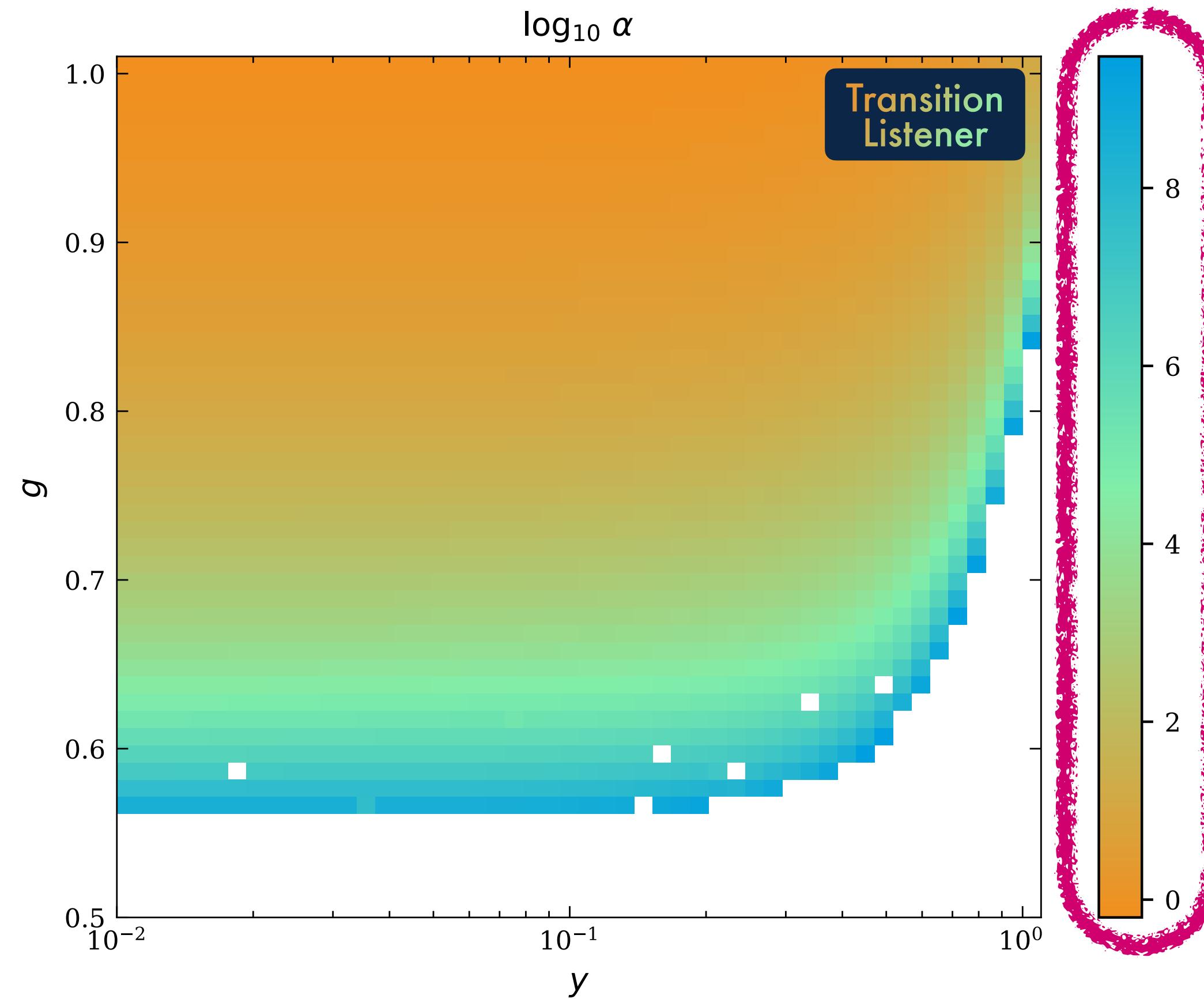
PTA	Bins	Variant	lnL	Δ lnL	σ	Within 3σ?
NANOGrav 15yr	14	PTArcade	-47.19	-55.94	0.00	✓
	14	mock	-110.02	6.89	3.71	
	14	smooth	-47.19	-55.94	0.00	
NANOGrav 15yr	5	PTArcade	-52.95	23.40	6.84	✗
	5	mock	-35.02	5.47	3.31	
	5	smooth	-35.02	5.47	3.31	
NANOGrav 12.5yr	5	PTArcade	-69.00	32.11	8.01	✗
	5	mock	-45.02	8.13	4.03	
	5	smooth	-45.02	8.13	4.03	
IPTA DR2	13	PTArcade	-31.93	-73.74	0.00	✓
	13	mock	-115.02	9.35	4.32	
	13	smooth	-31.93	-73.74	0.00	



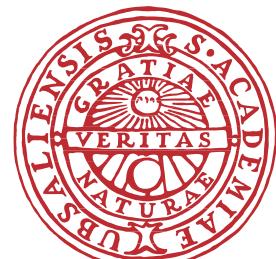
If you're not convinced yet...



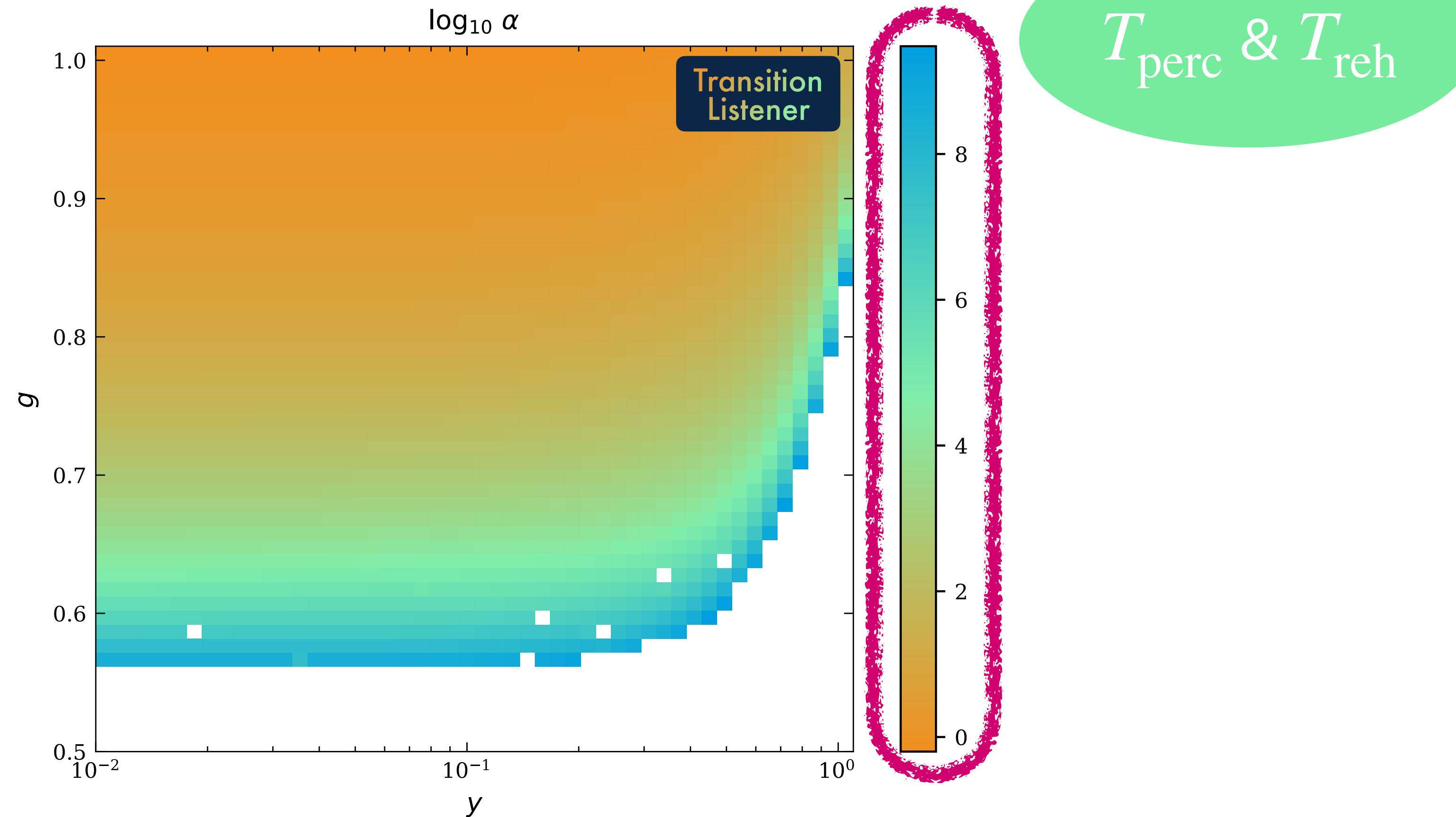
If you're not convinced yet...



Extreme supercooling with $\alpha = 10^{10}$ 



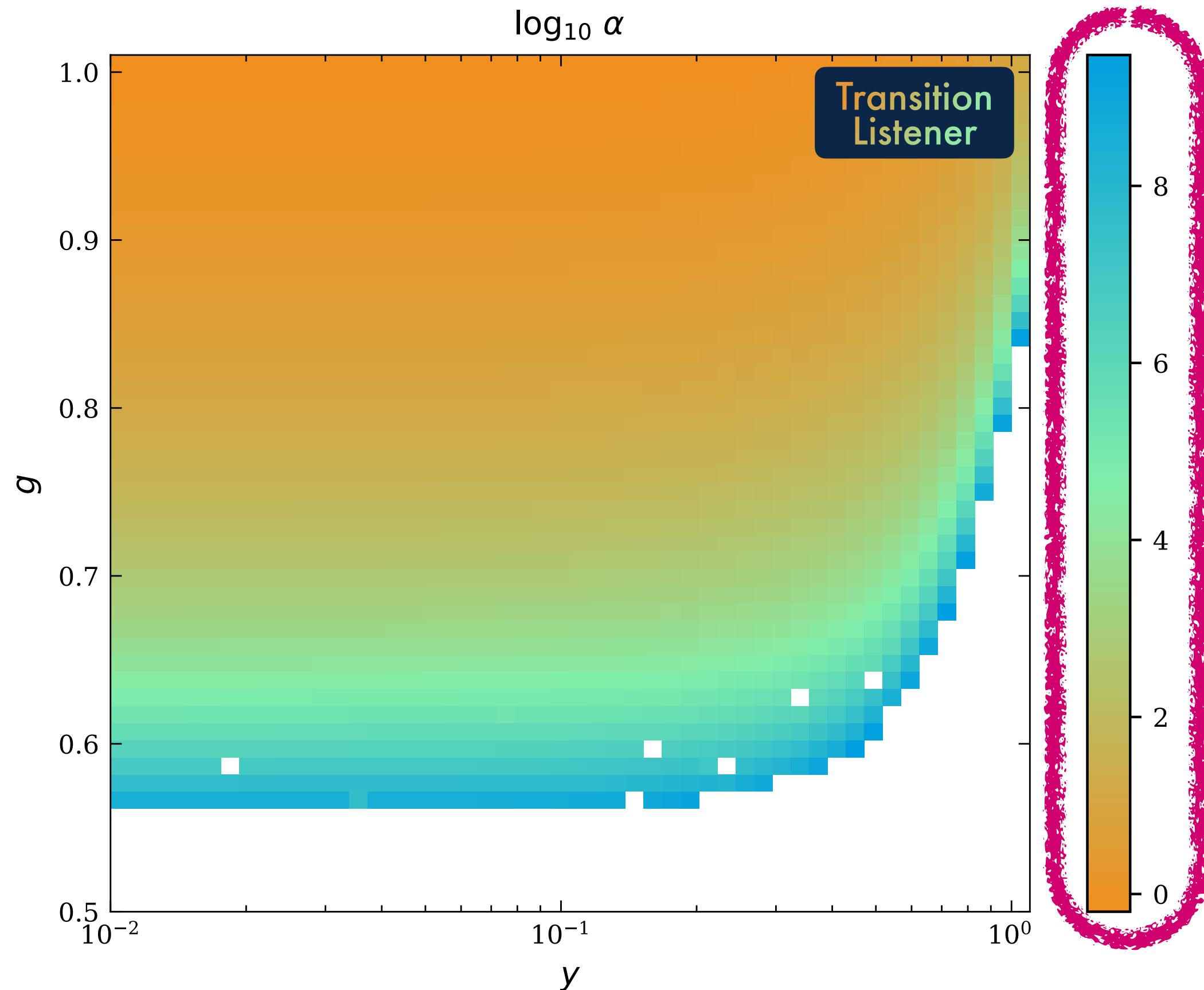
If you're not convinced yet...



Extreme supercooling with $\alpha = 10^{10}$



If you're not convinced yet...



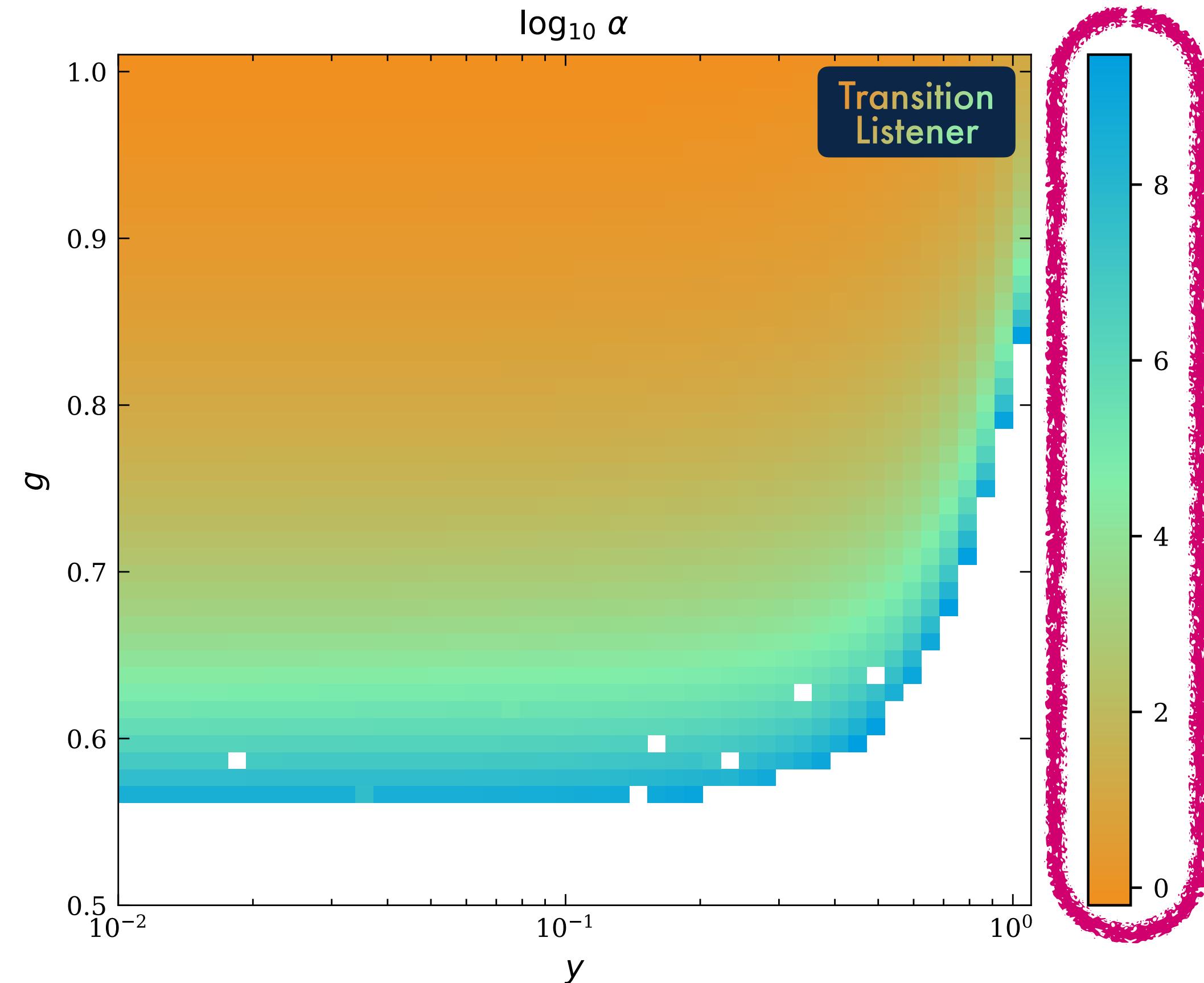
T_{perc} & T_{reh}

Extreme supercooling with $\alpha = 10^{10}$

Incl.
SM, SMEFT, dark
sectors, ...



If you're not convinced yet...



Extreme supercooling with $\alpha = 10^{10}$ 

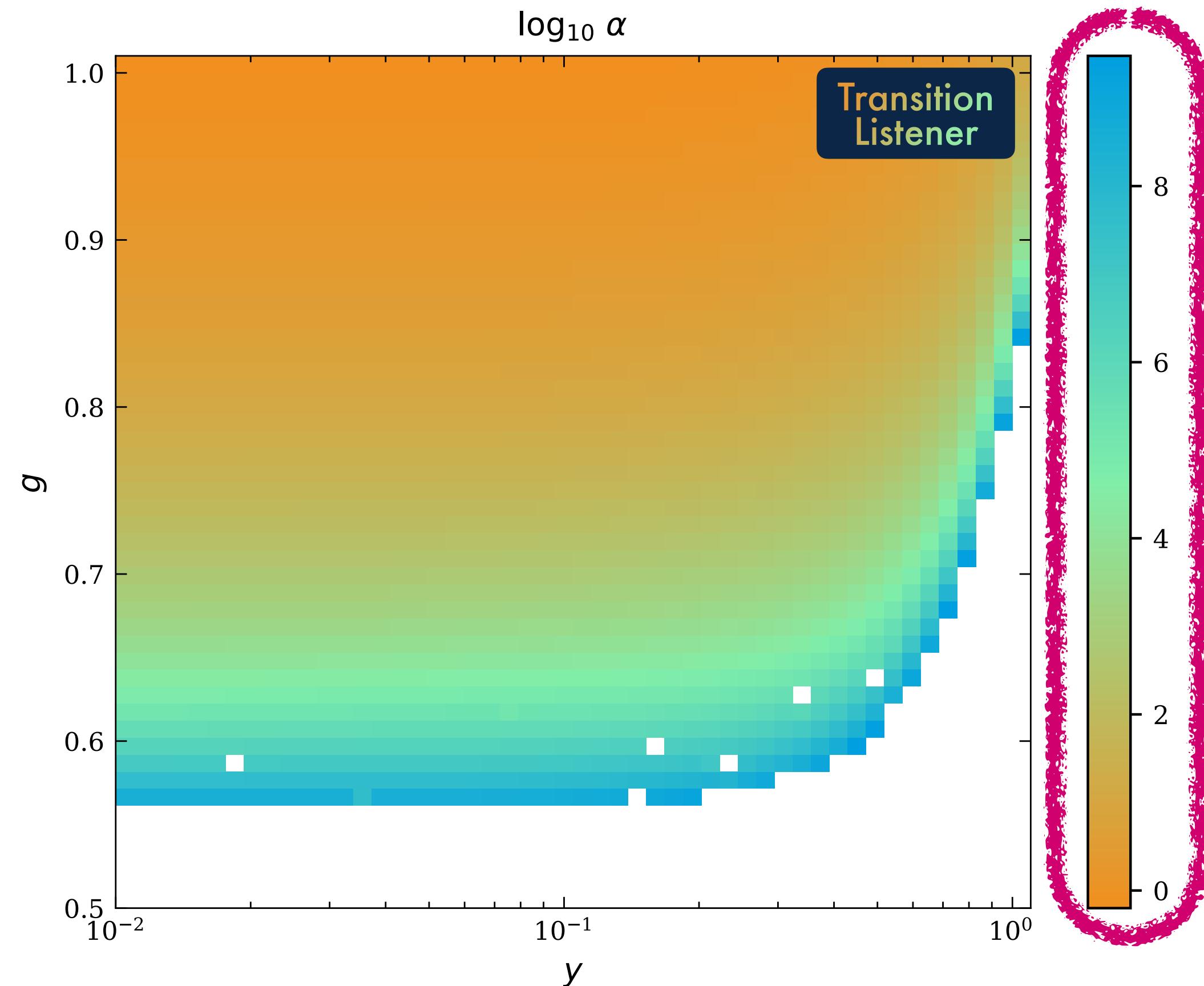
$T_{\text{perc}} \& T_{\text{reh}}$

Incl.
SM, SMEFT, dark
sectors, ...

$\mathcal{V}_{\text{wall}}$

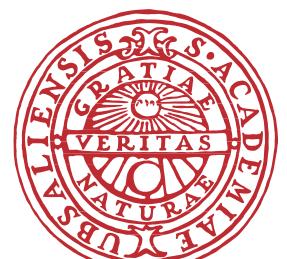


If you're not convinced yet...

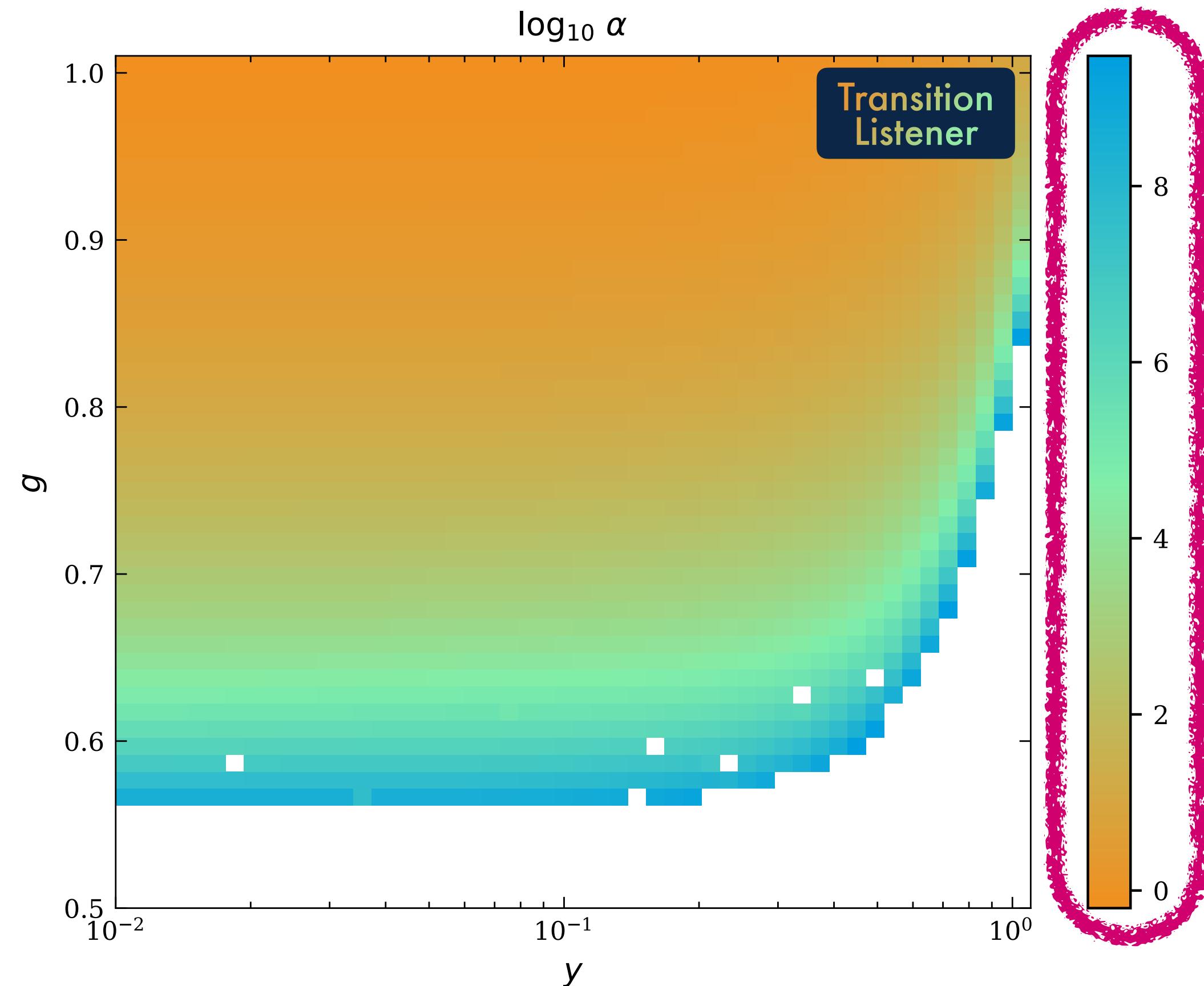


Extreme supercooling with $\alpha = 10^{10}$ 

- Documentation
- $T_{\text{perc}} \& T_{\text{reh}}$
- $\mathcal{V}_{\text{wall}}$
- Incl. SM, SMEFT, dark sectors, ...



If you're not convinced yet...



Extreme supercooling with $\alpha = 10^{10}$ 

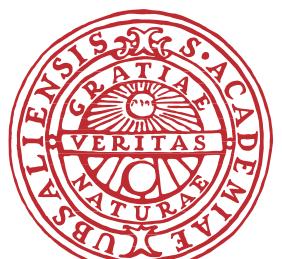
T_{perc} & T_{reh}

Documentation

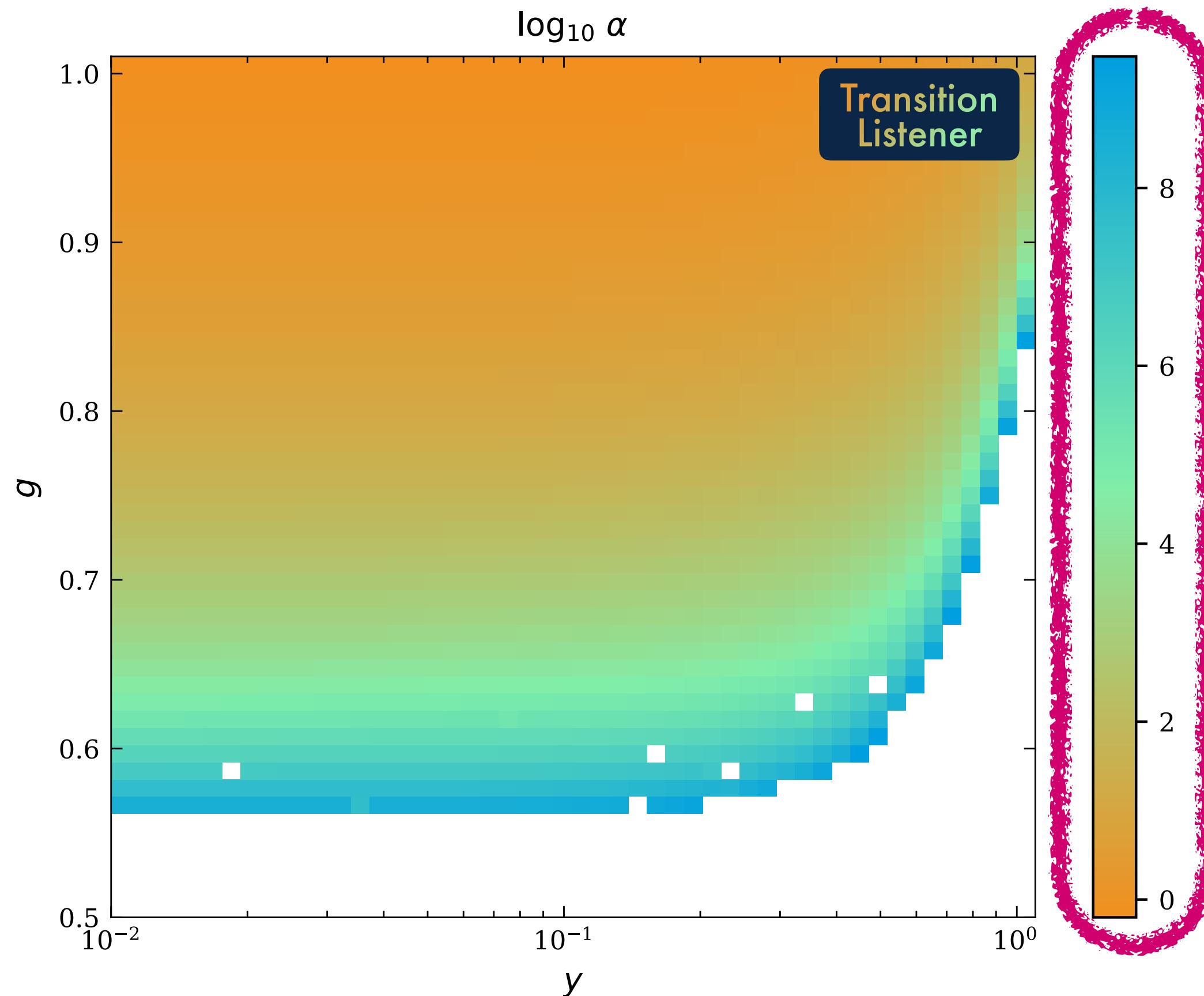
Proper error handling

$\mathcal{V}_{\text{wall}}$

Incl.
SM, SMEFT, dark
sectors, ...

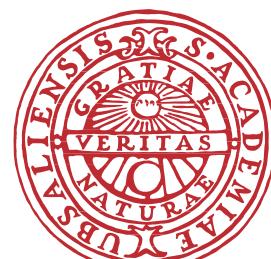


If you're not convinced yet...

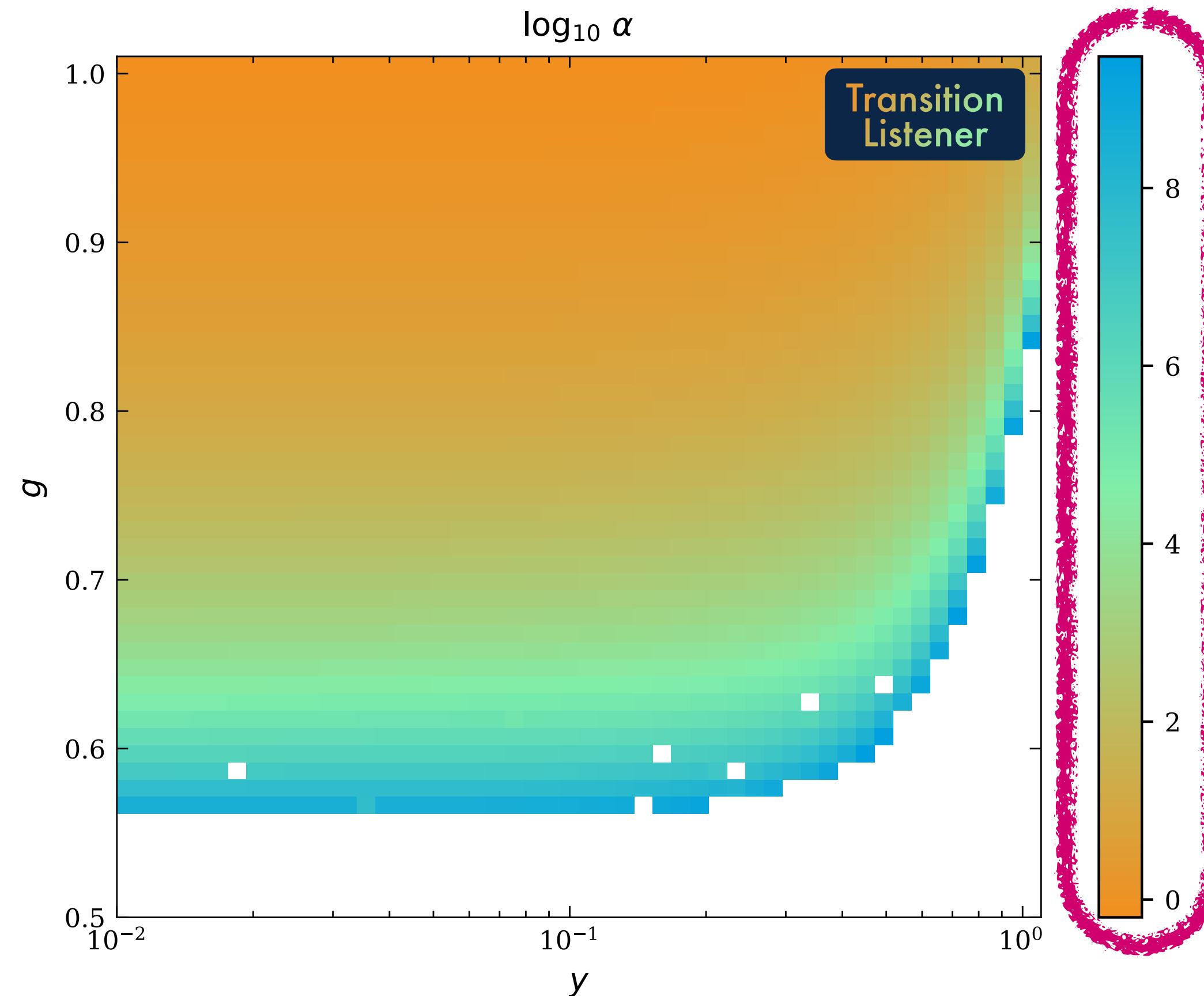


Extreme supercooling with $\alpha = 10^{10}$ 

- Documentation
- $T_{\text{perc}} \& T_{\text{reh}}$
- Proper error handling
- Not just EWSB
- $\mathcal{V}_{\text{wall}}$
- Incl. SM, SMEFT, dark sectors, ...



If you're not convinced yet...

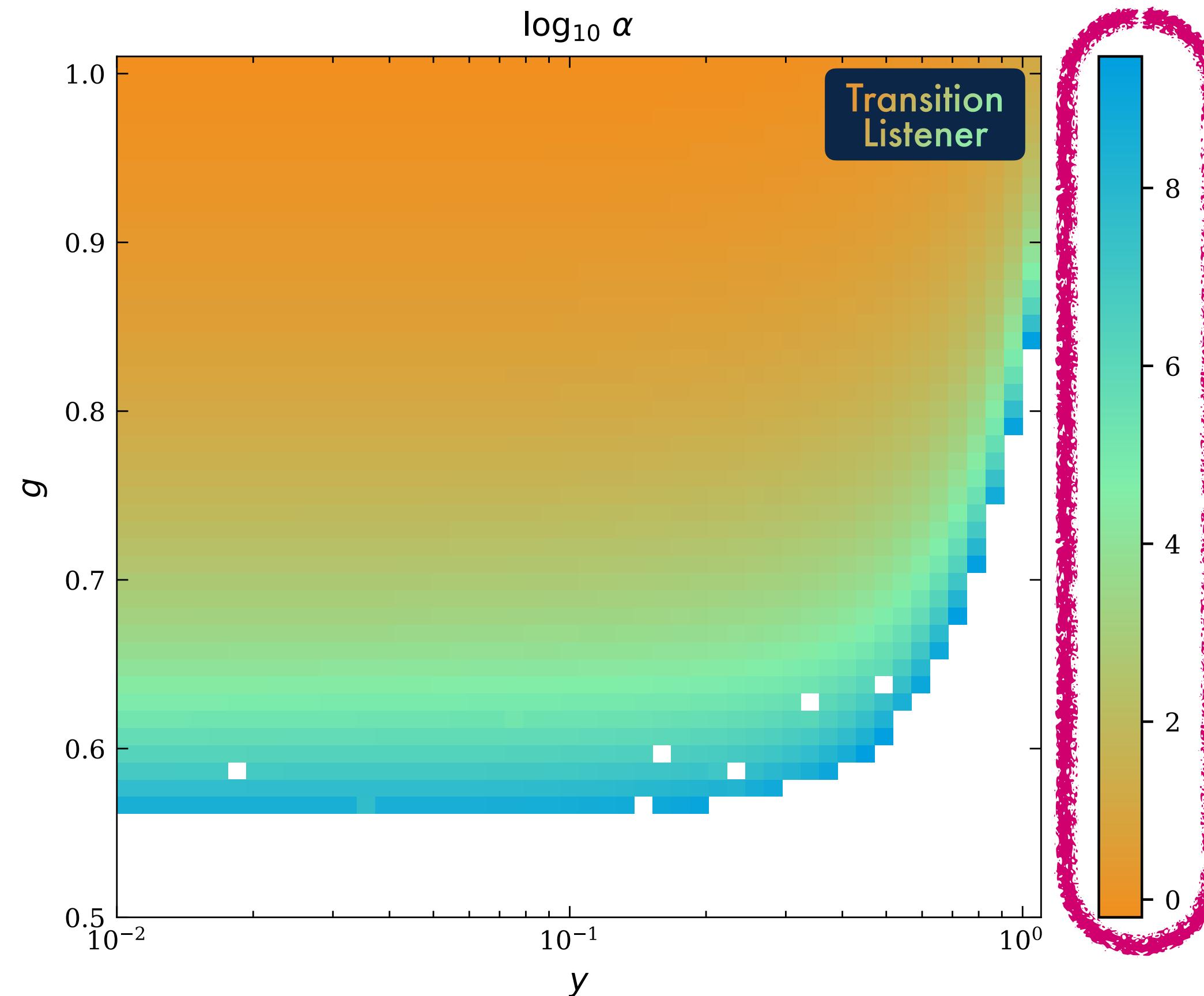


Extreme supercooling with $\alpha = 10^{10}$ 

- Documentation
- $T_{\text{perc}} \& T_{\text{reh}}$
- Proper error handling
- Not just EWSB
- $\mathcal{V}_{\text{wall}}$
- Several Higgs fields
- Incl. SM, SMEFT, dark sectors, ...

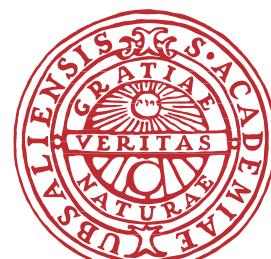


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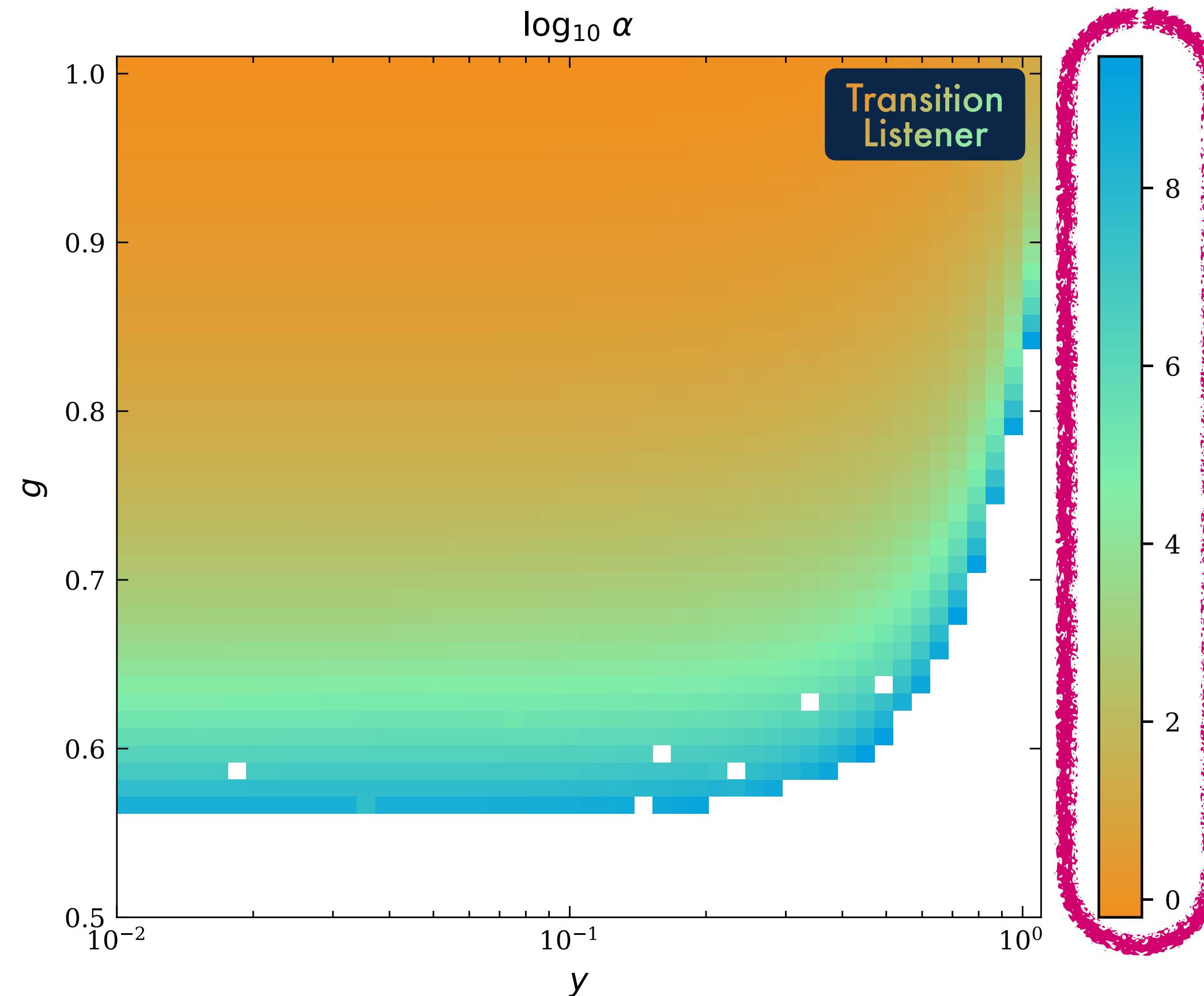


Extreme supercooling with $\alpha = 10^{10}$ 

- Documentation
- T_{perc} & T_{reh}
- Proper error handling
- Not just EWSB
- $\mathcal{V}_{\text{wall}}$
- PTA likelihoods
- Several Higgs fields
- Incl. SM, SMEFT, dark sectors, ...

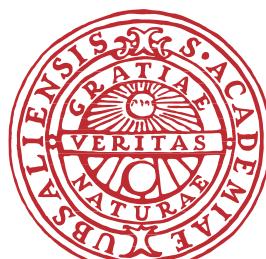


If you're not convinced yet...

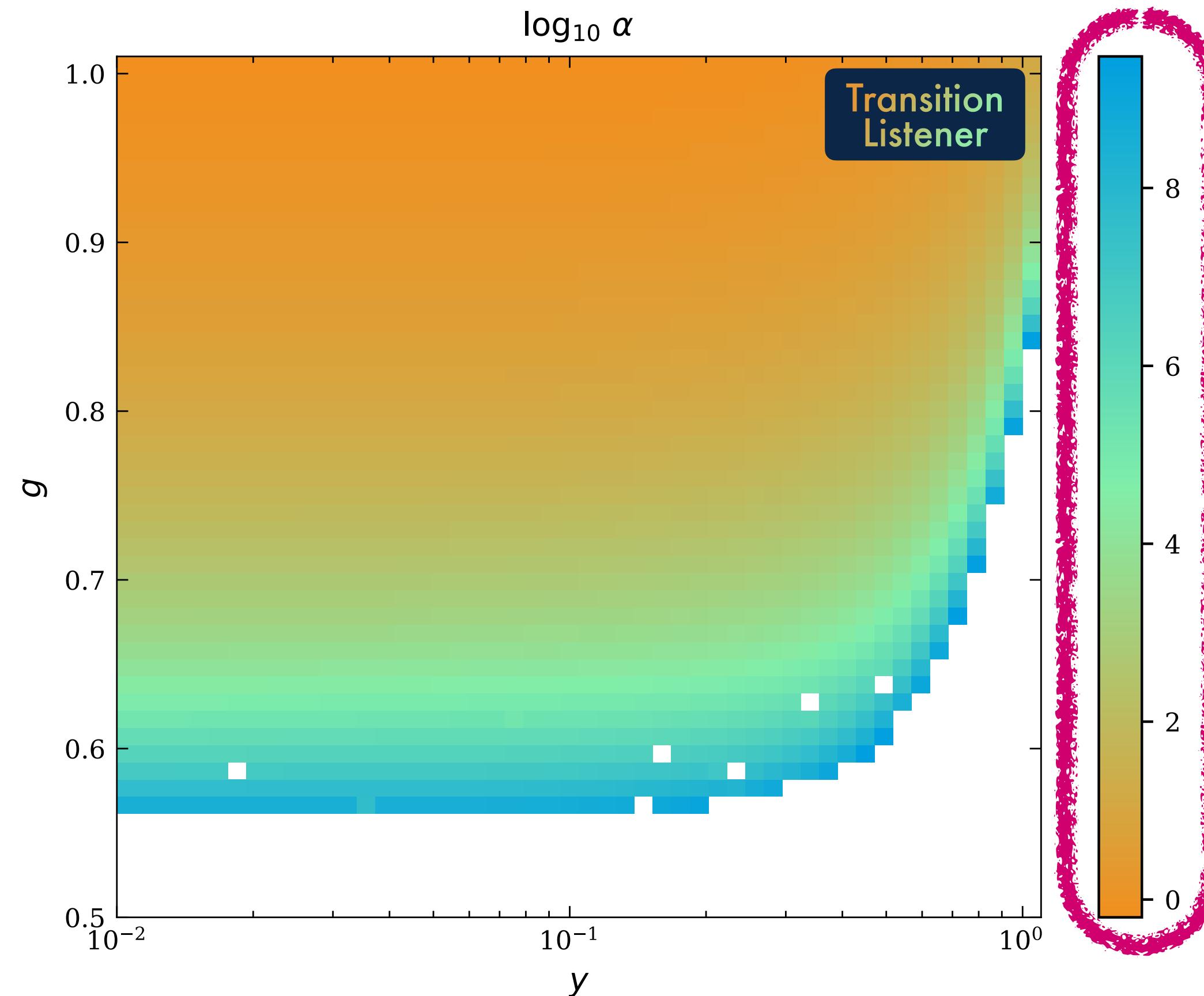


Extreme supercooling with $\alpha = 10^{10}$ 

- Documentation
- T_{perc} & T_{reh}
- Proper error handling
- Not just EWSB
- Incl. Nested sampler
- $\mathcal{V}_{\text{wall}}$
- Several Higgs fields
- PTA likelihoods
- Incl. SM, SMEFT, dark sectors, ...

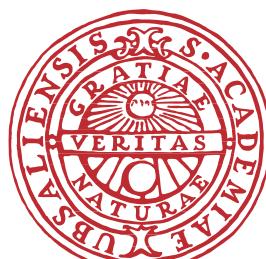


If you're not convinced yet...

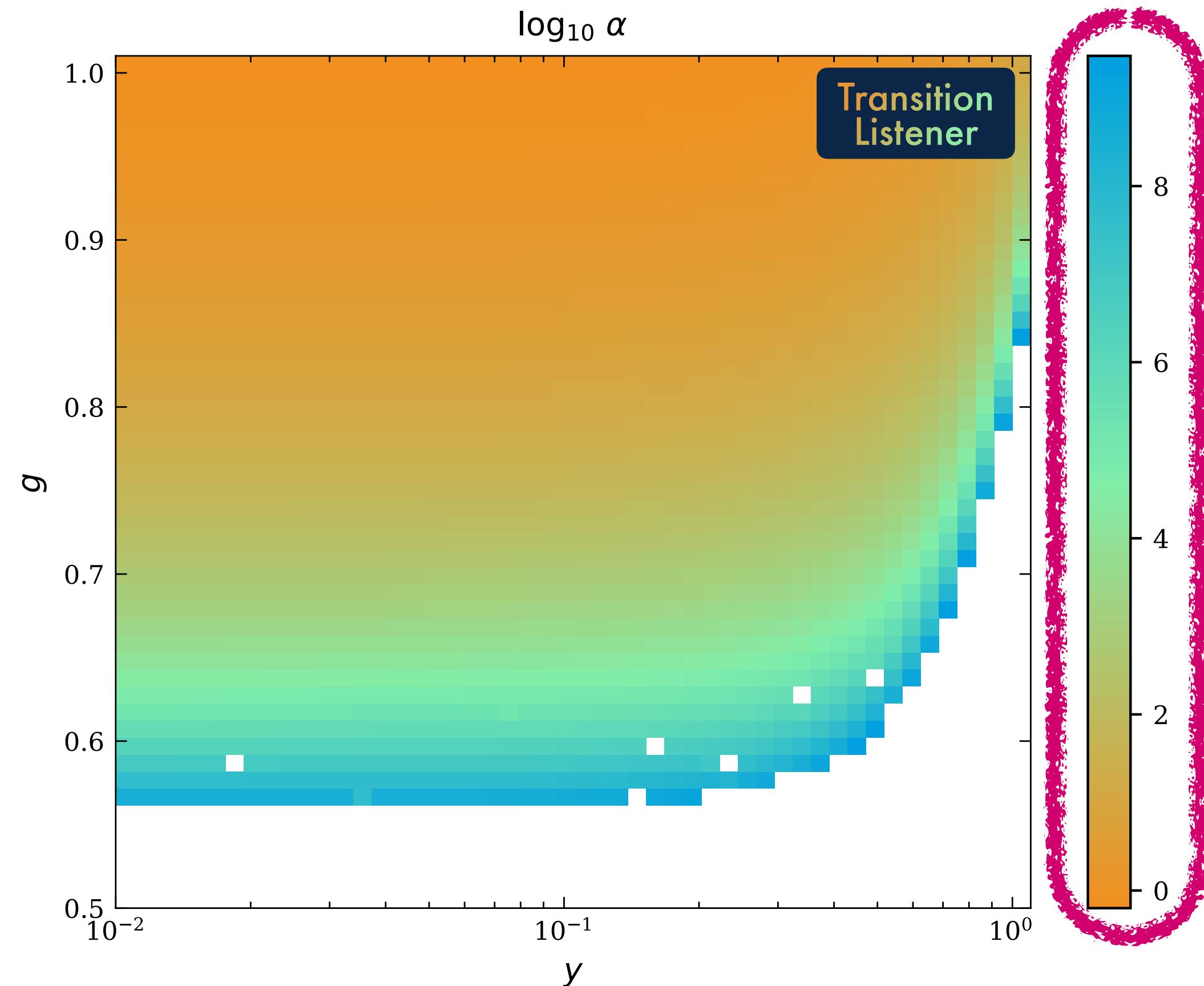


Extreme supercooling with $\alpha = 10^{10}$ 

- Documentation
- T_{perc} & T_{reh}
- Proper error handling
- Integration into GAMBIT
- Not just EWSB
- Incl. Nested sampler
- $\mathcal{V}_{\text{wall}}$
- Several Higgs fields
- PTA likelihoods
- Incl. SM, SMEFT, dark sectors, ...



If you're not convinced yet...

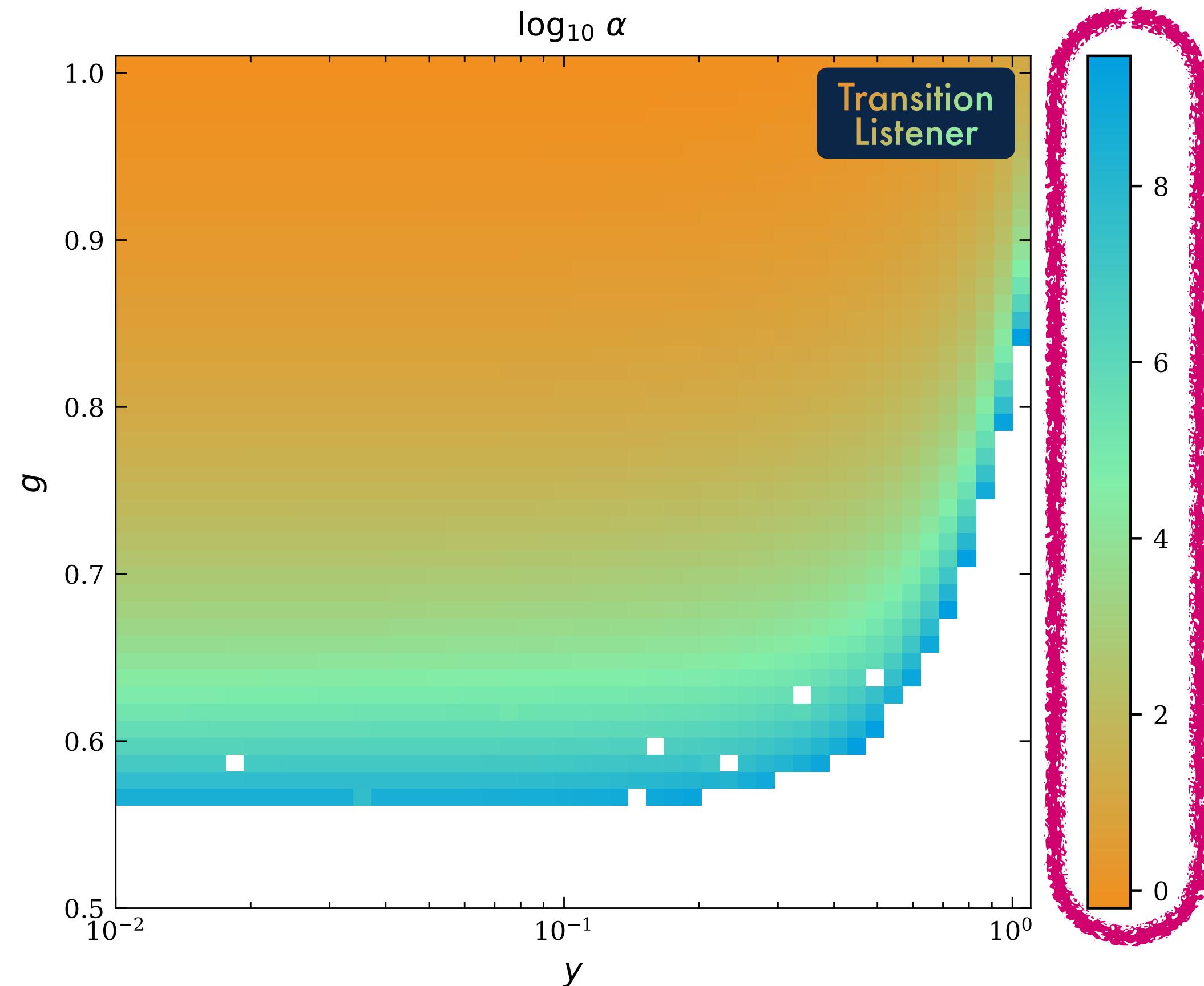


Extreme supercooling with $\alpha = 10^{10}$ 

- Documentation
- T_{perc} & T_{reh}
- Proper error handling
- Integration into GAMBIT
- Not just EWSB
- Incl. Nested sampler
- $\mathcal{V}_{\text{wall}}$
- Several Higgs fields
- Incl. SM, SMEFT, dark sectors, ...
- SNR for LISA, ET, ...

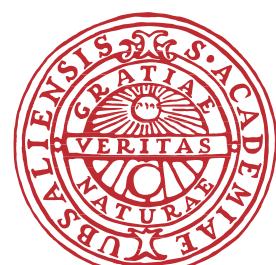


If you're not convinced yet...



Extreme supercooling with $\alpha = 10^{10}$

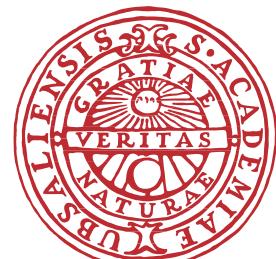
- Documentation
- T_{perc} & T_{reh}
- Proper error handling
- Integration into GAMBIT
- Not just EWSB
- Incl. Nested sampler
- ν_{wall}
- Fully modular
- Incl. SM, SMEFT, dark sectors, ...
- SNR for LISA, ET, ...
- Several Higgs fields
- PTA likelihoods



Summary



- PTAs could have observed a dark sector phase transition on top of the black hole background
 - ➡ Dark sector phase transition can explain the PTA signal **better than only SMBHBs**
 - ➡ Performed global fit with PTA, BBN, CMB, bullet cluster, and beam dump likelihoods
 - ➡ Best-fit scenarios **can be tested by upcoming beam-dump & collider experiments**
 - ➡ **Soon: TransitionListener v2**



**Thank you very much
for your attention!**

Do you have any questions?

